A General 3-D Non-Stationary 5G Wireless Channel Model

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Abstract—A novel unified framework of geometry-based stochastic models for the fifth generation (5G) wireless communication systems is proposed in this paper. The proposed general 5G channel model aims at capturing small-scale fading channel characteristics of key 5G communication scenarios, such as massive multiple-input multiple-output, high-speed train, vehicle-to-vehicle, and millimeter wave communications. It is a 3-D non-stationary channel model based on the WINNER II and Saleh-Valenzuela channel models considering array-time cluster evolution. Moreover, it can easily be reduced to various simplified channel models by properly adjusting model parameters. Statistical properties of the proposed general 5G small-scale fading channel model are investigated to demonstrate its capability of capturing channel characteristics of various scenarios, with excellent fitting to some corresponding channel measurements.

Index Terms—3D non-stationary 5G wireless channel models, massive MIMO systems, mmWave communications, high-speed train communications, V2V communications.

I. INTRODUCTION

TO SATISFY the demands of the fifth generation (5G) wireless communication networks, known as increased data rate, reduced latency, energy, and cost [1], a number of advanced technologies have been proposed in the literature as potential 5G technologies. Massive multiple-input multiple-output (MIMO), i.e., an enhanced MIMO technique with a large number of antennas, is able to greatly improve communication reliability, spectral efficiency, and energy efficiency [2]–[5]. Vehicle-to-vehicle (V2V) communications [6], [7] were proposed in the heterogeneous network architecture of 5G to enable vehicles to connect mutually without base stations. High-speed train (HST) communication also attracts attention for the emerging development of high mobility trains with speed expected to be higher than 500 km/h. Furthermore, millimeter wave (mmWave) frequency bands (30–300 GHz) have been proposed to be used for 5G wireless communications to solve the spectrum crisis problem. The mmWave frequency bands are capable of providing large bandwidth (in the order of GHz) and exploiting polarization and massive MIMO [8]–[10]. In order to design and evaluate 5G systems, a channel model which can capture channel characteristics of the above-mentioned potential technologies is essential. However, conventional channel models such as 3GPP spatial channel model (SCM) [11], the WINNER II [12], WINNER+ [13], 3GPP three dimensional (3D) SCM [14], IMT-A [15], and COST 2100 channel models [16]–[18] are not able to sufficiently meet these emerging 5G requirements. Although both large-scale fading and small-scale fading have large impacts on system performance, small-scale fading of 5G wireless channels is less studied in the literature.

The first geometry-based stochastic model (GBSM) for 5G wireless channels was proposed by the METIS project [19]. However, the METIS GBSM did not sufficiently support channel characteristics of massive MIMO, V2V, and mmWave communications [19, Table 4–1]. Later, multiple industrial partners and academic institutes formed a special interest group (SIG) and jointly published a white paper for 5G channel models [20]. This SIG white paper has covered new channel characteristics from 6 GHz to 100 GHz, such as blockage, spatial consistency, support of large bandwidth and array, and novel path loss models. The SIG white paper was then used as the guideline for the 3GPP new radio (NR) channel model for frequencies from 0.5 to 100 GHz in [21]. Based on the 3GPP NR channel model, the IMT-2020 channel model [22] was recently proposed by the ITU. The IMT-2020 channel model supports frequency bands up to 100 GHz and can cover many new features, e.g., 3D propagation, spatial consistency, large bandwidth, large antenna array, etc. Additionally, another modeling approach known as the map-based model was introduced in the METIS channel model [19], 3GPP NR channel model [21], and IMT-2020 channel model [22]. Map-based models aim at computing channel coefficients in a deterministic manner when the layout of a network is predefined. The millimetre-wave evolution for

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backhaul and access (MiWEBA) project [23] proposed a channel model combining deterministic approach based on network layout with stochastic components to model mmWave channels. However, since layouts of networks are not always accessible, GBSMs attract more attentions from researchers. Therefore, we will focus on GBSMs and small-scale fading in this paper.

A. Related Work I: GBSMs for Massive MIMO

It was reported in [24] and [25] that massive MIMO channels have some specific characteristics which were ignored in conventional MIMO (numbers of transmit and receive antennas are relatively small) channel models [12]–[18]. First, when the number of antennas is large, the distance $\mathcal{D}$ between the transmitter (cluster) and the receiver may not be larger than the Rayleigh distance $2\mathcal{L}^2/\lambda$ [26], where $\mathcal{L}$ is the dimension of the antenna array and λ is the carrier wavelength. In this case, the effect of spherical wavefront is significant and the conventional plane wavefront assumption in [12]–[15] is not well-justified. The COST 2100 channel model and the METIS GBSM can support spherical wavefronts after minor extensions. Second, cluster appearance and disappearance can occur on the array axis. As a result, each antenna may have its own set of observable clusters. This has not been considered in most advanced GBSMs such as the SCM-extension model [27], the COST 2100 channel model [16], the METIS GBSM [19], the 3GPP NR channel model [21], and the IMT-2020 channel model [22]. A two-dimensional (2D) confocal ellipse model and a 3D twin-cluster model were proposed for massive MIMO channels in [28] and [29], respectively, while a comprehensive survey of massive MIMO channel measurements and models was given in [30]. Both the ellipse model and twin-cluster model in [28] and [29] employed the spherical wavefront assumption and adapted the cluster birth-death process in [31] and [32] to both the time and array axes to characterize cluster appearance and disappearance. However, the mean power evolution of clusters and rays, directional antennas, and polarized antennas were ignored in [28] and [29]. Most importantly, channel models in [28] and [29] were not designed to accommodate mmWave channels, V2V channels, and arbitrary antenna array layouts.

B. Related Work II: GBSMs for V2V and HST

In V2V channels, the transmitter, scatterers, and receiver can be all moving. Doppler frequencies caused by either the transmitter and/or scatterers and/or receiver should be taken into account. Wideband 2D GBSMs for V2V channels were proposed and validated via measurements in [33]–[35], where clusters were categorized into mobile clusters and static clusters. In V2V communications, transmitters and receivers may be lower than clusters on surrounding buildings. Therefore, 3D clusters were included in [36]–[38]. A 3D concentric-cylinder V2V channel model was introduced in [36], while 3D GBSMs combining a two-sphere model and an elliptic-cylinder model were proposed in [37] and [38]. Recently, birth-death process was used to model cluster dynamics in V2V channels in [39]. For HST communications, relevant

non-stationary GBSMs can be found in [40]–[43] and some measurement results were given in [44]. The non-stationary channel behavior of HST systems is similar to that of V2V channels with large Doppler frequencies. However, cluster evolution on the time axis was ignored in the METIS GBSM [19], 3GPP NR channel model [21], IMT-2020 channel model [22], and models in [33]–[39]. Thus, it is difficult to track the channel with respect to time in a continuous manner.

C. Related Work III: GBSMs for mmWave

As the supported bandwidth for mmWave is large (in the order of GHz [8]–[10]), GBSMs for mmWave channels need to consider high delay resolution, i.e., rays within a cluster may be resolvable and the numbers of rays within clusters may vary. The GBSM of the METIS channel model [19] supports frequency bands up to 70 GHz. However, the resolvable rays within clusters and the varying numbers of rays within clusters were not included. The quasi deterministic radio channel generator (QuaDRiGa) channel model [46] was used as the initial model for mmWave channels in the mmWave based mobile radio access network for 5G integrated communications (mmMAGIC) project [45]. However, it also ignored the resolvable rays and varying numbers of rays within clusters. The Saleh-Valenzuela (SV) channel model [47], which was originally proposed for indoor multipath propagations, has been used to evaluate system performance in the IEEE wireless personal area network (PAN) standard [48]–[51] with the supported bandwidth over 500 MHz. Since mmWave channels are expected to have bandwidths over 500 MHz, applications of the SV channel model to mmWave channels can be found in [52]–[56]. In a SV channel model, the number of rays within each cluster was assumed to follow a Poisson distribution. Complex gain and delay were assigned to each ray. A 3D mmWave channel model with random numbers of clusters and paths within each cluster was proposed in [57]. However, in the above SV-based mmWave channel models, time evolution and mean ray power evolution have not sufficiently been studied.

D. Contributions

To address the abovementioned research gaps, this paper has the following contributions [58].

1) A general 3D non-stationary 5G GBSM for terrestrial wireless communication systems is proposed, having the capability of simulating massive MIMO, V2V, HST, and mmWave small-scale fading channels [58]. It also considers time evolution of channels with all the model parameters as time varying. The proposed general 5G channel model is based on the WINNER II channel model [12], in order to keep consistency of 4G and 5G channel models, and the SV channel model in order to support the high delay resolution of mmWave channels [48]–[51]. Spherical wavefront and array-time cluster evolution are included to represent massive MIMO channel characteristics. Array-time evolution includes cluster birth-death process in both the array and time axes and geometrical relationship updates. The mean power updates of rays are also embedded in the proposal 5G
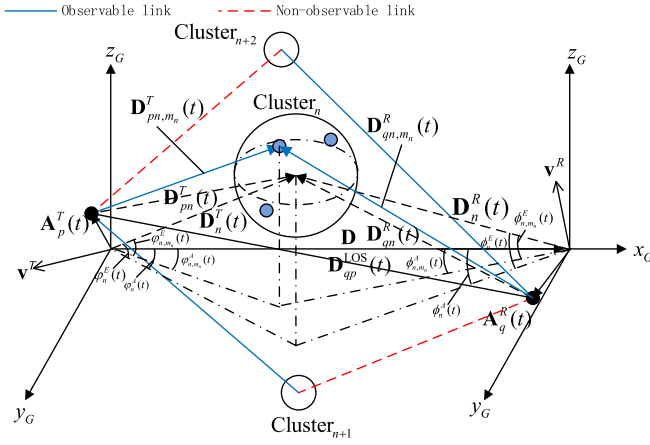
Fig. 1. A general 3D non-stationary 5G GBSM.

small-scale fading channel model with the assumption of the inverse square law.

2) The proposed general 5G GBSM can easily be reduced to various simplified channel models by setting proper channel parameters, which is demonstrated by fitting some statistical properties to the corresponding channel measurement data.

The rest of this paper is organized as follows. Section II gives a general description of the proposed unified framework for 5G small-scale fading channel models. Statistical properties of the proposed general 3D 5G GBSM are investigated in Section III. Simulation/numerical results and analysis are presented in Section IV. Conclusions are drawn in Section V.

II. A GENERAL 3D NON-STATIONARY 5G SMALL-SCALE FADING CHANNEL MODEL

Let us consider a MIMO system with M_R receive and M_T transmit antennas communicating at carrier frequency f_c. Let Ant_q^R denote the qth receive antenna and Ant_p^T denote the pth transmit antenna. Also, let Cluster_n denote the nth cluster. It should be noted that arbitrary antenna array layouts are assumed in the proposed model. Typical antenna array layouts include uniform linear arrays, 2D planar arrays, and 3D cube arrays. Antenna responses can be modified subject to actual antenna settings. The scattering environment between the transmitter and receiver is abstracted as effective clusters [12], which characterize the first and last bounces of the channel. Multi-bounces between the first and last bounces are abstracted by a virtual link. The proposed general 3D non-stationary 5G GBSM is illustrated in Fig. 1. It should be noticed that (x_G, y_G, z_G) axes are established as the global coordinate system (GCS) with origin at the center of the transmit array. This needs to be distinguished from the local coordinate systems (LCSs) with origins at the centers of transmit and receive arrays when calculating antenna pattern in a 3–D space. Spherical wavefront and cluster appearance and disappearance are assumed in order to support massive MIMO scenarios. In this case, each antenna may have its own set of observable clusters. Let $C_q^R(t)$ and $C_p^T(t)$ represent the cluster sets of Ant_q^R and

Ant_p^T at time t, respectively. Then, the total number of clusters $N(t)$ observable by both the transmitter and receiver at time t can be calculated as $N(t) = \text{card}\left(\bigcup\limits_{p=1}^{M_T} \bigcup\limits_{q=1}^{M_R} S_{qp}(t) \right)$ where $S_{qp}(t) = C_q^R(t) \bigcap C_p^T(t)$, card$(S)$ denotes the cardinality of the set S, $\bigcup$ and $\bigcap$ denote the union and intersection of sets, respectively. Also, both the transmitter and receiver are assumed to be in motion to support V2V scenarios, which results in Doppler frequencies at both sides. In addition, rays within clusters are considered to be resolvable in order to support the high time resolution in mmWave scenarios. Complex gain and delay should be assigned to each ray.

Let $\mathbf{A}_q^R(t)$ and $\mathbf{A}_p^T(t)$ denote the position vectors of Ant_q^R and Ant_p^T, respectively. Also, let ψ_A^R and ψ_E^R be azimuth and elevation angles of the receive array broadside, and let ψ_A^T and ψ_E^T be azimuth and elevation angles of the transmit array broadside, respectively. Let $\mathbf{D}$ denote the initial position vector of the receiver and is assumed to equal $[D, 0, 0]^T$, and D is the initial distance between the transmitter and receiver centers. The line-of-sight (LOS) distance vector $\mathbf{D}_{qp}^{\text{LOS}}(t)$ between Ant_q^R and Ant_p^T is computed as

$$\mathbf{D}_{qp}^{\text{LOS}}(t) = \mathbf{A}_q^R(t) - \mathbf{A}_p^T(t). \tag{1}$$

According to the geometrical relationships in Fig. 1 and the key parameters listed in Table I, distance vectors of Cluster_n at the transmitter and receiver are calculated as

$$\mathbf{D}_n^R(t) = D_n^R(t) \begin{bmatrix} \cos\phi_n^E(t)\cos\phi_n^A(t) \\ \cos\phi_n^E(t)\sin\phi_n^A(t) \\ \sin\phi_n^E(t) \end{bmatrix}^T + \mathbf{D} \tag{2}$$

$$\mathbf{D}_n^T(t) = D_n^T(t) \begin{bmatrix} \cos\varphi_n^E(t)\cos\varphi_n^A(t) \\ \cos\varphi_n^E(t)\sin\varphi_n^A(t) \\ \sin\varphi_n^E(t) \end{bmatrix}^T \tag{3}$$

where $D_n^R(t)$ and $D_n^T(t)$ are the Frobenius norms of $\mathbf{D}_n^R(t)$ and $\mathbf{D}_n^T(t)$, respectively. Distance vectors of the m_nth ray of Cluster_n to the transmitter and receiver centers are calculated as

$$\mathbf{D}_{n,m_n}^R(t) = D_n^R(t) \begin{bmatrix} \cos\phi_{n,m_n}^E(t)\cos\phi_{n,m_n}^A(t) \\ \cos\phi_{n,m_n}^E(t)\sin\phi_{n,m_n}^A(t) \\ \sin\phi_{n,m_n}^E(t) \end{bmatrix}^T + \mathbf{D} \tag{4}$$

$$\mathbf{D}_{n,m_n}^T(t) = D_n^T(t) \begin{bmatrix} \cos\varphi_{n,m_n}^E(t)\cos\varphi_{n,m_n}^A(t) \\ \cos\varphi_{n,m_n}^E(t)\sin\varphi_{n,m_n}^A(t) \\ \sin\varphi_{n,m_n}^E(t) \end{bmatrix}^T. \tag{5}$$

Distance vectors between the m_nth ray of Cluster_n and antenna elements are calculated as

$$\mathbf{D}_{qn,m_n}^R(t) = \mathbf{D}_{n,m_n}^R(t) - \mathbf{A}_q^R(t) \tag{6}$$

$$\mathbf{D}_{pn,m_n}^T(t) = \mathbf{D}_{n,m_n}^T(t) - \mathbf{A}_p^T(t). \tag{7}$$

It should be noticed that position vectors are all time dependent. After all vectors are obtained in the 3D space, the channel impulse response can be derived.

TABLE I

DEFINITIONS OF KEY 5G CHANNEL MODEL PARAMETERS

ψ_A^R, ψ_E^R	azimuth and elevation angles of the receive array broadside
ψ_A^T, ψ_E^T	azimuth and elevation angles of the transmit array broadside
$N(t)$	total number of observable clusters
M_n	number of rays within Cluster_n
$C_q^R(t), C_p^T(t)$	cluster set of Ant_q^R and cluster set of Ant_p^T
$S_{qp}(t)$	set of clusters observable for both Ant_q^R and Ant_p^T
$\phi_n^A(t), \phi_n^E(t)$	azimuth and elevation angles between Cluster_n and the receive array center
$\varphi_n^A(t), \varphi_n^E(t)$	azimuth and elevation angles between Cluster_n and the transmit array center
$\phi_{n,m_n}^A(t), \phi_{n,m_n}^E(t)$	azimuth and elevation angles between the m_nth ray of Cluster_n and the receive array center
$\varphi_{n,m_n}^A(t), \varphi_{n,m_n}^E(t)$	azimuth and elevation angles between the m_nth ray of Cluster_n and the transmit array center
$\mathbf{A}_q^R(t), \mathbf{A}_p^T(t)$	3D position vectors of Ant_q^R and Ant_p^T
$\mathbf{D}_n^R(t), \mathbf{D}_n^T(t)$	3D distance vectors between Cluster_n and the receiver (transmitter) array center
$\mathbf{D}_{n,m_n}^R(t), \mathbf{D}_{n,m_n}^T(t)$	3D distance vectors between Cluster_n and the receive (transmit) array center via the m_nth ray
$\mathbf{D}_{qn,m_n}^R(t), \mathbf{D}_{pn,m_n}^T(t)$	3D distance vectors between Cluster_n and Ant_q^R (Ant_p^T) via the m_nth ray
$f_{qn,m_n}^R(t), f_{pn,m_n}^T(t)$	Doppler frequencies of Ant_q^R (Ant_p^T) via Cluster_n and the m_nth ray
$\mathbf{D}_{qp}^{\text{LOS}}(t)$	3D distance vector of the LOS component between Ant_q^R and Ant_p^T
$f_{pq}^{\text{LOS}}(t)$	Doppler frequency of the LOS component between Ant_q^R and Ant_p^T
$\mathbf{v}^R, \mathbf{v}^T$	3D velocity vectors of the receive and transmit arrays
$\mathbf{v}_n^R, \mathbf{v}_n^T$	3D velocity vectors of the last bounce and first bounce of Cluster_n
$P_{n,m_n}(t)$	mean power of the m_nth ray of Cluster_n
$\mathbf{D}$	3D distance vector between the receive and transmit array centers
K	Rician factor
$\tilde{\lambda}$	mean number of rays within a cluster
κ	cross polarization power ratio
λ_G, λ_R	generation rate and recombination rate of clusters

A. Channel Impulse Response

Based on the WINNER II and SV channel models, the proposed 5G GBSM at time t with delay τ can be characterized by an $M_R \times M_T$ matrix $\mathbf{H}(t, \tau) = [h_{qp}(t, \tau)]$. The entries of $\mathbf{H}(t, \tau)$ consist of two components, i.e., the LOS component and the non-LOS (NLOS) component, and can be written as

$$
\begin{aligned}
& h_{qp}(t, \tau) \\
&= \underbrace{\sqrt{\frac{K(t)}{K(t)+1}} h_{qp}^{\text{LOS}}(t) \delta\left(\tau - \tau^{\text{LOS}}(t)\right)}_{\text{LOS}} \\
&+ \underbrace{\sqrt{\frac{1}{K(t)+1}} \sum_{n=1}^{N(t)} \sum_{m_n=1}^{M_n(t)} h_{qp,n,m_n}(t) \delta\left(\tau - \tau_n(t) - \tau_{m_n}(t)\right)}_{\text{NLOS}}.
\end{aligned}
$$

$$(8)$$

In (8), $K(t)$ is the Rician factor, $N(t)$ is the time variant number of clusters, $M_n(t)$ is the number of rays within Cluster_n, $\tau_n(t)$ is the delay of Cluster_n, and $\tau_{m_n}(t)$ is the relative delay of the m_nth ray in Cluster_n. It is important to mention that all the parameters of the proposed 5G GBSM are time-variant, which has the capability to model the time-evolution and high mobility features of channels and is essentially a nonstationary channel model. To simplify the model, we assume that the Rician factor and relative delays are constants during the generation of channel coefficients, i.e., $K(t) = K$ and $\tau_{m_n}(t) = \tau_{m_n}$. These may not hold in certain scenarios such as the HST cutting scenario where the Rician factor is changing with time [59]. However, the cutting scenario is not frequently occurring in 5G scenarios and it is of high complexity. Also,

the number of rays within a cluster is assumed to follow a Poisson distribution $\text{Pois}\left(\tilde{\lambda}\right)$ [54], i.e., $M_n(t) = M_n = \max\left\{\text{Pois}\left(\tilde{\lambda}\right), 1\right\}$, where $\tilde{\lambda}$ is both the mean and variance of M_n and $\max\{\cdot\}$ calculates the maximum value. Each ray within a cluster has its own complex gain and delay to support mmWave channels in the proposed 5G GBSM.

For the LOS component, if polarized antenna arrays are assumed at both the receiver and transmitter sides, the complex channel gain $h_{qp}^{\text{LOS}}(t)$ is presented as (9), as shown at the bottom of the next page, where Φ_{LOS} is uniformly distributed within $(0, 2\pi]$ [14]. The superscripts V and H denote vertical polarization and horizontal polarization, respectively. Functions $F^T(\mathbf{a}, \mathbf{b})$ and $F^R(\mathbf{a}, \mathbf{b})$ are antenna patterns with input vectors $\mathbf{a}$ and $\mathbf{b}$ in the GCS. The input vectors $\mathbf{a}$ and $\mathbf{b}$ need to be transformed into the LCS to obtain the antenna patterns. Detailed calculations are presented in Appendix A [14] and the antenna pattern functions can be modified according to practical antenna settings. For large bandwidth support, the antenna patterns can be frequency dependent. In this case, the antenna patterns can be implemented accordingly in this model as well. The Doppler frequency $f_{qp}^{\text{LOS}}(t)$ between Ant_q^R and Ant_p^T of the LOS component is expressed as

$f_{qp}^{\text{LOS}}(t) = \frac{1}{\lambda} \frac{\left\langle \mathbf{D}_{qp}^{\text{LOS}}(t), \mathbf{v}^R - \mathbf{v}^T \right\rangle}{\left\| \mathbf{D}_{qp}^{\text{LOS}}(t) \right\|}$ where $\langle \cdot, \cdot \rangle$ is the inner product operator, $\| \cdot \|$ calculates the Frobenius norm, and λ is the wavelength with respect to the central carrier frequency. Given the speed of light c, the delay $\tau^{\text{LOS}}(t)$ of the LOS component is computed as $\tau^{\text{LOS}}(t) = \|\mathbf{D}(t)\| / c$.

For NLOS components, if Cluster_n is observable to Ant_q^R and Ant_p^T, i.e., $\text{Cluster}_n \in S_{qp}(t)$, the complex channel gain is expressed as (10), as shown at the bottom of the next page,

where κ is the cross polarization power ratio and P_{n,m_n} is the normalized mean power of the m_nth ray in Cluster$_n$. The normalized mean power of Cluster$_n$ can be calculated as $P_n = \sum_{m_n} P_{n,m_n}$. Random phases $\Phi_{n,m_n}^{\mathrm{VV}}$, $\Phi_{n,m_n}^{\mathrm{VH}}$, $\Phi_{n,m_n}^{\mathrm{HV}}$, $\Phi_{n,m_n}^{\mathrm{HH}}$ are uniformly distributed within $(0, 2\pi]$ [12].

Conversely, if Cluster$_n$ is not observable, i.e., Cluster$_n \notin S_{qp}(t)$, the complex channel gain $h_{qp,n,m_n}(t) = 0$. Accordingly, the Doppler frequencies at the receiver and transmitter are calculated as

$$f_{qn,m_n}^R(t) = \frac{1}{\lambda} \frac{\left\langle \mathbf{D}_{qn,m_n}^R(t), \mathbf{v}^R - \mathbf{v}_n^R \right\rangle}{\left\| \mathbf{D}_{qn,m_n}^R(t) \right\|} \tag{11}$$

$$f_{pn,m_n}^T(t) = \frac{1}{\lambda} \frac{\left\langle \mathbf{D}_{pn,m_n}^T(t), \mathbf{v}^T - \mathbf{v}_n^T \right\rangle}{\left\| \mathbf{D}_{pn,m_n}^T(t) \right\|}. \tag{12}$$

Moreover, the delay $\tau_n(t)$ of the NLOS component is computed as

$$\tau_n(t) = \left[\left\| \mathbf{D}_n^R(t) \right\| + \left\| \mathbf{D}_n^T(t) \right\| \right] / c + \tilde{\tau}_n(t) \tag{13}$$

where $\tilde{\tau}_n(t)$ is an exponentially distributed random variable representing the virtual delay caused by the virtual link between the first and last bounces of Cluster$_n$ in the scattering environment. The time evolution of virtual delays will be introduced in Section II-D.

B. Array-Time Cluster Evolution for the General 3D 5G GBSM

The array-time cluster evolution for the proposed unified 5G GBSM framework is developed based on the birth-death process and the algorithm described in [29]. However, the proposed algorithm for the unified 5G GBSM framework in Fig. 2 improves the one in [29] by including mean power evolution and updates of rays within clusters. Let us assume the generation (birth) and recombination (death) rates of clusters are λ_G and λ_R, respectively. Then, the array-time cluster evolution for the unified 5G GBSM framework can be described as follows.

Step 1: An initial set of clusters are generated at time t. The generation procedure of initial clusters will be described in Section II-C.

Step 2: At time $t + \Delta t$, cluster evolution on the time axis is operated. In principle, each cluster should have its own survival probability according to the relative motion. However, for simplicity, mean relative velocities of clusters will be used to calculate survival probabilities of clusters.
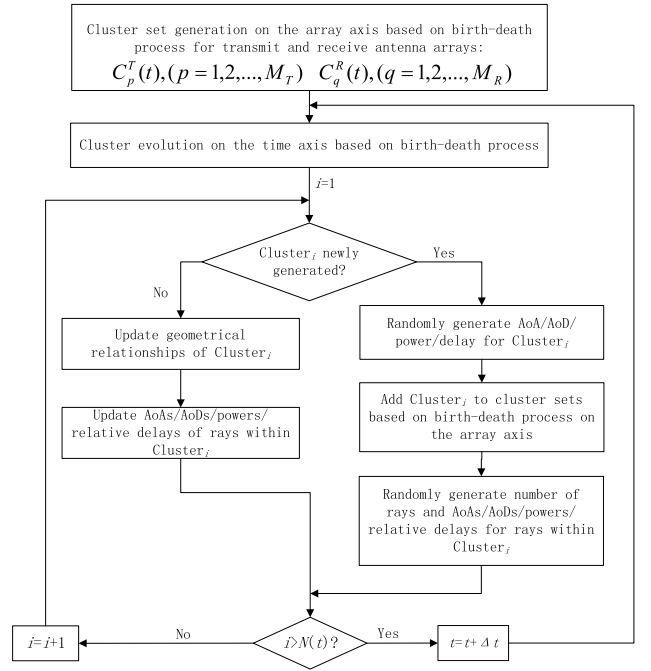

Fig. 2. Flowchart of the array-time cluster evolution for the proposed general 3D non-stationary 5G GBSM.

Mean relative velocities Δv^R and Δv^T are characterized as $\Delta v^R = \mathrm{E}\left[\left\| \mathbf{v}^R - \mathbf{v}_n^R \right\| \right]$ and $\Delta v^T = \mathrm{E}\left[\left\| \mathbf{v}^T - \mathbf{v}_n^T \right\| \right]$, respectively. As a result, the survival probability $P_{\mathrm{T}}(\Delta t)$ of a cluster after Δt is computed as

$$P_{\mathrm{T}}(\Delta t) = e^{-\lambda_R \frac{P_F(\Delta v^R + \Delta v^T)\Delta t}{D_c^s}} \tag{14}$$

where P_F is the percentage of moving clusters and D_c^s is a scenario-dependent coefficient describing space correlation. Typical values of D_c^s such as 10 m, 30 m, 50 m, and 100 m can be chosen with the same order of correlation distances in [21]. The survivability of each cluster at time $t + \Delta t$ is determined by $P_{\mathrm{T}}(\Delta t)$. Geometrical relationships, delays, and mean powers of survived clusters will be updated according to Section II-D. Meanwhile, a random number of new clusters are generated. This random number is generated according to a Poisson distribution with mean

$$\mathrm{E}[N_{\mathrm{new}}(t + \Delta t)] = \frac{\lambda_G}{\lambda_R}(1 - P_{\mathrm{T}}(\Delta t)). \tag{15}$$

Rays and geometrical parameters will be assigned to these new clusters as described in Section II-C, which also presents the array axis evolution for clusters.

$$h_{qp}^{\mathrm{LOS}}(t) = \begin{bmatrix} F_{p,\mathrm{V}}^T(\mathbf{D}_{qp}^{\mathrm{LOS}}(t), \mathbf{A}_p^T(t)) \\ F_{p,\mathrm{H}}^T(\mathbf{D}_{qp}^{\mathrm{LOS}}(t), \mathbf{A}_p^T(t)) \end{bmatrix}^{\mathrm{T}} \begin{bmatrix} e^{j\Phi_{\mathrm{LOS}}} & 0 \\ 0 & -e^{j\Phi_{\mathrm{LOS}}} \end{bmatrix} \begin{bmatrix} F_{q,\mathrm{V}}^R(\mathbf{D}_{qp}^{\mathrm{LOS}}(t), \mathbf{A}_q^R(t)) \\ F_{q,\mathrm{H}}^R(\mathbf{D}_{qp}^{\mathrm{LOS}}(t), \mathbf{A}_q^R(t)) \end{bmatrix} e^{j2\pi f_{qp}^{\mathrm{LOS}}(t)t} \tag{9}$$

$$h_{qp,n,m_n}(t) = \begin{bmatrix} F_{p,\mathrm{V}}^T(\mathbf{D}_{n,m_n}^T(t), \mathbf{A}_p^T(t)) \\ F_{p,\mathrm{H}}^T(\mathbf{D}_{n,m_n}^T(t), \mathbf{A}_p^T(t)) \end{bmatrix}^{\mathrm{T}} \begin{bmatrix} e^{j\Phi_{n,m_n}^{\mathrm{VV}}} & \sqrt{\kappa}e^{j\Phi_{n,m_n}^{\mathrm{VH}}} \\ \sqrt{\kappa}e^{j\Phi_{n,m_n}^{\mathrm{HV}}} & e^{j\Phi_{n,m_n}^{\mathrm{HH}}} \end{bmatrix} \begin{bmatrix} F_{q,\mathrm{V}}^R(\mathbf{D}_{n,m_n}^R(t), \mathbf{A}_q^R(t)) \\ F_{q,\mathrm{H}}^R(\mathbf{D}_{n,m_n}^R(t), \mathbf{A}_q^R(t)) \end{bmatrix}$$
$$\times \sqrt{P_{n,m_n}(t)}e^{j2\pi f_{qn,m_n}^R(t)t}e^{j2\pi f_{pn,m_n}^T(t)t} \tag{10}$$

TABLE II
DISTRIBUTIONS OF PARAMETERS OF CLUSTERS

Parameters	M_n	$\tilde{\tau}_n, \tau_{m_n}, D_n^T, D_n^R$	$\phi_n^A, \phi_n^E, \varphi_n^A, \varphi_n^E$
Distributions	Poisson	Exponential	Wrapped Gaussian

Step 3: When the array-time evolution is finished, the algorithm returns to Step 2 to enter the next time instant.

C. Generation of New Clusters

For a new cluster, say Cluster$_n$, certain parameters such as the number of rays within the cluster, virtual delay, mean power, angular parameters, and relative delays of rays need to be assigned to this cluster. These parameters are randomly generated according to the distributions listed in Table II. The virtual delays $\tilde{\tau}_n$ of clusters are assumed to be exponentially distributed, as in the WINNER II channel model [12], and can be expressed by

$$\tilde{\tau}_n = -r_\tau \sigma_\tau \cdot \ln u_n \tag{16}$$

where u_n is uniformly distributed within $(0, 1)$, r_τ is the delay scalar ($r_\tau = 2.3$ for NLOS urban outdoor scenario and $r_\tau = 2.4$ for NLOS indoor office scenario [12]), and σ_τ is a randomly generated delay spread (E $\left[\log_{10}\sigma_\tau\right] = -6.63$ and std $\left[\log_{10}\sigma_\tau\right] = 0.32$ for NLOS urban outdoor scenario and E $\left[\log_{10}\sigma_\tau\right] = -7.60$ and std $\left[\log_{10}\sigma_\tau\right] = 0.19$ for NLOS indoor office scenario [12]). The mean powers $\tilde{P}_n'$ of clusters are generated as [12]

$$\tilde{P}_n' = \exp\left(-\tilde{\tau}_n \frac{r_\tau - 1}{r_\tau \sigma_\tau}\right) 10^{-\frac{Z_n}{10}} \tag{17}$$

where Z_n follows a Gaussian distribution $\mathcal{N}(0, 3)$ [12]. Unlike the virtual delay and mean power of clusters, which are generated as in the WINNER II channel model, generations of angular parameters, relative delays of rays, and mean power of rays are not following the WINNER II channel model. The angular parameters ϕ_n^A, ϕ_n^E, φ_n^A, and φ_n^E of Cluster$_n$ are assumed to obey wrapped Gaussian distributions. Angles of arrival (AoAs) of Cluster$_n$ are generated as

$$\phi_n^A = \text{std}\left[\phi_n^A\right] Y_n^A + \psi_A^R \tag{18}$$

$$\phi_n^E = \text{std}\left[\phi_n^E\right] Y_n^E + \psi_E^R \tag{19}$$

where $Y_n^A, Y_n^E \sim \mathcal{N}(0, 1)$, std $\left[\phi_n^A\right]$ and std $\left[\phi_n^E\right]$ are standard deviations of AoAs and need to be estimated. The parameter estimation procedure is introduced in Appendix C. The mean power generation method of a cluster is extended to compute the mean power of rays within clusters as [54]

$$\tilde{P}_{n,m_n}' = \exp\left(-\tau_{m_n} \frac{r_\tau - 1}{\text{E}\left[\tau_{m_n}\right]}\right) 10^{-\frac{Z_{n,m_n}}{10}} \tag{20}$$

where Z_{n,m_n} follows a Gaussian distribution $\mathcal{N}(0, 3)$ [12]. The mean relative delay E $\left[\tau_{m_n}\right]$ of rays of Cluster$_n$ will be given in Section IV. The mean power of rays is then scaled by the cluster power as $\tilde{P}_{n,m_n} = \tilde{P}_n' \frac{\tilde{P}_{n,m_n}'}{\sum\limits_{m_n} \tilde{P}_{n,m_n}'}$. Then, the angular

1: Generate $M_n \sim \text{Pois}\left(\tilde{\lambda}\right)$ rays for the cluster;
2: Generate virtual delay/mean power/distance for the cluster;
3: Generate AoAs/Angles of departure (AoDs)/relative delays/relative mean powers for the rays within the cluster;
4: Generate discrete $\tilde{q} \sim \text{U}(1, M_R)$, generate $r \sim \exp\left(\frac{\lambda_R}{D_c^a}\right)$, and let $\tilde{i} = 1$;
5: **while** ($\tilde{i} \leq M_R$) **do**
6:     **if** ($\|\mathbf{A}_{\tilde{i}}^R - \mathbf{A}_{\tilde{q}}^R\| \leq r$) **then**
7:         Add the cluster to $C_{\tilde{i}}^{R}(t)$;
8:     **end if**
9:     $\tilde{i} = \tilde{i} + 1$;
10: **end while**

Fig. 3. Psuedo codes for the new cluster generation algorithm.

parameters of Cluster$_n$ via the m_nth ray can be calculated by adding the angular offset of the ray, i.e.,

$$\left[\phi_{n,m_n}^A \; \phi_{n,m_n}^E \; \varphi_{n,m_n}^A \; \varphi_{n,m_n}^E\right]^{\text{T}}$$
$$= \left[\phi_n^A \; \phi_n^E \; \varphi_n^A \; \varphi_n^E\right]^{\text{T}} + \left[\Delta\phi^A \; \Delta\phi^E \; \Delta\varphi^A \; \Delta\varphi^E\right]^{\text{T}} \tag{21}$$

where $\Delta\phi^A$, $\Delta\phi^E$, $\Delta\varphi^A$, and $\Delta\varphi^E$ are angular offsets of the ray and are assumed to follow Laplace distributions [12] with zero mean and standard deviation of 1 degree (0.017 radian) for simplicity. The standard deviation of angular offsets can be modified subject to measurements.

Next, which antennas are able to observe the newly generated cluster should be determined. To avoid repeated description, only the receiver side is presented, the transmitter side follows the same procedure. First, the newly generated cluster is added to the cluster set of a randomly selected receive antenna $\text{Ant}_{\tilde{q}}^R$. Second, we generate a 3D ball with radius $r \sim \exp\left(\frac{\lambda_R}{D_c^a}\right)$ where D_c^a is the scenario-dependent coefficient normalizing antenna spacings. Typical values of D_c^a such as 30 m and 50 m can be chosen with the same order of correlation distances in [21]. Third, we compute the distances between antennas $\text{Ant}_{\tilde{q}}^R$ and Ant_q^R for all q. Then, we add the newly generated cluster to the cluster sets of antennas satisfying $\|\mathbf{A}_q^R - \mathbf{A}_{\tilde{q}}^R\| \leq r$. As a consequence, the probability that both $\text{Ant}_{\tilde{q}}^R$ and Ant_q^R are able to observe this newly generated cluster will be $\exp\left(\frac{\lambda_R}{D_c^a}\|\mathbf{A}_q^R - \mathbf{A}_{\tilde{q}}^R\|\right)$. The psuedo codes of the new cluster generation algorithm are shown in Fig. 3.

D. Evolution of Survived Clusters

In order to highlight time evolution of the proposed model, geometrical relationships, virtual delays, and mean powers of survived clusters need to be updated from t to $t + \Delta t$. To begin with, antenna position vectors are updated as

$$\mathbf{A}_q^R(t + \Delta t) = \mathbf{A}_q^R(t) + \mathbf{v}^R \Delta t \tag{22}$$

$$\mathbf{A}_p^T(t + \Delta t) = \mathbf{A}_p^T(t) + \mathbf{v}^T \Delta t. \tag{23}$$

At the same time, distance vectors of clusters need to be adjusted as

$$\mathbf{D}_n^R(t + \Delta t) = \mathbf{D}_n^R(t) + \mathbf{v}_n^R \Delta t \tag{24}$$

$$\mathbf{D}_n^T(t + \Delta t) = \mathbf{D}_n^T(t) + \mathbf{v}_n^T \Delta t. \tag{25}$$

Other distance vectors in (1)–(7) can be updated accordingly. Delays are updated as

$$\tau_n(t + \Delta t)$$
$$= \left[\left\| \mathbf{D}_n^R(t + \Delta t) \right\| + \left\| \mathbf{D}_n^T(t + \Delta t) \right\| \right] / c + \tilde{\tau}_n(t + \Delta t). \tag{26}$$

The random virtual delays $\tilde{\tau}_n(t + \Delta t)$ are modeled as $\tilde{\tau}_n(t + \Delta t) = e^{-\frac{\Delta t}{\varsigma}} \tilde{\tau}_n(t) + (1 - e^{-\frac{\Delta t}{\varsigma}}) X$ where X is a random variable independent to $\tilde{\tau}_n$ but identically distributed as $\tilde{\tau}_n$ and ς is a scenario-dependent parameter describing the coherence of virtual links. Typical values of the coherence of virtual links such as 5 s, 7 s, and 30 s are chosen based on reasonable assumptions. Thus, the updated delay will carry information of the delay in the previous time instant.

Another important aspect is the evolution of cluster mean power. Constant cluster mean powers were assumed in [28] and [29], which were not sufficient to characterize time evolution of the channel. Therefore, in this paper, with the assumption that the cluster mean powers satisfy the inverse square law, the time evolution of cluster mean power can be expressed as (derivations given in Appendix B)

$$\tilde{P}_{n,m_n}(t + \Delta t) = \tilde{P}_{n,m_n}(t) \frac{3\tau_n(t) - 2\tau_n(t + \Delta t) + \tau_{m_n}}{\tau_n(t) + \tau_{m_n}}. \tag{27}$$

The mean power terms $\tilde{P}_{n,m_n}$ in the mean power evolution in (27) are not normalized. They need to be normalized such that $P_{n,m_n} = \tilde{P}_{n,m_n} / \sum_{n,m_n} \tilde{P}_{n,m_n}$ before being plugged into (10). To guarantee smooth power transitions when clusters appear or disappear, a simple linear power scaling is performed within 1 ms. That is to say, the power of a disappearing cluster will be scaled linearly from its instant power to zero within 1 ms, and the power of a newly generated cluster will be scaled from 0 to its power shown in (17). The choice of a 1 ms transition period is aligned with the length of one subframe in LTE [60], which is easier for system-level simulations with the proposed channel model. Other non-linear transitions can be found in [46].

E. Simplified Channel Models

The proposed general 3D non-stationary 5G GBSM can easily be reduced to various simplified channel models by adjusting certain model parameters.

1) By setting the numbers of antennas (M_R and M_T) as relatively small numbers, the spherical wavefront effect and cluster evolution on the array axis will become insignificant. In this case, the general 5G massive MIMO channel model is reduced to a conventional (non-massive) MIMO channel model.
2) By setting the velocity of the transmitter $\mathbf{v}^T = \mathbf{0}$, the general 5G V2V channel model is reduced to a fixed-to-mobile (F2M) channel model.

3) By setting the relative delays of rays as 0, i.e., $\tau_{m_n} = 0$, rays within a cluster will become irresolvable in the delay domain. Consequently, the general 5G mmWave channel model is simplified as a SCM-like wideband channel model.
4) By setting all elevation angles as zero, i.e., $\psi_E^R = \psi_E^T = \phi_n^E(t) = \varphi_n^E(t) = 0$, the impacts of elevation angles are ignored. Then, the 3D 5G channel model is simplified to 2D.

By properly adjusting the parameters of the proposed general 5G channel model, various simplified channel models can be obtained, such as 3D wideband massive MIMO, 3D wideband HST conventional MIMO, 3D mmWave conventional MIMO, and 2D wideband V2V conventional MIMO channel models.

III. STATISTICAL PROPERTY ANALYSIS

A. Time-Variant Power Delay Profile (PDP)

The time-variant PDP $\Lambda(t, \tau)$ of the channel can be expressed as [61]

$$\Lambda(t, \tau) = \sum_n^{N(t)} \sum_{m_n}^{M_n} P_{n,m_n}(t) \delta \left(\tau - \tau_n(t) - \tau_{m_n} \right). \tag{28}$$

It should be noted that the PDP is from all observable clusters at both the transmit and receive arrays. The time-variant properties of PDP are caused by the time-dependent mean powers and delays of rays. These are related to the geometrical relationship updates of the scattering environment.

B. Stationary Interval

The stationary interval is utilized in [44] to measure the estimated period within which the channel amplitude response can be regarded as stationary. It can be used to determine the frequency of channel estimation in HST communications. The definition of the stationary interval is the maximum time length within which the autocorrelation function (ACF) of the PDP exceeds the 80% threshold [44]. It should be noticed that the 80% threshold in [44] is empirical and can be adjusted according to requirements. Also, the definition of stationary interval in [44] would fail to work if the ACF of the PDP is not monotonically decreasing or has multiple crossing points at the threshold. Therefore, an improved definition of the stationary interval $I(t)$ at time t is proposed as $I(t) = \inf \left\{ \Delta t | R_{\Lambda(t, \Delta t) \leq 0.8} \right\}$ where $\inf \{\cdot\}$ calculates the infimum of a function and $R_{\Lambda(t, \Delta t)}$ is the normalized ACF of the PDP defined by [44]

$$R_\Lambda(t, \Delta t) = \frac{\int \Lambda(t, \tau) \Lambda(t + \Delta t, \tau) d\tau}{\max \left\{ \int \Lambda^2(t, \tau) d\tau, \int \Lambda^2(t + \Delta t, \tau) d\tau \right\}}. \tag{29}$$

C. Time-Variant Transfer Function

The time-variant transfer function $H_{qp}(\xi, t)$ is the Fourier transform of the channel impulse response with respect to delay, which can be expressed as (30), as shown at the bottom of the next page, where ξ is frequency [61].

D. Space-Time-Frequency Correlation Function

To study the correlation properties, the space-time-frequency correlation function (STFCF) $\rho_{qp,q'p'}(\|\mathbf{A}_p^T - \mathbf{A}_{p'}^T\|, \|\mathbf{A}_q^R - \mathbf{A}_{q'}^R\|, \Delta\xi, \Delta t; \xi, t)$ can be calculated as [61]

$$\rho_{qp,q'p'}(\|\mathbf{A}_p^T - \mathbf{A}_{p'}^T\|, \|\mathbf{A}_q^R - \mathbf{A}_{q'}^R\|, \Delta\xi, \Delta t; \xi, t)$$
$$= \mathrm{E}\left[H_{qp}^*(\xi, t)H_{q'p'}(\xi + \Delta\xi, t + \Delta t)\right]. \quad (31)$$

The LOS component is computed based on the relative position between the transmitter and receiver. The parameters of the NLOS components are randomly generated. Therefore, the LOS and NLOS components are assumed to be uncorrelated for simplicity. Then, (31) can be written as the sum of the correlation of the LOS component and the correlation of the NLOS components, i.e.,

$$\rho_{qp,q'p'}(\|\mathbf{A}_p^T - \mathbf{A}_{p'}^T\|, \|\mathbf{A}_q^R - \mathbf{A}_{q'}^R\|, \Delta\xi, \Delta t; \xi, t)$$
$$= \rho_{qp,q'p'}^{\mathrm{LOS}}(\|\mathbf{A}_p^T - \mathbf{A}_{p'}^T\|, \|\mathbf{A}_q^R - \mathbf{A}_{q'}^R\|, \Delta\xi, \Delta t; \xi, t)$$
$$+ \rho_{qp,q'p'}^{\mathrm{NLOS}}(\|\mathbf{A}_p^T - \mathbf{A}_{p'}^T\|, \|\mathbf{A}_q^R - \mathbf{A}_{q'}^R\|, \Delta\xi, \Delta t; \xi, t). \quad (32)$$

The correlation of the LOS component is calculated as

$$\rho_{qp,q'p'}^{\mathrm{LOS}}(\|\mathbf{A}_p^T - \mathbf{A}_{p'}^T\|, \|\mathbf{A}_q^R - \mathbf{A}_{q'}^R\|, \Delta\xi, \Delta t; \xi, t)$$
$$= \frac{K}{K+1}h_{qp}^{\mathrm{LOS}*}(t)h_{q'p'}^{\mathrm{LOS}}(t + \Delta t)e^{j2\pi\sigma_1} \quad (33)$$

with $\sigma_1 = \xi\left[\tau^{\mathrm{LOS}}(t) - \tau^{\mathrm{LOS}}(t + \Delta t)\right] + \Delta\xi\tau^{\mathrm{LOS}}(t + \Delta t)$. Similarly, the correlation of the NLOS components is calculated as (34), as shown at the bottom of this page, with $\sigma_2 = \xi(\tau_n(t) + \tau_{m_n} - \tau_{n'}(t + \Delta t) - \tau_{m_{n'}}) - \Delta\xi(\tau_{n'}(t + \Delta t) + \tau_{m_{n'}})$. Because cluster evolution is considered in the proposed general 5G GBSM, the mean number of survived cluster shared by $h_{qp,n,m_n}(t)$ and $h_{q'p',n',m_{n'}}(t + \Delta t)$ can be calculated as

$$\mathrm{E}\left\{\mathrm{card}\left(S_{qp}(t)\bigcap S_{q'p'}(t + \Delta t)\right)\right\}$$
$$= P_{\mathrm{survival}}\mathrm{E}\left\{\mathrm{card}\left(S_{qp}(t)\right)\right\} \quad (35)$$

where P_{survival} is the cluster survival probability when a cluster evolves from Ant_p^T, Ant_q^R, and t to $\mathrm{Ant}_{p'}^T$, $\mathrm{Ant}_{q'}^R$, and $t + \Delta t$, respectively, i.e.,

$$P_{\mathrm{survival}} = e^{-\lambda_R\left[\frac{\|\mathbf{A}_p^T - \mathbf{A}_{p'}^T\| + \|\mathbf{A}_q^R - \mathbf{A}_{q'}^R\|}{D_c^a} + \frac{P_F(\Delta v^R + \Delta v^T)\Delta t}{D_c^s}\right]}. \quad (36)$$

Those newly generated clusters from $h_{qp,n,m_n}(t)$ to $h_{q'p',n',m_{n'}}(t + \Delta t)$ are independent to the survived clusters. Therefore, they do not contribute to the correlation coefficient.

Then, the STFCF for NLOS components in (34) reduces to (37), as shown at the bottom of this page.

As the dimension of the STFCF is high, it is difficult to present the STFCF visually. However, by setting $\Delta\xi = 0$, $q = q'$, and $p = p'$, the STFCF is reduced to the time-variant ACF. By setting $\Delta t = 0$, $\Delta\xi = 0$ and $p = p'$ ($q = q'$), the STFCF is reduced to the receive (transmit) space cross-correlation function (CCF). Similarly, by setting $q = q'$, $p = p'$, and $\Delta t = 0$, the STFCF is reduced to the time-variant frequency correlation function (FCF).

IV. RESULTS AND ANALYSIS

In the simulations, we assume that the generation rate $\lambda_{\mathrm{G}} = 80/\mathrm{m}$ [31, Table I] and the recombination rate $\lambda_{\mathrm{R}} = 4/\mathrm{m}$, so that the mean number of clusters is fixed as 20 [12]. The percentage of moving clusters is $P_F = 0.3$ [31]. The parameter estimation of the proposed 5G small-scale fading channel model is based on the minimum mean square error (MMSE) criterion, i.e., $\epsilon = |\hat{\mathsf{f}} - \mathsf{f}(\mathsf{P})|^2$, where $\hat{\mathsf{f}}$ is the measured statistical property such as space CCF and complementary cumulative distribution function (CCDF) of coherence bandwidth, f is the statistical property of the channel model, and P is the parameter set of the channel model. Note that the parameter set P for a specific statistical property is not necessary to include all parameters of the channel model, since only a small number of parameters will significantly affect this statistical property. Besides the parameter set P, the rest parameters are generated randomly according to the WINNER II channel model [12]. Based on the MMSE criterion, an exhaustive search of the parameter set P will be performed using an optimization procedure until ϵ reaches a certain threshold and then the parameter set will be obtained. Details of the parameter estimation procedure are introduced in Appendix C. The cluster parameters finally obtained for simulations are listed in Table III. Their distributions can be referred to Table II.

To validate the correctness of the proposed general 5G GBSM, the analytical ACFs of the simulation model and corresponding simulation results of the wideband conventional MIMO channel model for both Cluster$_1$ and Cluster$_2$ are compared in Fig. 4. Half-wavelength linear arrays are assumed at both the transmitter and receiver. It should be noted that these ACFs are normalized with respect to Cluster$_1$. It can be seen from Fig. 4 that the simulated ACFs align well with the analytical ACFs of the simulation model for both Cluster$_1$ and Cluster$_2$.

$$H_{qp}(\xi, t) = \int_{-\infty}^{\infty} h_{qp}(t, \tau)e^{-j2\pi\xi\tau}d\tau = \sqrt{\frac{K}{K+1}}h_{qp}^{\mathrm{LOS}}(t)e^{-j2\pi\xi\tau^{\mathrm{LOS}}(t)} + \sqrt{\frac{1}{K+1}}\sum_{n=1}^{N(t)}\sum_{m_n=1}^{M_n(t)}h_{qp,n,m_n}(t)e^{-j2\pi\xi[\tau_n(t)+\tau_{m_n}]} \quad (30)$$

$$\rho_{qp,q'p'}^{\mathrm{NLOS}}(\|\mathbf{A}_p^T - \mathbf{A}_{p'}^T\|, \|\mathbf{A}_q^R - \mathbf{A}_{q'}^R\|, \Delta\xi, \Delta t; \xi, t) = \frac{1}{K+1}\mathrm{E}\left[\sum_{n=1}^{N(t)}\sum_{n'=1}^{N(t+\Delta t)}\sum_{m_n=1}^{M_n}\sum_{m_{n'}=1}^{M_{n'}}h_{qp,n,m_n}^*(t)h_{q'p',n',m_{n'}}(t + \Delta t)e^{j2\pi\sigma_2}\right] \quad (34)$$

$$\rho_{qp,q'p'}^{\mathrm{NLOS}}(\delta_T, \delta_R, \Delta\xi, \Delta t; \xi, t) = \frac{P_{\mathrm{survival}}}{K+1}\mathrm{E}\left[\sum_{n=1}^{N(t)}\sum_{n'=1}^{N(t)}\sum_{m_n=1}^{M_n}\sum_{m_{n'}=1}^{M_{n'}}h_{qp,n,m_n}^*(t)h_{q'p',n',m_{n'}}(t + \Delta t)e^{j2\pi\sigma_2}\right] \quad (37)$$

TABLE III
SIMULATION PARAMETERS FOR DIFFERENT SIMPLIFIED 5G CHANNEL MODELS

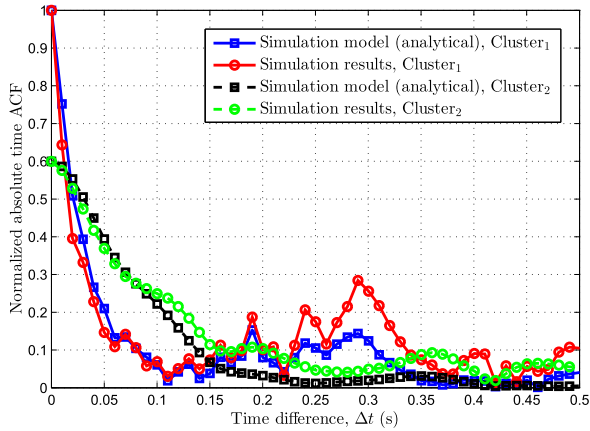| 3D wideband massive MIMO			3D wideband HST conventional MIMO		
Parameters	Mean	Standard deviation	Parameters	Mean	Standard deviation
M_n	20	0	M_n	20	0
τ_n	930 ns	930 ns	τ_n	930 ns	930 ns
τ_{m_n}	0 ns	0 ns	τ_{m_n}	0 ns	0 ns
(D_n^R, D_n^T)	(25, 30) m	(15, 10) m	(D_n^R, D_n^T)	(25, 30) m	(15, 10) m
ϕ_n^A	0.78 rad	1.15 rad	ϕ_n^A	0.78 rad	0.90 rad
ϕ_n^E	0.78 rad	0.18 rad	ϕ_n^E	0.78 rad	0.18 rad
φ_n^A	1.05 rad	0.54 rad	φ_n^A	1.05 rad	0.54 rad
φ_n^E	0.78 rad	0.11 rad	φ_n^E	0.78 rad	0.11 rad
D_c^a	30 m	0 m	D_c^a	50 m	0 m
D_c^s	100 m	0 m	D_c^s	100 m	0 m
ς	30 s	0 s	ς	7 s	0 s
(ψ_A^R, ψ_E^R)	$\left(\frac{\pi}{4}, \frac{\pi}{4}\right)$ rad	(0, 0)	(ψ_A^R, ψ_E^R) rad	$\left(\frac{\pi}{4}, \frac{\pi}{4}\right)$	(0, 0)
(ψ_A^T, ψ_E^T)	$\left(\frac{\pi}{3}, \frac{\pi}{4}\right)$ rad	(0, 0)	(ψ_A^T, ψ_E^T) rad	$\left(\frac{\pi}{3}, \frac{\pi}{4}\right)$	(0, 0)
2D wideband V2V conventional MIMO			3D mmWave conventional MIMO		
Parameters	Mean	Standard deviation	Parameters	Mean	Standard deviation
M_n	20	0	M_n	15	3.87
τ_n	930 ns	930 ns	τ_n	305 ns	305 ns
τ_{m_n}	0 ns	0 ns	τ_{m_n}	3 ns	3 ns
(D_n^R, D_n^T)	(25, 30) m	(15, 10) m	(D_n^R, D_n^T)	(5, 5) m	(3, 3) m
ϕ_n^A	0.78 rad	0.91 rad	ϕ_n^A	0.78 rad	0.91 rad
ϕ_n^E	0 rad	0 rad	ϕ_n^E	0.78 rad	0.18 rad
φ_n^A	1.04 rad	0.53 rad	φ_n^A	1.04 rad	0.53 rad
φ_n^E	0 rad	0 rad	φ_n^E	0.78 rad	0.11 rad
D_c^a	30 m	0 m	D_c^a	30 m	0 m
D_c^s	10 m	0 m	D_c^s	100 m	0 m
ς	5 s	0 s	ς	7 s	0 s
(ψ_A^R, ψ_E^R)	$\left(\frac{\pi}{4}, \frac{\pi}{4}\right)$ rad	(0, 0)	(ψ_A^R, ψ_E^R)	$\left(\frac{\pi}{4}, \frac{\pi}{4}\right)$ rad	(0, 0)
(ψ_A^T, ψ_E^T)	$\left(\frac{\pi}{3}, \frac{\pi}{4}\right)$ rad	(0, 0)	(ψ_A^T, ψ_E^T)	$\left(\frac{\pi}{3}, \frac{\pi}{4}\right)$ rad	(0, 0)

Fig. 4. Comparison between the normalized analytical and simulated ACFs of Cluster$_1$ and Cluster$_2$ of the wideband conventional MIMO channel model ($f_c = 2$ GHz, $\|\mathbf{D}\| = 200$ m, $M_R = M_T = 2$, $\Delta v^R = \Delta v^T = 0$ m/s, $|\mathbf{v}^T| = 0$, $|\mathbf{v}^R| = 5$ m/s, $D_c^a = 50$ m, $D_c^s = 100$ m, $M_1 = M_2 = 81$, $\varsigma = 7$ s, NLOS).
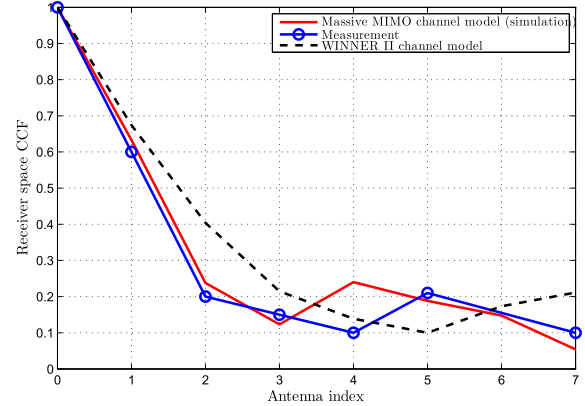

Fig. 5. The receiver normalized space CCFs of the 3D wideband massive MIMO channel model (simulations), measurement in [24], and WINNER II channel model ($f_c = 2.6$ GHz [24], $\|\mathbf{D}\| = 200$ m, $M_R = M_T = 32$, $\Delta v^R = \Delta v^T = 0$ m/s [24], $|\mathbf{v}^T| = |\mathbf{v}^R| = 0$ [24], $D_c^a = 30$ m, $D_c^s = 100$ m, $\kappa = -8$ dB, polarized antennas, NLOS).

The receiver normalized space CCF of the 3D wideband massive MIMO channel model (simulation) in Table III, the measured averaged space CCF in the NLOS scenario in [24, Fig. 10], and the space CCF of the WINNER II channel model are compared in Fig. 5. The horizontal axis of Fig. 5 has been normalized with respect to half wavelength. The measurement in [24] was performed in an outdoor environment with a 128-element polarized virtual linear array covering both LOS and NLOS scenarios. Each polarized antenna pair was also separated by half wavelength. When the antenna index difference is larger than 2, the correlation coefficients drop to a relatively low level and different sub-channels can be considered as uncorrelated. In this case, the fitting is not important anymore. It is clear that the space CCF of the proposed massive MIMO channel model aligns well with the measured data when the antenna index difference is less than 3. However, the WINNER II channel model
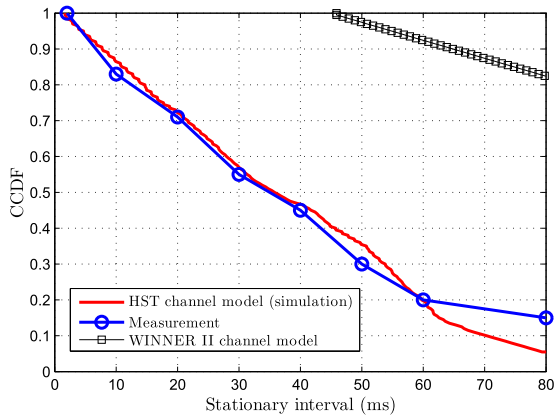
Fig. 6. The CCDFs of the stationary intervals for the 3D wideband HST conventional MIMO channel model (simulation), measurement in [44], and WINNER II channel model (f_c = 932 MHz [44], $\|\mathbf{D}\|$ = 200 m, $M_R = M_T = 2$, $\Delta v^R = \Delta v^T = 0.5$ m/s, $\|\mathbf{v}^R\|$ = 60 m/s [44], $\|\mathbf{v}^T\|$ = 0 m/s [44], $D_c^a = 50$ m, $D_c^s = 100$ m, $\varsigma = 7$ s, NLOS).
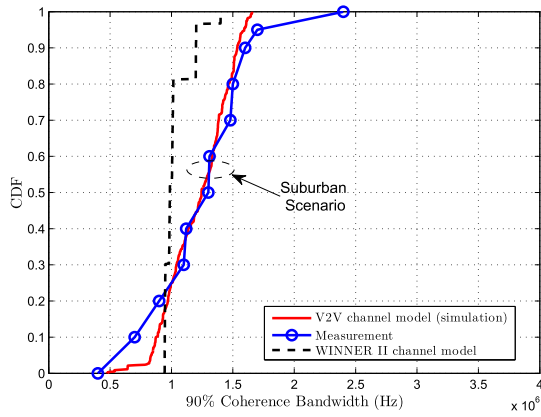

Fig. 8. A snapshot of the simulated normalized APS at the receiver of the 2D mmWave massive MIMO channel model (f_c = 58 GHz, $M_T = 2$, $M_R = 32$, $\|\mathbf{D}\|$ = 6 m, $\Delta v^R = \Delta v^T = 0$ m/s, $|\mathbf{v}^T| = |\mathbf{v}^R| = 0$, $D_c^a = 30$ m, $D_c^s = 100$ m, NLOS).

Fig. 7. The CDFs of 90% coherence bandwidths of the 2D wideband V2V conventional MIMO channel model, measurement (suburband scenario) in [63], and WINNER II channel model (f_c = 5.9GHz [63], $\|\mathbf{D}\|$ = 400m, $\Delta v^R = \Delta v^T = 0.5$m/s, $\|\mathbf{v}^T\| = \|\mathbf{v}^R\|$ = 25m/s, $D_c^a = 30$m, $D_c^s = 10$m, $\varsigma = 5$s, NLOS).

Fig. 9. The CCDFs of RMS delay spreads of the 3D mmWave conventional MIMO channel model, measurement in [64], and WINNER II channel model (f_c = 58 GHz [64], $\|\mathbf{D}\|$ = 6 m, $\Delta v^R = \Delta v^T = 0$ m/s, $\|\mathbf{v}^T\| = \|\mathbf{v}^R\| = 0$ m/s, $D_c^a = 30$ m, $D_c^s = 100$ m, $\varsigma = 7$ s, NLOS).

overestimates antenna correlations because cluster evolution was not considered on the array axis.

The CCDFs of the stationary intervals of the 3D wideband HST conventional MIMO channel model (with velocity 60 m/s) in Table III, the measurement in [44, Fig. 4(a)] with an omnidirectional antenna, and the WINNER II channel model are shown in Fig. 6. The median of the stationary interval is approximately 40 ms. Clearly, the proposed HST channel model can fit the measurement result very well. The WINNER II channel model has a much higher stationary interval due to the fact that it does not have cluster power evolution in the time domain.

The 90% coherence bandwidth measures the bandwidth in which the channel can be regarded as flat. The cumulative distribution function (CDF) of 90% coherence bandwidth of the 2D wideband V2V conventional MIMO channel model in Table III is illustrated in Fig. 7, which is also validated by that of the measured suburban V2V channel in [63, Fig. 5(a)]. The measurement in [63] was performed in a suburban scenario with both transmitter and receiver moving
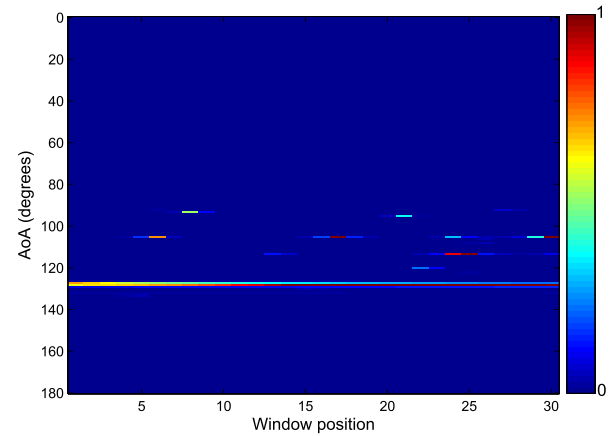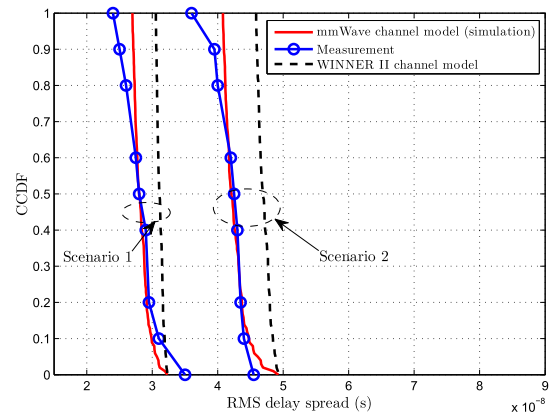
in the same direction. The 90% coherence bandwidth of the WINNER II channel model has smaller spread because its PDP is not time variant.

A snapshot of the simulated normalized angular power spectrum (APS) at the receiver with a half-wavelength linear array of the 2D mmWave massive MIMO channel model is illustrated in Fig. 8. The APS is estimated with the smooth multiple signal classification (MUSIC) algorithm [62], [65] using a sliding window of 3 consecutive antennas. With these sliding windows, the smooth MUSIC algorithm is able to resolve more AoAs than the conventional MUSIC algorithm. It can be observed that the number of clusters is small because of the high carrier frequency of mmWave. Meanwhile, appearance and disappearance of clusters on the array axis can also be seen due to the massive MIMO antenna array.

Fig. 9 presents the CCDFs of the root mean square (RMS) delay spreads of the 3D mmWave conventional MIMO channel model in Table III, the measurements in [64, Fig. 5], and the WINNER II channel model. The measurements in [64] were performed in indoor scenarios with omnidirectional antennas in azimuth. Scenario 1 and Scenario 2 are the Room H

Parameters	Mean	Standard deviation
M_n	Determined via assumption	0
τ_n	Randomly generated via WINNER II	Randomly generated via WINNER II
τ_{m_n}, D_n^T, D_n^R	Determined via assumption	Determined via assumption
$\phi_n^A, \phi_n^E, \varphi_n^A, \varphi_n^E$	Randomly generated via WINNER II	Determined via parameter estimation
D_c^a	Determined via parameter estimation	0 m
D_c^s	Determined via parameter estimation	0 m
ς	Determined via parameter estimations	0 s

scenario and Room F scenario in [64, Fig. 5], respectively. It is clear that measurement results for different scenarios in [64, Fig. 5] can be fitted properly by the proposed 3D mmWave channel model. The WINNER II channel model does not support mmWave small-scale channel characteristics well as it overestimates the RMS delay spread and has smaller variations. The RMS delay spread of the mmWave channel model is between 20 ns and 50 ns.

V. CONCLUSIONS

In this paper, a unified framework for 5G wireless small scale fading channel models has been proposed, based on the WINNER II and SV channel models. The proposed general 3D non-stationary 5G channel model can model massive MIMO, V2V, HST, and mmWave communication scenarios, as well as considering time evolution feature of channels and arbitrary antenna array layouts. The modeling of time evolution of channels includes cluster evolution on the time axis, geometrical relationship updates, and evolution of delays and powers of rays. It has been shown that the simulated statistical properties of the proposed general 3D non-stationary 5G GBSM can fit well the corresponding measurements. The proposed general 5G GBSM can be reduced to various simplified channel models by properly setting certain parameters. For future work, applications of the proposed channel model to 5G system simulators and parameter estimations of the proposed 5G channel model from more channel measurements need to be considered. Also, the general 5G GBSM can be further extended by considering cooperative MIMO channel model with multi-link correlations, HST channel model with time-variant Rician factor, HST channel model in tunnel scenarios, time-variant antenna pattern, and the Rician factor evolution in both time and array domains in massive MIMO scenarios.

APPENDIX A
CALCULATION OF ANTENNA PATTERNS IN (9)

In a 3D space, the geometry of antenna pattern depends on the orientation of antennas. The LCS is obtained by a sequence of rotations from the GCS [14]. First, a rotation of α^T about x_G axis is operated. Second, a rotation of β^T about the new

y_G axis is operated. Third, a rotation of γ^T about the new z_G axis is operated. These three operations can be expressed as (38), as shown at the bottom of this page, [14].

Let $\mathbf{a}$ and $\mathbf{b}$ be positions vectors in the GCS, and let $(\tilde{x}, \tilde{y}, \tilde{z})^T$ be the coordinates of $\mathbf{a} - \mathbf{b}$ in the LCS. Then, $(\tilde{x}, \tilde{y}, \tilde{z})^T = \mathbf{R}(\mathbf{a} - \mathbf{b})$. Let $w(x, y)$ be the four-quadrant inverse tangent function [66] of x and y, and let $\tilde{\theta} = w(\tilde{y}, \tilde{x})$ and $\tilde{\phi} = w(\tilde{z}, \sqrt{\tilde{x}^2 + \tilde{y}^2})$. Then, the antenna patterns in (9) can be computed as $F_H(\mathbf{a}, \mathbf{b}) = G(\tilde{\theta}, \tilde{\phi}) \cos \tilde{\theta}$ and $F_V(\mathbf{a}, \mathbf{b}) = G(\tilde{\theta}, \tilde{\phi}) \sin \tilde{\theta}$. In this paper, dipole antennas are assumed at the transmitter side. In this case [67], $G(\tilde{\theta}, \tilde{\phi}) = \sqrt{1.64} \frac{\cos\left(\frac{\pi}{2} \cos \tilde{\phi}\right)}{\sin \tilde{\phi}}$. At the receiver side, calculation follows a similar procedure. Omnidirectional antennas are assumed at the receiver side. In this case, $G(\tilde{\theta}, \tilde{\phi}) = 1$. Both antenna patterns can be replaced by the actual antennas used. The rotation angles α^T, α^R, β^T, β^R, γ^T, and γ^R are all set as $\frac{\pi}{15}$ for simplicity, which can be modified according to realistic settings.

APPENDIX B
CALCULATION OF (27)

Let us consider the time interval between t and $t + \Delta t$, where Δt is small. Then, the ray mean power difference $\Delta \tilde{P}_{n,m_n}(t)$ between these two time instants is computed as

$$\Delta \tilde{P}_{n,m_n}(t) = \tilde{P}_{n,m_n}(t + \Delta t) - \tilde{P}_{n,m_n}(t). \tag{39}$$

With the assumption of the inverse power law, the ray mean power is inversely proportional to the ηth ($\eta > 1$) power of travel distance, i.e., $\tilde{P}_{n,m_n}(t) = \frac{C}{[\tau_n(t) + \tau_{n,m_n}]^\eta c^\eta}$, where C is a constant. The derivative of $\tilde{P}_{n,m_n}(t)$ with respect to t is obtained by

$$\frac{\Delta \tilde{P}_{n,m_n}(t)}{\Delta t}$$

$$= \left(\frac{C}{[\tau_n(t) + \tau_{n,m_n}]^\eta c^\eta} \right)'$$

$$= -\eta \frac{C}{[\tau_n(t) + \tau_{n,m_n}]^{\eta+1} c^\eta} (\tau_n(t))'$$

$$= -\eta \frac{C}{[\tau_n(t) + \tau_{n,m_n}]^{\eta+1} c^\eta} \frac{[\tau_n(t + \Delta t) - \tau_n(t)]}{\Delta t}. \tag{40}$$

$$\mathbf{R} = \begin{bmatrix} \cos \gamma^T & -\sin \gamma^T & 0 \\ \sin \gamma^T & \cos \gamma^T & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} \cos \beta^T & 0 & \sin \beta^T \\ 0 & 1 & 0 \\ -\sin \beta^T & 0 & \cos \beta^T \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 \\ 0 & \cos \alpha^T & -\sin \alpha^T \\ 0 & \sin \alpha^T & \cos \alpha^T \end{bmatrix}. \tag{38}$$

Thus, the ray mean power evolution in terms of time can be derived as

$$\frac{\Delta \tilde{P}_{n,m_n}(t)}{\tilde{P}_{n,m_n}(t)} = \frac{-\eta}{\tau_n(t) + \tau_{n,m_n}} \frac{[\tau_n(t + \Delta t) - \tau_n(t)]}{\Delta t} \Delta t. \quad (41)$$

It follows that

$$\tilde{P}_{n,m_n}(t + \Delta t)$$
$$= \tilde{P}_{n,m_n}(t) \frac{(\eta + 1)\tau_n(t) - \eta\tau_n(t + \Delta t) + \tau_{n,m_n}}{\tau_n(t) + \tau_{n,m_n}}. \quad (42)$$

For simplicity, in this paper we use $\eta = 2$ following the inverse square law. Then, (27) is obtained.

APPENDIX C
PARAMETER ESTIMATION PROCEDURE OF THE PROPOSED MODEL

A typical parameter estimation method can be found in [68]. This paper follows a similar procedure as in [68], i.e., estimating parameters minimizing the difference in statistical properties between the model and measurement. The parameter estimation procedure in this paper directly estimates parameters to fit the statistic properties of the channel. The parameters of the proposed model can be divided into three categories, i.e., parameters determined via reasonable assumptions, parameters determined via parameter estimation methods, and parameters randomly generated. The categories of parameters are listed in Table IV. Let P be the set of parameters to be estimated, i.e., $\mathsf{P} = \left\{ \text{std}\left[\phi_n^A\right], \text{std}\left[\phi_n^E\right], \text{std}\left[\varphi_n^A\right], \text{std}\left[\varphi_n^E\right], D_c^a, D_c^s, \varsigma \right\}$ and $\mathsf{f}(\mathsf{P})$ be a statistical property with channel impulse responses generated using P. The estimated parameters $\hat{\mathsf{P}}$ can be obtained via optimization methods, e.g., exhaustive search, by minimizing $\hat{\mathsf{P}} = \arg\min_{\mathsf{P}} |\hat{\mathsf{f}} - \mathsf{f}(\mathsf{P})|^2$ where $\hat{\mathsf{f}}$ is the measured statistical property. This can be summarized into a number of steps. Step 1:

1) Define target threshold ϵ_{T} and initialize parameters $\hat{\mathsf{P}}$.
2) Generate channel coefficients with parameters $\hat{\mathsf{P}}$.
3) Calculate the statistical property $\mathsf{f}(\hat{\mathsf{P}})$ using the generated channel coefficients.
4) Compute the error between the model and measurement $\epsilon = |\hat{\mathsf{f}} - \mathsf{f}(\hat{\mathsf{P}})|^2$.
5) If $\epsilon \leqslant \epsilon_{\mathrm{T}}$, output $\hat{\mathsf{P}}$; Otherwise, generate a new set of $\hat{\mathsf{P}}$ and go to Step 2.

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