# Image Processing Toolbox 

For Use with MATLAB ${ }^{\text {© }}$

## Computation

Visualization

Programming

The
MATH
WORKS
Inc.
User's Guide
Version 2

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## I mage Processing Tool box User's Guide

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## What Is the Image Processing Toolbox?

The Image Processing Tool box is a collection of functions that extend the capability of the MATLAB ${ }^{\circledR}$ numeric computing environment.

## What Can You Do with the Image Processing Toolbox?

The tool box supports a wide range of image processing operations, including:

- Geometric operations
- Neighborhood and block operations
- Linear filtering and filter design
- Transforms
- Image analysis and enhancement
- Binary image operations
- Region of interest operations

Many of the tool box functions are MATLAB M-files, which contain MATLAB code that implements specialized image processing algorithms. You can view the MATLAB code for these functions using the statement:
type function_name
You can extend the capabilities of the Image Processing Toolbox by writing your own M-files, or by using the tool box in combination with other tool boxes, such as the Signal Processing Tool box and the Wavelet Tool box.

## New Features in Version 2.2

Version 2.2 offers the following new features: 16-bit image processing (most functions); speed optimization of many functions, including buf ill, busel ect, bW abel, di late, er ode, hi steq, i mesize, imot at e, or dfilt 2, medf ilt 2, and i main nt 8, new border-padding options for medfilt 2 and or dfilt2; and a new function, i m2ui nt 16.

In addition, some of the new features and changes in MATLAB 5.3 (Release 11) are relevant to the operation of the Image Processing Tool box 2.2. Rel evant changes in MATLAB 5.3 include: improved support for integer types (ui nt 8,
i nt 8, ui nt 16, i nt 16, ui nt 32, and i nt 32); support for two new fileformats, PNG and HDF-EOS; 16-bit image display; and 16-bit TIFF fileI/O.

## Updates to Earlier Versions

Version 2.1 offered the following new features: inverse Radon transform; interactive pixel value display including distancebetween two pixels; advanced feature measurement; Canny edge detection; YCbCr col or space support; easier data precision conversion; and a new feature for the bwf ill function-the ability to automatically detect and fill holes in objects.

Version $\mathbf{2 . 0}$ offered the fol lowing new features: support for 8-bit image data; support for manipulating RGB and multiframe images as multidimensional arrays; optimization of some 1.0 functions; and many new functions.

For a detailed description of the changes in Versions 2.0, 2.1, and 2.2, see the Release 11 New Features document.

For a list of all of the functions in the Image Processing Toolbox, see "F unctions by Category."

## Related Products

The MathWorks provides several products that are especially relevant to the kinds of tasks you can perform with the I mage Processing Tool box.

For more information about any of these products, see either:

- Theonline documentation for that product, if it is loaded or if you are reading the documentation from the CD
- TheM athWorks Web site, at ht t p: / / mwn. nat hwor ks. com seethe "products" section

Note The products listed below all include functions that extend the Image Processing Tool box's capabilities.

| Product | Description |
| :--- | :--- |
| Fuzzy Logic Tool box | Tool to hel p master fuzzy logic techniques and <br> their application to practical control problems |
| Mapping Tool box | Tool for analyzing and displaying <br> geographically based information from within <br> MATLAB |
| MATLAB | Integrated technical computing environment <br> that combines numeric computation, advanced <br> graphics and visualization, and a high-level <br> programming language |
| Neural Network Tool box | Comprehensive environment for neural <br> network research, design, and simulation <br> within MATLAB |
| Optimization Tool box | Tool for general and large-scale optimization of <br> nonlinear problems, as well as for linear <br> programming, quadratic programming, <br> nonlinear least squares, and solving nonlinear <br> equations |
| Signal Processing | Tool for algorithm development, signal and <br> linear system analysis, and time-series data <br> modeling |
| Tool box | Tool for analyzing historical data, modeling <br> systems, developing statistical algorithms, and <br> learning and teaching statistics |
| Statistics Tool box | Tool for signal and image analysis, <br> compression, and de-noising |
| Wavelet Tool box |  |

The Signal Processing Tool box and the Wavelet Tool box are closely related products. The Signal Processing Tool box is strongly recommended for 2-D FIR filter design to generate the inputs (1-D windows and 1-D filter prototypes) to the 2-D FIR design functions. (The Signal Processing Toolbox supports a wide
range of signal processing operations, from waveform generation to filter design and implementation, parametric modeling, and spectral analysis.)

The I mage Processing Tool box 2.2 requires MATLAB 5.3. The I mage Processing Tool box uses MATLAB as the computational engine for most of its algorithms. Additionally, MATLAB offers powerful capabilities, such as advanced data manipulation and analysis, that you can useto complement and enhance the features in the Image Processing Tool box.

See the MATLAB documentation for descriptions of the MATLAB Ianguage, including how to enter and manipulate data and how to use MATLAB's extensive collection of functions. It also explains how to create your own functions and scripts. The MATLAB Function Reference provides reference descriptions of the supplied MATLAB functions and commands.

## Post Installation Notes

To determine if the Image Processing Tool box is installed on your system, type this command at the MATLAB prompt:
ver
When you enter this command, MATLAB displays information about the version of MATLAB you are running, including a list of all toolboxes installed on your system and their version numbers.
For information about installing the tool box, see the MATLAB Installation Guidefor your platform.

[^0]
## About This Manual

This manual has four main parts:

- Chapter 1, "Getting Started", contains two step-by-step examples that will help you get started using the I mage Processing Tool box. This chapter is written as both an introduction to the most frequently used operations, as well as a demonstration of some of the image analysis that can be performed.
- Chapter 2, "Introduction", and Chapter 3, "Displaying and Printing Images", discuss working with image data and displaying images in MATLAB and the Image Processing Toolbox.
- Chapters 4 to 11 provide in-depth discussion of the concepts behind the software. Each chapter covers a different topic in image processing. For example, Chapter 7 discusses linear filtering, and Chapter 11 discusses binary image operations. Each chapter provides numerous examples that apply the toolbox to representative image processing tasks.
- Chapter 12, "Function Reference", gives a detailed reference description of each tool box function. Reference descriptions include a synopsis of the function's syntax, as well as a complete explanation of options. Many reference descriptions also include examples, a description of the function's algorithm, and references to additional reading material.


## User Experience Levels

This section gives brief suggestions for how to use the documentation, depending on your level of experience in using the tool box and MATLAB, and your knowledge of image processing concepts.

All new toolbox users should read Chapter 1, "Getting Started" and Chapter 2, "Introduction."

> Note If you are not familiar with MATLAB, it is strongly suggested that you start by reading and running the examples in Getting Started with MATLAB.

Users who are less knowledgeable about image processing concepts will find that the following chapters, in particular, contain valuable introductory discussions: Chapter 5, "Neighborhood and Block Operations", Chapter 6,
"Linear Filtering and Filter Design", Chapter 9, "Binary Image Operations", and Chapter 11, "Color."

Experienced tool box users should read the Release Notes. This guide is available as an online document that can be opened by clicking on its title at the top of the Contents tab of the MATLAB Help browser. To open the Help browser, select Help from the MATLAB desktop's View menu.

While experienced users may primarily prefer to use the reference chapters of this user guide, they should note that some functions are demonstrated in longer examples in the tutorial chapters. To see if a function has an example in a tutorial chapter, check the index entry of the function name.

## Words You Need to Know

At the beginning of each chapter we provide glossaries of key words you need to know in order to understand the information in the chapter. The chosen words are defined generally, and then sometimes include a MATLAB specific definition.

Many of the words are standard image processing terms that we definefor your convenience. In some cases, the words are included because they can sometimes be confusing, even for domain experts. Here are some examples:

- In image processing, one word is sometimes used to describe more than one concept. F or example, image resolution can be defined as the height and width of an image as a quantity of pixels in each direction, or it can be defined as the number of pixels per linear measure, such as 100 pixels per inch.
- In image processing, one concept is sometimes described by different terminology. F or example, a grayscaleimage can also be called an intensity image. We use the word intensity in our documentation and include a definition for it, because it may be unfamiliar to those who use the word "grayscale." (It is also defined in order to explain how MATLAB stores an intensity image.)

If you want to know whether a word is defined in one of the chapter glossaries, look up the word in the index. If we have defined it, theindex entry for theword will have a subentry of "definition."

F or terminol ogy that is new to you and not covered in our "Words You Need to Know" tables, we suggest you consult a more complete image processing glossary.

## Typographical Conventions

This manual uses some or all of these general MathWorks documentation conventions, as well as some special ones described after the following table..

| Item | Convention to Use | Example |
| :---: | :---: | :---: |
| Example code | Mbnospace font | To assign the value 5 to A , enter $A=5$ |
| Function names/syntax | Mbnospace font | The cos function finds the cosine of each array element. Syntax line example is MLGet Var M__var_name |
| Keys | Boldface with an initial capital letter | Press the Return key. |
| Literal strings (in syntax descriptions in Reference chapters) | Monospace bol d for literals | $\mathrm{f}=\mathrm{fr}$ eqspace( $\mathrm{n}, \mathrm{l}$ whol $\mathbf{e}^{\prime}$ ) |
| Mathematical expressions | Italics for variables Standard text font for functions, operators, and constants | This vector represents the polynomial $p=x^{2}+2 x+3$ |
| MATLAB output | Monospace font | MATLAB responds with A = |
| Menu names, menu items, and controls | Boldface with an initial capital letter | Choose the File menu. |


| Item | Convention to Use | Example |
| :--- | :--- | :--- |
| New terms | Italics | An array is an ordered <br> collection of information. |
| String variables (from a finite <br> list) | Mbnospace it tal i cs | sysc = d2c( sysd, ' met hod' ) |

## Image Processing Toolbox Typographical Conventions

We often use the variable names I , RGB, X, and BWin the code examples in this User Guide. I is used for intensity images, RGB for RGB images, X for indexed images, and BWfor binary images (where it stands for "black and white"). In addition, $n \not \square p$ is often used as a variable name for the colormap associated with an indexed image.
See Chapter 2, "I ntroduction" for more information about these different representations.

We use conventions to differentiate data ranges from MATLAB vectors. While both are enclosed by square brackets, there are the fol lowing differences: commas signify a range, the lack of commas and the use of the monospace font signify a MATLAB vector.
$[0,1]$ is a range of pixel values from 0 to 1 .
[ 0,255 ] is a range of pixel values from 0 to 255.
[ 0 1] is a vector of two values, 0 and 1 .

## Image Processing Demos

The Image Processing Tool box is supported by a full complement of demo applications. These are very useful as templates for your own end-user applications, or for seeing how to use and combine your tool box functions for powerful image analysis and enhancement. The tool box demos are located under the subdirectory,
. . . \TOOLBOX\ I MAGES I MDEMDS
under the top-level directory in which MATLAB is installed.
The table below lists the demos available. Demos whose names begin with "i pss" operate as slide shows.

The easiest way to run an individual demo is to enter its name at the MATLAB command prompt. You can also launch MATLAB demos from the MATLAB demo window. To invoke this window, type deno at the command prompt. To see the list of available image processing demos, double-click on Toolboxes from the list on the left, and then select Image Processing. Select the desired demo and click the Run button.

To view the code in a demo, type
edit demoname
at the MATLAB command prompt.
For information on what is happening in the demo and how to use it, press the Info button, which is located in the lower right corner of each demo window. All demos that are not slide shows offer a selection of images on which to operate and a number of settings for you to experiment with. Most of these demos also have an Apply button, which must be pressed to see the results of your new settings.

## Demos for the Image Processing Toolbox

| Demo Name | Brief Description |
| :---: | :---: |
| dct demo | Discrete cosine transform (DCT) image compression: you choose the number of coefficients and it shows you a reconstructed image and an error image. |
| edgedero | Edge detection: all supported types with optional manual control over threshold, direction, and sigma, as appropriate to the method used. |
| firdeno | 2-D Finite impulse response (FIR) filters: design your own filter by changing the cut-off frequency and filter order. |
| i madj deñ | Contrast adjustment and histogram equalization: adjust intensity values using brightness, contrast, and gamma correction, or by using histogram equalization. |
| i pss 001 | Connected components labeling slide show: includes double thresholding, feature-based logic, and binary morphology. All operations are performed on one image. |
| i pss 002 | Feature-based logic slide show containing two examples: the first example shows object selection using AND operations on the on pixels in two binary images; the second example shows filtering and thresholding on a single image. |
| i pss003 | Correction of nonuniform illumination slide show: creates a coarse approximation of the background, subtracts it from the image, and then adjusts the pixel intensity values to fill the entire range. |
| I andsat dem® | Landsat color composites: choose a scene and assign spectral bands to RGB intensities to create images that reveal topography, vegetation, and moisture; toggle saturation stretching to see its effect on image contrast. |

## Demos for the Image Processing Toolbox (Continued)

| Demo Name | Brief Description |
| :--- | :--- |
| nrfil t dem | Noise reduction using linear and nonlinear filters: <br> enables you to add different types of noise with variable <br> densities, and choose a filter neighborhood size. |
| qt deñ | Quadtree decomposition: enables you to select a <br> threshold and see a representation of the sparse <br> matrix, and a reconstruction of the original image. |
| roi deñ | Region of Interest (ROI) selection: enables you to select <br> an ROI and apply operations such as unsharp and fill. <br> It displays the binary mask of the ROI. |

## MATLAB Newsgroup

If you read newsgroups on the I nternet, you might be interested in the MATLAB newsgroup (comp. soft-sys. mat lab). This newsgroup gives you access to an active MATLAB user community. It is an excellent way to seek advice and to share algorithms, sample code, and M-files with other MATLAB users.

## Getting Started

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## Overview

This chapter contains two exercises to get you started doing image processing using MATLAB and the I mage Processing Tool box. The exercises include sections called "Here's What J ust H appened" so that you can read further about the operations you just used. In addition, the exercises contain cross-references to other sections in this manual that havein-depth discussions on the concepts presented in the examples.

Note If you are new to MATLAB, you should first read Getting Started with MATLAB.

All of the images displayed by the exercises in this chapter are supplied with the I mage Processing Tool box. Note that the images shown in this documentation differ slightly from what you see on your screen because the surrounding MATLAB figure window has been removed to save space.
"Exercise 1 - Some Basic Topics" covers the basic tasks of reading and di splaying an image, adjusting its contrast, and writing it back to disk. This exercise introduces you to one of the supported image types (the intensity image) and to one of the numeric storage classes used for images (ui nt 8). "Exercise 2 - Advanced Topics" includes more sophisticated topics, such as components labeling and feature measurement, which are two of the many specialized types of image processing that you can perform using the Image Processing Tool box.

## Exercise 1 - Some Basic Topics

Before beginning with this exercise, start MATLAB. You should already have installed the I mage ProcessingToolbox, which runs seamlessly from MATLAB. For information about installing the tool box, see the MATLAB Installation Guidefor your platform.

## 1. Read and Display an Image

Clear the MATLAB workspace of any variables and close open figure windows.
clear, close all
To read an image use the i mread command. Let's read in a TIFF image named pout. t if (which is one of the sample images that is supplied with the Image Processing Tool box), and store it in an array named I .

```
I =i mread('pout.tif');
```

Now call i ms how to display I.
i mshow (I)


## 2. Check the Image in Memory

Enter the whos command to see how I is stored in memory. whos

MATLAB responds with

| Name | Size | Bytes | Cl ass |
| :---: | :---: | ---: | :--- |
| I | $291 \times 240$ | 69840 | ui nt 8 array |
| Grand total is | 69840 | el ements using 69840 bytes |  |

## Here's What J ust Happened

Step 1. The i mead function recognized pout. tif as a valid TIFF file and stored it in the variableI. (For the list of graphics formats supported, see i mead in the "F unction Reference" chapter.)

The functions i mread and inshowread and display graphics images in MATLAB. In general, it is preferable to use i ms howfor displaying images because it handles the image-related MATLAB properties for you. (The MATLAB function i mage is for low-level programming tasks.)

Note that if pout.tif were an indexed image, the appropriate syntax for i mead would be,
[ $\mathrm{X}, \mathrm{map}$ ] = imead('pout.tif');
(For more information on the supported image types, see "I mage Types in the Toolbox" on page 2-5.)

Step 2. Y ou called the whos command to see how pout . tif had been stored into the MATLAB workspace. As you saw, pout . ti $f$ is stored as a 291-by-240 array. Since pout . ti f was an 8-bit image, it gets stored in memory as an ui nt 8 array. MATLAB can store images in memory as ui nt 8 , ui nt 16 , or doubl e arrays. (See "Reading a Graphics I mage" on page 2-14 for an explanation of when the different storage classes are used.)

## 3. Perform Histogram Equalization

As you can see, pout .tif is a somewhat low contrast image. To see the distribution of intensities in pout. tif in its current state, you can create a histogram by calling the imi st function. (Precede the call to i mist with the
fi gure command so that the histogram does not overwrite the display of the image I in the current figure window.)
figure, inmi st(I) \% Display a histogram of lin a new figure.


Notice how the intensity range is rather narrow. It does not cover the potential range of [ 0,255 ], and is missing the high and low values that would result in good contrast.

Now call hi st eq to spread the intensity values over the full range, thereby improving the contrast of I. Return the modified image in the variableI 2.

I2 = hi steq(I); \% Equalize I and out put in new array 12.
Display the new equalized image, I 2 , in a new figure window.
figure, inshow(12) \% Display the new equalized image 12.


Call i mis st again, this time for 12.
figure, i nhist(12) \% Show the hi stogramfor the new image 12.


See how the pixel values now extend across the full range of possible values.

## Here's What J ust Happened

Step 3. You adjusted the contrast automatically by using the function hi st eq to evenly distribute the image's pixel values over the full potential range for the storage class of the image. For an image $X$, with a storage class of ui nt 8 , the full range is $0 \leq X \leq 255$, for ui nt 16 it is $0 \leq X \leq 65535$, and for double it is $0 \leq X \leq 1$. Note that the convention elsewhere in this user guide (and for all MATLAB documentation) is to denote the above ranges as [0,255], [0,65535], and [0,1], respectively.

If you compare the two histograms, you can see that the histogram of $I 2$ is more spread out and flat than the histogram of I 1 . The process that flattened and spread out this histogram is called histogram equalization.

For more control over adjusting the contrast of an image (for example, if you want to chose the range over which the new pixel values should span), you can use thei madj ust function, which is demonstrated under " 6 . Adjust the Image Contrast" on page 1-17 in Exercise 2.

## 4. Write the Image

Write the newly adjusted image I 2 back to disk. Let's say you'd like to save it as a PNG file. Use i mwrite and specify a filename that includes the extension 'png'.
imwite (I2, ' pout 2. png');

## Here's What J ust Happened

Step 4. MATLAB recognized the file extension of ' png' as valid and wrote the image to disk. It wrote it as an 8-bit image by default because it was stored as a ui nt 8 intensity image in memory. If 12 had been an image array of type RGB and class ui nt 8, it would have been written to disk as a 24-bit image. If you want to set the bit depth of your output image, use the Bi t Dept h parameter with i mwrite. This example writes a 4-bit PNG file.
i mwrite(I 2, 'pout 2. png', 'Bi t Depth', '4' );
Note that all output formats do not support the same set of output bit depths. For example, the toolbox does not support writing 1-bit BMP images. See i mwrite in the "Reference" chapter for the list of valid bit depths for each format. See also "Writing a Graphics Image" on page 2-15 for a tutorial discussion on writing images using the Image Processing Tool box.

## 5. Check the Contents of the Newly Written File

Now, use the i nfi i nf o function to see what was written to disk. Be sure not to end the line with a semicol on so that MATLAB displays the results. Also, be sure to use the same path (if any) as you did for the call to i mwri te, above.
i minfo('pout 2. png' )
MATLAB responds with
ans $=$

```
Fil enane: ' pout 2. png'
FileMbdDate: ' 03-J un- 1999 15: 50: 25'
FileSi ze: 36938
For mat: ' png'
For mat Versi on: [ ]
W dth: 240
Hei ght: 291
Bi t Dept h: 8
Col or Type: ' grayscal e'
```

Note The value in the FileMbdDate field for your file will be different from what is shown above. It will show the date and time that you used i mwr i te to create your image. Note also that we truncated the number of field names and values returned by this call.

## Here's What J ust Happened

Step 5. When you called i mf inf o, MATLAB displayed all of the header fields for the PNG file format that are supported by the toolbox. You can modify many of these fields by using additional parameters in your call to i mwr ite. The additional parameters that are available for each file format are listed in tables in the reference entry for i mwrite. (See "Querying a Graphics File" on page 2-16 for more information about using i mfi nfo.)

## Exercise 2 - Advanced Topics

In this exercise you will work with another intensity image, rice. tif and explore some more advanced operations. The goals of this exercise are to remove the nonuniform background from ri ce. ti f , convert the resulting image to a binary image by using threshol ding, use components labeling to return the number of objects (grains or partial grains) in the image, and compute feature statistics.

## 1. Read and Display An Image

Clear the MATLAB workspace of any variables and close open figure windows. Read and display the intensity image rice.tif.

```
clear, cl ose all
| = imead('rice.tif');
i nshow(1)
```



## 2. Perform Block Processing to Approximate the Background

Notice that the background illumination is brighter in the center of the image than at the bottom. Use the bl kpr oc function to find a coarse estimate of the background illumination by finding the minimum pixel value of each 32-by-32 block in the image.

```
backApprox = bl kproc(I,[32 32],'min(x(:))');
```

To see what was returned to backAppr ox, type
backApprox
MATLAB responds with backApprox =

| 80 | 81 | 81 | 79 | 78 | 75 | 73 | 71 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 90 | 91 | 91 | 90 | 89 | 87 | 84 | 83 |
| 94 | 96 | 96 | 97 | 96 | 95 | 94 | 90 |
| 90 | 93 | 93 | 95 | 96 | 95 | 94 | 93 |
| 80 | 83 | 85 | 87 | 87 | 88 | 87 | 87 |
| 68 | 69 | 72 | 74 | 76 | 76 | 77 | 76 |
| 48 | 51 | 54 | 56 | 59 | 60 | 61 | 61 |
| 40 | 40 | 40 | 40 | 40 | 40 | 40 | 41 |

## Here's What J ust Happened

Step 1. You used the tool box functions i mead and i ms how to read and display an 8-bit intensity image. i mead and inshow are discussed in Exercise 1, in " 2 . Check the Image in Memory" on page 1-3, under the "Here's What J ust Happened" discussion.

Step 2. bl kproc found the minimum value of each 32-by-32 block of I and returned an 8-by-8 matrix, backAppr ox. You called bl kpr oc with an input image of $I$, and a vector of [ 32 32], which means that I will be divided into 32-by-32 blocks. bl kpr oc is an example of a "function function," meaning that it enables you to supply your own function as an input argument. You can pass in the name of an M -file, the variable name of an inline function, or a string containing an expression (this is the method that you used above). The function defined in the string argument (' min $\left.\mathrm{x}(:)^{\prime}\right)$ ' ) tells bl kproc what operation to perform on each block. For detailed instructions on using function functions, see Appendix A.

MATLAB's min function returns the minimum value of each column of the array within parentheses. To get the minimum value of the entire block, use the notation ( $x(:)$ ), which reshapes the entire block into a single column. For more information, see min in the MATLAB Function Reference.

## 3. Display the Background Approximation As a Surface

Use the surf command to create a surface display of the background approximation, backAppr ox. surf requires data of class doubl e, however, so you first need to convert backAppr ox using the doubl e command. You also need to divide the converted data by 255 to bring the pixel values into the proper range for an image of class doubl e, [01].
backApprox = doubl e(backApprox)/255; \% Convert i nage to double. figure, surf(backApprox);


To see the other side of the surface, reverse the $y$-axis with this command, set(gca,'ydir','reverse'); \%Reverse the y-axi s.


To rotate the surface in any direction, click on the rotate button in the tool bar (shown at left), then click and drag the surface to the desired view.

## Here's What J ust Happened

Step 3. You used the surf command to examine the background image. The surf command creates col ored parametric surfaces that enable you to view mathematical functions over a rectangular region. In the first surface display, $[0,0]$ represents the origin, or upper-left corner of the image. The highest part of the curve indicates that the highest pixel values of backAppr ox (and consequently ri ce. ti f) occur near the middle rows of the image. The lowest pixel values occur at the bottom of the image and are represented in the surface plot by the lowest part of the curve. Because the minimum intensity values in each block of this image make a smooth transition across the image, the surface is comprised of fairly smooth curves.

The surface plot is a Handle Graphics® object, and you can therefore fine-tune its appearance by setting properties. ("H andle Graphics" is the name for the collection of low-level graphics commands that create the objects you generate using MATLAB.) The call to reverse the y-axis is one of many property settings that you can make. It was made using the set command, which is used to set all properties. In the line,
set (gca, 'ydi r', 'reverse');
gca refers to the handle of the current axes object and stands for "get current axes." You can al so set many properties through the Property Editor. To invoke the Property Editor, open the figure window's Edit menu, and select Figure Properties, Axes Properties, or Current Object Properties. To select an object to modify with the Property Editor, click the property the following button on the figure window, $t$, then click on the object. You can also use the other buttons in the tool bar to add new text or line objects to your figure.

For information on working with MATLAB graphics, see the MATLAB graphics documentation.

## 4. Resize the Background Approximation

Our estimate of the background illumination is only 8 -by-8. Expand the background to the same size as the original background image (256-by-256) by using the i mesi ze function, then display it.
backApprox256 = i mesi ze(backApprox, [256 256], ' bilinear'); figure, inshow backApprox256) \% Show resi zed background i mage.


## Here's What J ust Happened

Step 4. You used i m esi ze with "bilinear" interpolation to resize your 8-by-8 background approximation, backAppr ox, to an image of size 256-by-256, so that it is now the same size as ri ce. ti f. If you compare it to ri ce.tif you can see that it is a very good approximation. The good approximation is possible because of the low spatial frequency of the background. A high-frequency background, such as a field of grass, could not have been as accurately approximated using so few blocks.

The interpolation method that you choose for i mresi ze determines the values for the new pixels you add to backAppr ox when increasing its size. (Note that interpolation is also used to find the best values for pixels when an image is decreased in size.) The other types of interpolation supported by i mresi ze are "nearest neighbor" (the default), and "bicubic." F or more information on interpolation and resizing operations, see "Interpolation" on page 4-4 and "Image Resizing" on page 4-6.

## 5. Subtract the Background Image from the Original Image

Now subtract the background image from the original image to create a more uniform background. First, change the storage class of I to doubl e, because subtraction can only be performed on doubl e arrays.

```
I = im2doubl e(I); % Convert l to storage class of double.
```

Now subtract backAppr ox 256 from I and store it in a new array, 12.
$12=1$ - backApprox256; \% Subtract the background froml.
Subtracting backAppr ox256 from I may yield some out-of-range values in the image. To correct the dynamic range of pixel values, use the max and min functions to clip pixel values outside the range [0,1].
$12=\max (\mathrm{min}(12,1), 0) ; \% \mathrm{Cl} \mathrm{p}$ the pixel val ues to the validrange.
Now display the image with its more uniform background.
figure, inshow( 12 )


## Here's What Just Happened

Step 5. Y ou subtracted a background approximation image from ri ce. ti f. B efore subtracting the background approximation it was necessary to convert the image to class doubl e. This is because subtraction, like many of MATLAB's mathematical operations, is only supported for data of class doubl e.

The ease with which you can subtract one image from another is an excellent example of how MATLAB's matrix-based design makes it a very powerful tool for image processing.

After subtraction was completed, another step was required before displaying the new image, because subtraction often leads to out-of- range values. You therefore used the min and max functions to clip any values outside the range of [01].

The following call

$$
12=\max (0, \min n(1,12)) ;
$$

can more easily be explained by dividing the expression into two steps, as follows.
l $2=\mathrm{min}(12,1)$;
replaces each value in I 2 that is greater than 1 with 1 , and
$12=\max (12,0)$;
replaces each value in I 2 that is less than 0 with 0 .
The Image Processing Toobox has a demo, i pss003, that approximates and removes the background from an image. For information on how to run this (and other demos), see "I mage Processing Demos" in the Preface.

## 6. Adjust the Image Contrast

The image is now a bit too dark. Use i madj ust to adjust the contrast.
13 = imadjust(I2, [0 $\max (12(:))]$, [ 0 1]); \%Adjust the contrast.
Display the newly adjusted image.


## Here's What J ust Happened

Step 6. You used the i madj ust command to increase the contrast in the image. i madj ust takes an input image and can also take two vectors: [ I ow hi gh] and [ bot tomt op]. Theoutput image is created by mapping the value I ow in the input image to the value bot tomin the output image, mapping the value hi gh in the input image to the valuet op in the output image, and linearly scaling the values in between. See the reference pages for i madj ust for more information.

The expression $\max (\mathrm{I} 2(:))$ that you entered as the hi gh value for the input image uses the MATLAB max command to reshape I 2 into a single column and return its maximum pixel value.

## 7. Apply Thresholding to the Image

Create a new binary threshol ded image, bw, by comparing each pixel in I 3 to a threshold value of 0. 2.

[^1]

Now call the whos command to see what type of array thethreshol ded image bw is.
whos
MATLAB responds with

| Name | Si ze | Byt es Cl ass |  |
| :--- | :---: | ---: | :--- |
|  |  |  |  |
| I $256 \times 256$ | 524288 | doubl e array |  |
| I 2 | 2566256 | 524288 | doubl e array |
| I 3 | $256 \times 256$ | 524288 | doubl e array |
| backApprox | $8 \times 8$ | 512 | doubl e array |
| backApprox256 | $256 \times 256$ | 524288 | doubl e array |
| bw | $256 \times 256$ | 524288 | doubl e array (logi cal) |

Grand total is 327744 el ements using 2621952 bytes

## Here's What J ust Happened

Step 7. Y ou compared each pixel in I 3 with a threshold value of 0. 2. MATLAB interprets this command as a logical comparison and therefore outputs values of 1 or 0 , where 1 means "true" and 0 means "false." The output value is 1 when the pixel in 13 is greater than 0.2 , and 0 otherwise.

Notice that when you call the whos command, you see the expression I ogi cal listed after the class for bw. This indicates the presence of a logical flag. Theflag indicates that bw is a logical matrix, and the I mage Processing Toolbox treats logical matrices as binary images. Thresholding using MATLAB's logical operators always results in a logical image. F or more information about binary images and the logical flag, see "Binary Images" on page 2-7.

Thresholding is the process of calculating each output pixel value based on a comparison of the corresponding input pixel with a threshold value. When used to separate objects from a background, you provide a threshold value over which a pixel is considered part of an object, and under which a pixel is considered part of the background. Dueto the uniformity of the background in I3 and its high contrast with the objects in it, a fairly wide range of threshold values can produce a good separation of the objects from the background. Experiment with other threshold values. Notethat if your goal were to calculate the area of the image that is made up of the objects, you would need to choose a more precise threshold value - one that would not allow the background to encroach upon (or "erode") the objects.

Note that the Image Processing Tool box also supplies the function i m2bw, which converts an RGB, indexed, or intensity imagetoa binary image based on the threshold value that you supply. Y ou could have used this function in place of the MATLAB command, $b w=13>0.2$. For example, bw = i m2bw $13,0.2$ ). See the reference page for i m2bw for more information.

## 8. Use Connected Components Labeling to Determine the Number of Objects in the Image

Usethebw abel function tolabel all of the connected components in the binary image bw.
[ I abel ed, numObj ects] = bw abel (bw, 4); \% Label components.
Show the number of objects found by bw abel .
num@bj ect s
MATLAB responds with
numobj ects $=$
80
You have just calculated how many objects (grains or partial grains of rice) are in rice.tif.

Note The accuracy of your results depends on a number of factors, including:

- The size of the objects
- The accuracy of your approximated background
- Whether you set the connected components parameter to 4 or 8
- The value you choose for thresholding
- Whether or not any objects are touching (in which case they may be labeled as one object)

In this case, some grains of rice are touching, so bw abel treats them as one object.

To add some color to the figure, display I abel ed using a vi brant colormap created by the hot function.

```
map = hot(num@bj ects+1); % Create a col ormap.
i mฐhow( I abel ed+1, map); % Of f set i ndi ces to col ormap by 1.
```



## Here's What J ust Happened

Step 8. You called bul abel to search for connected components and label them with unique numbers. bw abel takes a binary input image and a value of 4 or 8 to specify the "connectivity" of objects. The value 4, as used in this example, means that pixels that touch only at a corner are not considered to be "connected." For more information about the connectivity of objects, see "Connected-Components Labeling" on page 9-16.

A labeled image was returned in the form of an indexed image, where zeros represent the background, and the objects have pixel values other than zero (meaning that they are labeled). E ach object is given a unique number (you can see this when you go to the next step," 9 . Examine an Object"). The pixel values are indices into the col ormap created by hot.

Your last call to inshow uses the syntax that is appropriate for indexed images, which is,

```
i nshow(I abel ed+1, map);
```

Becausel abel ed is an indexed image, and 0 is meaningless as an index into a colormap, a value of 1 was added to all pixels before display. The hot function creates a col ormap of the size you specify. We created a colormap with one more col or than there are objects in the image because the first col or is used for the background. MATLAB has several col ormap-creating functions, including gray, pi nk, copper, and hsv. For information on these functions, see col or map in the MATLAB Function Reference.

Y ou can also return the number of objects by asking for the maximum pixel value in the image. F or example,
$\max (1$ abel ed(: ) )
ans $=$

80

## 9. Examine an Object

You may find it hel pful to takea closer look at I abel ed to see what bw abel has done to it. Use the i mer op command to select and display pixels in a region of I abel ed that includes an object and some background.
To ensure that the output is displayed in the MATLAB window, do not end the line with a semicol on. In addition, choose a small rectangle for this exercise, so that the displayed pixel values don't wrap in the MATLAB command window.

The syntax shown below makes i mer op work interactively. Y our mouse cursor becomes a cross-hair when placed over theimage. Click at a position in I abel ed where you would like to select the upper left corner of a region. Drag the mouse to create the selection rectangle, and release the button when you are done.
grai n=i merop(label ed) \%Crop a portion of Iabeled.
We chose the left edge of a grain and got the following results.
grain $=$

| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 60 | 60 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 0 | 0 | 0 | 0 | 0 | 60 | 60 | 60 | 60 |
| 0 | 0 | 0 | 60 | 60 | 60 | 60 | 60 | 60 |
| 0 | 0 | 0 | 60 | 60 | 60 | 60 | 60 | 60 |
| 0 | 0 | 0 | 60 | 60 | 60 | 60 | 60 | 60 |
| 0 | 0 | 0 | 60 | 60 | 60 | 60 | 60 | 60 |
| 0 | 0 | 0 | 60 | 60 | 60 | 60 | 60 | 60 |
| 0 | 0 | 0 | 0 | 0 | 60 | 60 | 60 | 60 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |

## Here's What J ust Happened

Step 9. You called i mer op and selected a portion of the image that contained both some background and part of an object. The pixel values were returned in the MATLAB window. If you examine the results above, you can see the corner of an object labeled with 60's, which means that it was the 60th object labeled by bul abel. Notice how the 60's create an edge amidst a background of 0's.

| 0 | 5 | 1 | 1 |  |  | 60 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 1 |  | 616 | 615 | 60 | 60 |
| 0 | 615 | 6.6 | 66 | 66 | 60 | 60 |
| 0 | 66 | 60 | 66 | 66 | 60 | 60 |
| 0 | 66 | 60 | 6.6 | 60 | 60 | 60 |
| 0 | 60 | 60 | 65 | 60 | 60 | 60 |
| 0 | 019 | 60 | 65 | 60 | 60 | 60 |
| 0 |  |  | 65 | 60 | 60 | 60 |
| 0 | 0 | 0 | 5 | 1 | 5 | 0 |
| 1 | 0 | 0 | 5 | 1 | [ |  |

i mer op can alsotake a vector specifying the coordinates for the crop rectangle. In this case, it does not operate interactively. For example, this call specifies a crop rectangle whose upper-left corner begins at $(15,25)$ and has a height and width of 10.

```
rect = [15 25 10 10];
roi = i merop(l abel ed, rect)
```

Y ou are not restricted to rectangular regions of interest. The tool box also has a roi pol y command that enables you to select polygonal regions of interest. Many image processing operations can be performed on regions of interest, including filtering and filling. See Chapter 10, "Region-Based Processing" for more information.

## 10. Compute Feature Measurements of Objects in the Image

The i mf eat ure command computes feature measurements for objects in an image and returns them in a structure array. When applied to an image with labeled components, it creates one structure element for each component. Use
i mff eat ur e to create a structure array containing some basic types of feature information for I abel ed.

```
    grai n=i nf eat ure(I abel ed, ' basi c' )
```

MATLAB responds with
grai $n=$
80x1 struct array with fiel ds:
Area
Centroid
Boundi ngBox
Find the area of the grain labeled with 51's, or "grain 51." To do this, use dot notation to access the data in the Ar ea field. Note that structure field names are case sensitive, so you need to capitalize the name as shown.
grai n(51). Ar ea
returns the following results
ans $=$
323
Find the smallest possible bounding box and the centroid (center of mass) for grain 51.
grai $n(51)$. Boundi ngBox, grai $n(51)$. Cent roid
returns
ans $=$
$\begin{array}{llll}141.5000 & 89.5000 & 26.0000 & 27.0000\end{array}$
ans $=$
155. 3437 102. 0898

Create a new vector, al I grai ns, which holds just the area measurement for each grain. Then call the whos command to see how al I grai ns is allocated in the MATLAB workspace.
al I grai $n s=[$ grai $n$. Area];
whos al I grai ns
MATLAB responds with

| Name | Size | Bytes Cl ass |  |
| :--- | ---: | ---: | :--- |
| al I grai ns | $1 \times 80$ | 640 | doubl e array |

Grand total is 80 el ements using 640 bytes
al I gr ai ns contains a one-row array of 80 elements, where each element contains the area measurement of a grain. Check the area of the 51st element of al l grai ns.
al I grai ns(51)
returns
ans $=$

323
which is the same result that you received when using dot notation to access the Ar ea field of grai ns(51).

## Here's What J ust Happened

Step 10. Y ou called i mf eat ur e to return a structure of basic feature measurements for each threshol ded grain of rice. i nf eat ur e supports many types of feature measurement, but setting the measur ements parameter to basi c is a convenient way to return three of the most commonly used measurements: the area, the centroid (or center of mass), and the bounding box. The bounding box represents the smallest rectangle that can contain a region, or in this case, a grain. The four-element vector returned by the Boundi ngBox field,
$\left[\begin{array}{llll}{[141.5000} & 89.5000 & 26.0000 & 27.0000\end{array}\right]$
shows that the upper left corner of the bounding box is positioned at [ 141. 5 89. 5], and the box has a width of 26.0 and a height of 27. 0. (The position is defined in spatial coordinates, hence the decimal values. For more information on the spatial coordinate system, see "Spatial Coordinates" on page 2-22.) F or more information about working with MATLAB structure arrays, see "Structures" in the MATLAB graphics documentation.

You used dot notation to access the Ar ea field of all of the elements of grain and stored this data toa new vector al I gr ai ns. This step simplifies anal ysis made on area measurements because you do not have to use field names to access the area.

## 11. Compute Statistical Properties of Objects in the Image

Now use MATLAB functions to calculate some statistical properties of the thresholded objects. First use max to find the size of the largest grain. (If you have followed all of the steps in this exercise, the "largest grain" is actually two grains that are touching and have been labeled as one object).

$$
\max (\text { al I grai ns })
$$

returns
ans $=$

Use the fi nd command to return the component label of this large-sized grain.
bi ggrai nर्= i nd( al I grai ns $=749$ )
returns
bi ggrai $\mathrm{n}=$
68
Find the mean grain size.
mean( al I grai ns)
returns
ans $=$
275. 8250

Make a histogram containing 20 bins that show the distribution of rice grain sizes.
hi st (al I grai ns, 20)


## Here's What J ust Happened

Step 11. Y ou used some of MATLAB's statistical functions, max, mean, and hi st to return the statistical properties for the thresholded objects in rice.tif.

The I mage Processing Tool box also has some statistical functions, such as mean2 and st d2, which are well suited to image data because they return a single value for two-dimensional data. The functions mean and st d were suitable here because the data in al I gr ai ns was one dimensional.

The histogram shows that the most common sizes for rice grains in this image are in the range of 300 to 400 pixels.

## Where to Go From Here

For more information about how the tool box handles image types and storage classes, or to learn more about reading and writing images, see Chapter 2, "Introduction." For instructions on displaying images of all types, please see Chapter 3, "Displaying and Printing Images."

Tutorial discussions for image processing operations are contained in the chapters starting with Chapter 5, "N eighborhood and Block Operations." Those chapters assume that you understand the information presented in the chapters starting with this chapter through Chapter 4, "Geometric Operations."

The reference pages for all of the I mage Processing Tool box functions are contained in Chapter 12, "Function Reference." These complement the M-file help that is displayed in the MATLAB command window when you type
hel p functi onname
For example,
hel p inshow

## Online Help

The I mage Processing Tool box User's Guide is available online in both HTML and PDF formats. To access the HTML help, select Help from View menu of theMATLAB desktop. Then, from theleft pane of the Help browser, expand the topic list next to I mage Processing Toolbox. To access the PDF help, click on Image Processing Toolbox in the Contents tab of the Help browser, and go to the hyperlink under "Printable Documentation (PDF)." (Note that to view the PDF help, you must have Adobe's Acrobat Reader installed.)

## Toolbox Demos

Some features of the I mage Processing Tool box are implemented in demo applications. The demos are useful for seeing the tool box features put into action and for borrowing codefor your own applications. See "I mage Processing Demos" in the Preface for a completelist and summary of the demos, as well as instructions on how to run them.

1 G etting Started

## Introduction

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## Overview

This chapter introduces you to the fundamentals of image processing using MATLAB and the I mage Processing Tool box. It describes the types of images supported, and how MATLAB represents them. It also explains the basics of working with image data and coordinate systems.

## Words You Need to Know

An understanding of the following terms will help you to use this chapter. For more explanation of this tableand others likeit, see "Words Y ou Need to K now" in the Preface.

| Words | Definitions |
| :--- | :--- |
| Binary image | An image containing only black and white pixels. In MATLAB, <br> a binary image is represented by a ui nt 8 or doubl e logi cal <br> matrix containing O's and l's (which usually represent black <br> and white, respectively). A matrix is logical when its "logical <br> flag" is turned "on." We often use the variable name BWto <br> represent a binary image in memory. |
| Image type | The defined relationship between array values and pixel <br> colors. The tool box supports binary, indexed, intensity, and <br> RGB image types. |
| Indexed image | An image whose pixel values are direct indices into an RGB <br> colormap. In MATLAB, an indexed image is represented by an <br> array of class ui nt 8, ui nt 16, or doubl e. The col ormap is <br> always an m-by-3 array of class doubl e. We often use the <br> variable name x to represent an indexed image in memory, <br> and map to represent the colormap. |


| Words | Definitions |
| :--- | :--- |
| Intensity image | An image consisting of intensity (grayscale) values. In <br> MATLAB, intensity images are represented by an array of <br> class ui nt 8, ui nt 16, or doubl e. While intensity images are not <br> stored with col ormaps, MATLAB uses a system col ormap to <br> display them. We often use the variable name I to represent <br> an intensity image in memory. This term is synonymous with <br> the term "grayscale." |
| Multiframe image | An image file that contains more than one image, or frame <br> When in MATLAB memory, a multiframe image is a 4-D array <br> where the fourth dimension specifies the frame number. This <br> term is synonymous with the term "multipage image." |
| RGB image | An image in which each pixel is specified by three values - <br> one each for the red, blue, and green components of the pixel's <br> col or. In MATLAB, an RGB image is represented by an <br> m-by-n-by-3 array of class ui nt 8, ui nt 16, or doubl e. We often <br> use the variable name RGB to represent an RGB image in <br> memory. |
| Storage class | The numeric storage class used to store an image in MATLAB. <br> The storage classes used in MATLAB are ui nt 8, ui nt 16, and <br> doubl e. Somefunction descriptions in the reference chapter of <br> this User's Guide have a section entitled "Class Support" that |
| specifies which image classes the function can operate on. |  |
| When this section is absent, the function can operate on all |  |
| supported storage classes. |  |

# Images in MATLAB and the Image Processing Toolbox 

The basic data structure in MATLAB is the array, an ordered set of real or complex elements. This object is naturally suited to the representation of images, real-valued, ordered sets of color or intensity data.

MATLAB stores most images as two-dimensional arrays (i.e., matrices), in which each element of the matrix corresponds to a single pixel in the displayed image. (Pixel is derived from picture element and usually denotes a single dot on a computer display.) For example, an image composed of 200 rows and 300 columns of different col ored dots would be stored in MATLAB as a 200-by-300 matrix. Some images, such as RGB, require a three-dimensional array, where the first plane in the third dimension represents the red pixel intensities, the second plane represents the green pixel intensities, and the third plane represents the blue pixel intensities.

This convention makes working with images in MATLAB similar to working with any other type of matrix data, and makes the full power of MATLAB available for image processing applications. F or example, you can select a single pixel from an image matrix using normal matrix subscripting.

## I ( 2,15 )

This command returns the value of the pixel at row 2, column 15 of the image I .

## Storage Classes in the Toolbox

By default, MATLAB stores most data in arrays of class doubl e. The data in these arrays is stored as double precision (64-bit) floating-point numbers. All of MATLAB's functions and capabilities work with these arrays.

For image processing, however, this data representation is not always ideal. The number of pixels in an image may be very large; for example, a 1000-by-1000 image has a million pixels. Since each pixel is represented by at least one array element, this image would require about 8 megabytes of memory.

In order to reduce memory requirements, MATLAB supports storing image data in arrays of class ui nt 8 and ui nt 16. The data in these arrays is stored as 8 -bit or 16 -bit unsigned integers. These arrays require one eighth or one fourth as much memory as doubl e arrays.

## Image Types in the Toolbox

The Image Processing Tool box supports four basic types of images.

- Index images
- Intensity images
- Binary images
- RGB images

This section discusses how MATLAB and the Image Processing Tool box represent each of these image types.

## Indexed Images

An indexed image consists of a data matrix, $X$, and a colormap matrix, map. $X$ can be of class ui nt 8 , ui nt 16, or doubl e. map is an m-by-3 array of class doubl e containing floating-point values in the range[0,1]. E ach row of mpp specifies the red, green, and blue components of a single color. An indexed image uses "direct mapping" of pixel values to colormap values. The color of each image pixel is determined by using the corresponding value of $X$ as an index into map. The value 1 points to the first row in map, the value 2 points to the second row, and so on.

A col ormap is often stored with an indexed image and is automatically loaded with the image when you usethei mead function. However, you are not limited to using the default col ormap-you can use any col ormap that you choose. The figure bel ow illustrates the structure of an indexed image. The pixels in the
image are represented by integers, which are pointers (indices) to col or values stored in the col ormap.


Figure 2-1: Pixel Values Are Indices to a Colormap in Index ed Images
The relationship between the values in the image matrix and the col ormap depends on the class of the image matrix. If the image matrix is of class doubl e, the value 1 points to the first row in the colormap, the value 2 points to the second row, and so on. If the image matrix is of class ui nt 8 or ui nt 16 , there is an offset - the value 0 points tothefirst row in the col ormap, the value 1 points to the second row, and so on. The offset is also used in graphics file formats to maximize the number of colors that can be supported. In the image above, the image matrix is of class doubl e. Because there is no offset, the value 5 points to the fifth row of the colormap.

Note that the tool box provides limited support for indexed images of class ui nt 16. Y ou can read these images into MATLAB and display them, but before you can process a ui nt 16 indexed image you must first convert it to either a doubl e or a ui nt 8 . To convert to a doubl e, call i m2doubl e; to reduce the image to 256 colors or fewer (ui nt 8) call i mappr ox. For more information, see the reference pages for i m2doubl e and i mapprox.

## Intensity Images

An intensity image is a data matrix, I, whose values represent intensities within somerange. MATLAB stores an intensity image as a single matrix, with each element of the matrix corresponding to one image pixel. The matrix can be of class doubl e, ui nt 8, or ui nt 16. While intensity images are rarely saved with a colormap, MATLAB uses a colormap to display them.

The elements in the intensity matrix represent various intensities, or gray levels, where the intensity 0 usually represents black and the intensity 1, 255, or 65535 usually represents full intensity, or white.

The figure below depicts an intensity image of class doubl e.


Figure 2-2: Pixel Values in an Intensity Image Define Gray Levels

## Binary Images

In a binary image, each pixel assumes one of only two discrete values. Essentially, these two values correspond to on and of f. A binary image is stored as a two-dimensional matrix of 0's (of f pixels) and l's (on pixels).

A binary image can be considered a special kind of intensity image, containing only black and white. Other interpretations are possible, however; you can also think of a binary image as an indexed image with only two col ors.

A binary image can be stored in an array of class doubl e or ui nt 8. (Thetoolbox does not support binary images of class ui nt 16.) An array of class ui nt 8 is generally preferable to an array of class doubl e, becausea ui nt 8 array uses far less memory. In the Image Processing Toolbox, any function that returns a binary image returns it as a ui nt 8 logical array. The tool box uses a logical flag to indicate the data range of a ui nt 8 logical array: if the logical flag is "on" the data range is [0,1]; if the logical flag is off, the tool box assumes the data range is $[0,255]$.)

The figure below depicts a binary image.


Figure 2-3: Pixels in A Binary Image Have Two Possible Values: 0 or 1

## RGB Images

An RGB image, sometimes referred to as a "truecol or" image, is stored in MATLAB as an m-by-n-by-3 data array that defines red, green, and blue col or components for each individual pixel. RGB images do not use a palette. The color of each pixel is determined by the combination of the red, green, and blue intensities stored in each col or plane at the pixel's location. Graphics file formats store RGB images as 24-bit images, where the red, green, and blue components are 8 bits each. This yields a potential of 16 million colors. The
precision with which a real-life image can be replicated has led to the commonly used term "truecolor image."

An RGB MATLAB array can be of class doubl e, ui nt 8, or ui nt 16. In an RGB array of class doubl e, each color component is a value between 0 and 1. A pixel whose col or components are ( $0,0,0$ ) displays as black, and a pixel whose color components are ( $1,1,1$ ) displays as white. The three color components for each pixel are stored along the third dimension of the data array. For example, the red, green, and blue color components of the pixel $(10,5)$ are stored in $\operatorname{RGB}(10,5,1), \operatorname{RGB}(10,5,2)$, and $\operatorname{RGB}(10,5,3)$, respectively.

Figure 2-4 depicts an RGB image of class doubl e.


Figure 2-4: The Color Planes of an RGB Image
To determine the color of the pixel at $(2,3)$, you would look at the RGB triplet stored in ( $2,3,1: 3$ ). Suppose $(2,3,1)$ contains the value $0.5176,(2,3,2)$ contains 0 . 1608 , and $(2,3,3)$ contains 0 . 0627 . The color for the pixel at $(2,3)$ is
0.51760 .16080 .0627

To further illustrate the concept of the three separate col or planes used in an RGB image, the code sample below creates a simple RGB image containing uninterrupted areas of red, green, and blue, and then creates one image for each of its separate color planes (red, green, and blue). It displays each color plane image separately, and also displays the original image.

```
RGB=r eshape( ones( 64, 1)*reshape(j et (64), 1, 192) , [ 64, 64, 3] );
R=RGB(:,:,1);
G=RGB(:,:, 2);
B=RGB(:,:,3);
i mshow(R)
fi gure, i mshow(G)
fi gure, i mshow( B)
fi gure, i mshow( RGB)
```



Red Plane


Green Plane


Blue Plane


Original Image

Figure 2-5: The Separated Color Planes of an RGB Image
Notice that each separated col or plane in the figure contains an area of white. The white corresponds to the highest values (purest shades) of each separate col or. F or example, in the "Red Plane" image, the white represents the highest
concentration of pure red values. As red becomes mixed with green or blue, gray pixels appear. The black region in the image shows pixel values that contain no red values, i.e., $\mathrm{R}=0$.

## Multiframe Image Arrays

F or some applications, you may need to work with collections of images related by time or view, such as magnetic resonance imaging (MRI) slices or movie frames.

The Image Processing Tool box provides support for storing multiple images in the same array. E ach separate image is called a frame If an array holds multiple frames, they are concatenated along the fourth dimension. For example, an array with five 400-by-300 RGB images would be 400-by-300-by-3-by-5. A similar multiframe intensity or indexed image would be 400-by-300-by-1-by-5.

Use the cat command to store separate images into one multiframe file. F or example, if you have group of images A1, A2, A3, A4, and A5, you can store them in a single array using

$$
A=\operatorname{cat}(4, A 1, A 2, A 3, A 4, A 5)
$$

You can also extract frames from a multiframe image. F or example, if you have a multiframe image MULTI, this command extracts the third frame.

$$
\text { FRMB }=\operatorname{MULTI}(:,:,:, 3)
$$

Note that in a multiframe image array, each image must be the same size and have the same number of planes. In a multiframe indexed image, each image must also use the same colormap.

## Multiframe Support Limitations

Many of the functions in the tool box operate only on the first two or first three dimensions. Y ou can still usefour-dimensional arrays with thesefunctions, but you must process each frame individually. F or example, this call displays the seventh frame in the array MLTI .

```
i mshow( MULTI (: , : , : , 7) )
```

If you pass an array to a function and the array has more dimensions than the function is designed to operate on, your results may be unpredictable. In some
cases, the function will simply process the first frame of the array, but in other cases the operation will not produce meaningful results.

See the reference pages for information about how individual functions work with the dimensions of an image array. For more information about displaying multiframe images, see Chapter 3, "Displaying and Printing I mages."

## Summary of Image Types and Numeric Classes

This table summarizes the way MATLAB interprets data matrix elements as pixel colors, depending on the image type and storage class.

| Image <br> Type | Class double | Class uint8 or uint16 |
| :--- | :--- | :--- |
| Binary | Image is an m-by-n array of <br> integers in the range $[0,1]$ <br> where the logical flag is on. | Image is an m-by-n array of <br> integers in the range $[0,1]$ <br> where the logical flag is on. |
| Indexed | Image is an m-by-n array of <br> integers in the range <br> $[1, p]$. | Image is an m-by-n array of <br> integers in the range <br> $[0, p-1]$. |
|  | Colormap is a p-by-3 array <br> of floating-point values in <br> the range $[0,1]$. | Colormap is a p-by-3 array of <br> floating-point values in the <br> range $[0,1]$. |


| Image <br> Type | Class double | Class uint8 or uint16 |
| :--- | :--- | :--- |
| Intensity | Image is an m-by-n array of <br> floating-point values that <br> are linearly scaled by <br> MATLAB to produce <br> col ormap indices. The <br> typical range of values is [0, <br> $1]$. | Image is an m-by-n array of <br> integers that are linearly <br> scaled by MATLAB to <br> produce colormap indices. <br> The typical range of values <br> is [0, 255] or [0, 65535]. |
|  | Colormap is a p-by-3 array <br> of floating-point values in <br> the range [0, 1] and is <br> typically grayscale. | Colormap is a p-by-3 array of <br> floating-point values in the <br> range [0, 1] and is typically <br> grayscale. |
| RGB <br> (Truecolor) | Image is an m-by-n-by-3 <br> array of floating-point <br> values in the range [0, 1]. | Image is an m-by-n-by-3 <br> array of integers in the <br> range [0, 255] or [0, 65535]. |

## Working with Image Data

MATLAB provides commands for reading, writing, and displaying several types of graphics file formats images. As with MATLAB-generated images, once a graphics file format image is displayed, it becomes a Handle Graphics® Image object. MATLAB supports the following graphics file formats:

- BMP (Microsoft Windows Bitmap)
- HDF (Hierarchical Data Format)
- J PEG (J oint Photographic Experts Group)
- PCX (Paintbrush)
- PNG (Portable Network Graphics)
- TIFF (Tagged Image File Format)
- XWD (X Window Dump)

For the latest information concerning the bit depths and/or image types supported for these formats, see the reference pages for i mread and inwrite.

This section discusses how to read, write, and work with graphics images. It also describes how to convert the storage class or graphics format of an image.

## Reading a Graphics Image

Thefunction i mread reads an image from any supported graphics image file in any of thesupported bit depths. Most of the images that you will read are 8-bit. When these are read into memory, MATLAB stores them as class ui nt 8. The main exception to this rule is that MATLAB supports 16 -bit data for PNG and TIFF images. If you read a 16-bit PNG or TIFF image, it will be stored as class ui nt 16 .

Note For indexed images, i mread always reads the colormap into an array of class doubl e, even though the image array itself may be of class ui nt 8 or ui nt 16 .

Toseethe many syntax variations for reading an image, see the referenceentry for i mread. For our discussion here we will show one of the most basic syntax uses of i m ead. This example reads the image ngc6543a. j pg.

```
RGB = i mread(' ngc6543a.j pg' );
```

You can write image data using the imrite function. The statements

```
I oad cl own
i mwrite( X, map, ' cl own. bmp' )
```

create a BMP file containing the clown image.

## Writing a Graphics Image

The function i mur it e writes an image to a graphics file in one of the supported formats. If the image is of class ui nt 8 and the format you choose supports 8 -bit images, by default the image is written as 8 -bit. If the image is of class doubl e, MATLAB's default behavior is to scale the data to class ui nt 8 before writing it to file, since most graphics file format images do not support double-precision data. When the image is of class ui nt 16, there are two possible default outcomes: if you write an image of class ui nt 16 to a format that supports 16-bit images (PNG or TIFF ), it is written as a 16 -bit file; if you write to a format that does not support 16-bit files, MATLAB first scales the data to class ui nt 8, as it does for images of class doubl e.

The most basic syntax for i mwri te takes the image variable name and a filename. If you include an extension in the filename, MATLAB infers the desired file format from it. This example writes an RGB image RGB to a BMP file.

```
i mwrite( RGB,' myfil e. bmp' );
```

For some graphics formats, you can specify additional parameters. One of the additional parameters for PNG files sets the bit depth. This example writes an intensity imagel to a 4-bit PNG file.

```
i mwrite(I,' cl own. png',' Bi t Dept h' ,4) ;
```

(The bit depths and image types supported for each format are shown in the reference pages for i mwrite.)

This example writes an image A to a J PEG file with a compression quality setting of 100 (the default is 75).

```
i mwrite( A, ' myfil e.j pg', 'Qual ity', 100);
```

See the reference entry for i mwr i t e for more information.

## Querying a Graphics File

The i nfi inf o function enables you to obtain information about graphics files that are in any of the formats supported by the tool box. The information you obtain depends on the type of file, but it always includes at least the following:

- Name of the file, including the directory path if the file is not in the current directory
- File format
- Version number of the file format
- File modification date
- File size in bytes
- Image width in pixels
- Image height in pixels
- Number of bits per pixel
- Image type: RGB (truecolor), intensity (grayscale), or indexed

See the reference entry for i mf i nf o for more information.

## Converting The Image Type of Images

For certain operations, it is hel pful to convert an image to a different image type. For example, if you want to filter a color image that is stored as an indexed image, you should first convert it to RGB format. When you apply the filter to the RGB image, MATLAB filters the intensity values in the image, as is appropriate. If you attempt to filter the indexed image, MATLAB simply applies the filter to the indices in the indexed image matrix, and the results may not be meaningful.

The Image Processing Tool box provides several functions that enable you to convert any image to another image type. These functions have mnemonic names; for example, i nd2gr ay converts an indexed image to a grayscale intensity format.

Note that when you convert an image from oneformat to another, the resulting image may look different from the original. F or example, if you convert a color indexed image to an intensity image, the resulting image is grayscale, not col or. F or moreinformation about how thesefunctions work, seetheir reference pages.

The table below summarizes these image conversion functions.

| Function | Purpose |
| :--- | :--- |
| di ther | Create a binary image from a grayscale intensity image <br> by dithering; create an indexed image from an RGB <br> image by dithering |
| gr ay2i nd | Create an indexed image from a grayscale intensity <br> image |
| gr aysl i ce | Create an indexed image from a grayscale intensity <br> image by thresholding |
| i m2bw | Create a binary image from an intensity image, <br> indexed image, or RGB image, based on a luminance <br> threshold |
| i nd2gr ay | Create a grayscale intensity image from an indexed <br> image |
| i nd2gr ay | Create an RGB image from an indexed image |
| mat 2gr ay | Create a grayscale intensity image from data in a <br> matrix, by scaling the data |
| rgb2gr ay | Create a grayscale intensity image from an RGB image |
| rgb2i nd | Create an indexed image from an RGB image |

You can also perform certain conversions just using MATLAB syntax. For example, you can convert an intensity image to RGB format by concatenating three copies of the original matrix along the third dimension.

$$
\text { RGB }=\operatorname{cat}(3,1,1,1) \text {; }
$$

The resulting RGB image has identical matrices for the red, green, and blue planes, so the image displays as shades of gray.
In addition to these standard conversion tools, there are some functions that return a different image type as part of the operation they perform. For example, the region of interest routines each return a binary image that you
can use to mask an indexed or intensity image for filtering or for other operations.

## Color Space Conversions

The I mage Processing Tool box represents col ors as RGB values, either directly (in an RGB image) or indirectly (in an indexed image). H owever, there are other methods for representing colors. F or example, a col or can be represented by its hue, saturation, and value components (HSV). Different methods for representing colors are called color spaces.

The tool box provides a set of routines for converting between RGB and other col or spaces. The image processing functions themsel ves assume all col or data is RGB, but you can process an image that uses a different color space by first converting it to RGB, and then converting the processed image back to the original color space. F or more information about color space conversion routines, see Chapter 11, "Color."

## Working with uint8 and uint16 Data

Use i m ead to read graphics images into MATLAB as ui nt 8 or ui nt 16 arrays; use i ns how to display these images; and use i nwr i t e to save these images. Most of the functions in thel mage Processing Tool box accept ui nt 8 and ui nt 16 input. See the reference entries for more information about i mread, inshow, ui nt 8 , and ui nt 16 .

MATLAB provides limited support for storing images as 8-bit or 16-bit unsigned integers. In addition to reading and writing ui nt 8 and ui nt 16 arrays, MATLAB supports the following operations:

- Displaying data values
- Indexing into arrays using standard MATLAB subscripting
- Reshaping, reordering, and concatenating arrays, using functions such as reshape, cat, and per mit e
- Saving to and loading from MAT-files
- The all and any functions
- Logical operators and indexing
- Relational operators
- The find function. Note that the returned array is of class doubl e.


## Mathematical O perations Support for uint8 and uint16

The following MATLAB mathematical operations support ui nt 8 and ui nt 16 data: conv2, convn, fft2, fftn, sum In these cases, the output is always double.

If you attempt to perform an unsupported operation on one of these arrays, you will receive an error. For example,
$B V B=B W I+B V D$
??? Function ' + ' not defined for variables of class 'uint 8 '.

## Converting The Storage Class of Images

If you want to perform operations that are not supported for ui nt 8 or ui nt 16 arrays, you can convert the data to double precision using the MATLAB function, doubl e. For example,

```
BVB = doubl e(BVI) + doubl e(BVZ);
```

However, converting between storage classes changes the way MATLAB and the tool box interpret the image data. If you want the resulting array to be interpreted properly as image data, you need to rescale or offset the data when you convert it.

For easier conversion of storage classes, use one of these tool box functions: i m2doubl e, i m2ui nt 8, and i m2ui nt 16. These functions automatically handle the rescaling and offsetting of the original data. For example, this command converts a double-precision RGB image with data in the range [ 0,1 ] to a ui nt 8 RGB image with data in the range $[0,255]$.
RGB2 = i m2ui nt 8( RGB1) ;

Note that when you convert from one class to another that uses fewer bits to represent numbers, you generally lose some of the information in your image. For example, a ui nt 16 intensity image is capable of storing up to 65,536 distinct shades of gray, but a ui nt 8 intensity image can store only 256 distinct shades of gray. If you convert a ui nt 16 intensity image to a ui nt 8 intensity image, i m2ui nt 8 must quantizethe gray shades in the original image. In other words, all values from 0 to 128 in the original image become 0 in the ui nt 8 image, values from 129 to 385 all become 1, and so on. This loss of information is often not a problem, however, since 256 still exceeds the number of shades of gray that your eye is likely to discern.

In an indexed image, the image matrix contains only indices into a colormap, rather than the color data itself, so there is no quantization of the color data possible during the conversion. Therefore, it is not always possible to convert an indexed image from one storage class to another. F or example, a ui nt 16 or doubl e indexed image with 300 colors cannot be converted to ui nt 8 , because ui nt 8 arrays have only 256 distinct values. If you want to perform this conversion, you must first reduce the number of the colors in the image using thei mapprox function. This function performs the quantization on the colors in the col ormap, to reduce the number of distinct colors in the image. See "Using imapprox" on page 11-12 for more information. F or more information on the storage class conversion functions see the reference pages for i m2doubl e, i mqui nt 8, i mZui nt 16.

## Turning the Logical Flag on or off

As discussed in "Binary Images" on page 2-7, a ui nt 8 binary image must have its logi cal flag on. If you usei mui nt 8 to convert a binary image of class doubl e to ui nt 8 , this flag is turned on automatically. If you do the conversion manually, however, you must use the I ogi cal function to turn on the logical flag. For example,

$$
B=I \text { ogi cal }(\text { ui nt } 8(\text { round }(A))) ;
$$

To turn the logical flag off, you can use the unary plus operator. F or example, if A is a ui nt 8 logical array,

$$
B=+A ;
$$

## Converting the Graphics File Format of an Image

Sometimes you will want to change the graphics format of an image, perhaps for compatibility with another software product. You can do this by reading in the image with i m ead, and then calling i mur i te with the appropriate format setting specified. F or example, to convert an image from a BMP to a PNG, read the BMP image using i mead, convert the storage class if necessary, and then write the image using i mwr i te, with 'PNG' specified as your target format. For the specifics of which bit depths are supported for the different graphics formats, and for how to specify the format type when writing an image to file, see the reference entries for i mread and i morite.

## Coordinate Systems

Locations in an image can be expressed in various coordinate systems, depending on context. This section discusses the two main coordinate systems used in the Image Processing Toolbox, and the relationship between them. These two coordinate systems are described in

- "Pixel Coordinates"
- "Spatial Coordinates"


## Pixel Coordinates

Generally, the most convenient method for expressing locations in an image is to use pixel coordinates. In this coordinate system, the image is treated as a grid of discrete elements, ordered from top to bottom and left to right, as illustrated by Figure 2-6.


Figure 2-6: The Pixel Coordinate System
F or pixel coordinates, the first component r (the row) increases downward, while the second component c (the column) increases to the right. Pixel coordinates are integer values and range between 1 and the length of the row or column.

There is a one-to-one correspondence between pixel coordinates and the coordinates MATLAB uses for matrix subscripting. This correspondencemakes the relationship between an image's data matrix and the way the image displays easy to understand. F or example, the data for the pixel in the fifth row, second column is stored in the matrix el ement $(5,2)$.

## Spatial Coordinates

In the pixel coordinate system, a pixel is treated as a discrete unit, uniquely identified by a single coordinate pair, such as (5,2). From this perspective, a location such as $(5.3,2.2)$ is not meaningful.
At times, however, it is useful to think of a pixel as a square patch. From this perspective, a location such as $(5.3,2.2)$ is meaningful, and is distinct from $(5,2)$. In this spatial coordinate system, locations in an image are positions on a plane, and they are described in terms of $x$ and $y$ (not $r$ and $c$ as in the pixel coordinate system).

Figure 2-7 illustrates the spatial coordinate system used for images. Notice that y increases downward.


Figure 2-7: The Spatial Coordinate System
This spatial coordinate system corresponds closely to the pixel coordinate system in many ways. For example, the spatial coordinates of the center point of any pixel are identical to the pixel coordinates for that pixel.
There are some important differences, however. In pixel coordinates, the upper-left corner of an image is (1,1), while in spatial coordinates, this location by default is $(0.5,0.5)$. This difference is due to the pixel coordinate system being discrete, while the spatial coordinate system is continuous. Also, the upper-left corner is always ( 1,1 ) in pixel coordinates, but you can specify a nondefault origin for the spatial coordinate system. See "Using a Nondefault Spatial Coordinate System" on page 2-23 for more information.

Another potentially confusing difference is largely a matter of convention: the order of the horizontal and vertical components is reversed in the notation for
these two systems. As mentioned earlier, pixel coordinates are expressed as ( $r, c$ ), while spatial coordinates are expressed as ( $x, y$ ). In the reference pages, when the syntax for a function uses $r$ and $c$, it refers to the pixel coordinate system. When the syntax uses $x$ and $y$, it refers to the spatial coordinate system.

## Using a Nondefault Spatial Coordinate System

By default, the spatial coordinates of an image correspond with the pixel coordinates. For example, the center point of the pixel in row 5, column 3 has spatial coordinates $x=3, y=5$. (Remember, the order of the coordinates is reversed.) This correspondence simplifies many of the tool box functions considerably. Several functions primarily work with spatial coordinates rather than pixel coordinates, but as long as you are using the default spatial coordinate system, you can specify locations in pixel coordinates.

In some situations, however, you may want to use a nondefault spatial coordinate system. F or example, you could specify that the upper-left corner of an image is the point $(19.0,7.5)$, rather than $(0.5,0.5)$. If you call a function that returns coordinates for this image, the coordinates returned will be values in this nondefault spatial coordinate system.

To establish a nondefault spatial coordinate system, you can specify the XDat a and YDat a image properties when you display the image. These properties are two-el ement vectors that control the range of coordinates spanned by the image. By default, for an image $A$, XDat a is [ $1 \operatorname{size}(A, 2)$ ], and YDat a is [1 size(A, 1)].

For example, if A is a 100 row by 200 column image, the default XDat a is [ 1 200], and the default YDat a is [ 1 100]. The values in these vectors are actually the coordinates for the center points of the first and last pixels (not the pixel edges), so the actual coordinate range spanned is slightly larger; for instance, if XDat a is [ 1 200], the $x$-axis range spanned by the image is [0.5 200.5].

These commands display an image using nondefault XDat a and YDat a.

```
A = nagic(5);
x = [ 19.5 23.5];
y = [8.0 12.0];
i mage(A,' XData',x,'YData',y), axi s i mage, col ormap(j et(25))
```



See the reference page for i ns how for information about the syntax variations that specify nondefault spatial coordinates.

## Displaying and Printing Images

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## Overview

The Image Processing Tool box supports a number of image display techniques. For example, the function ins how displays any supported image type with a single function call. Other functions handle more specialized display needs. This chapter describes basic display techniques for each image type supported by the tool box (e.g., RGB, intensity, and soon.), as well as how to set thetoolbox preferences for the i ns how function. It also discusses special display techniques, such as multiple image display and texture mapping. The final pages of this chapter include information about printing images and troubleshooting display problems

## Words You Need to Know

An understanding of the following terms will help you to use this chapter. For moreexplanation of this tableand others likeit, see "Words Y ou Need to K now" in the Preface.

| Words | Definitions |
| :--- | :--- |
| Color approximation | There are two ways in which this term is used in MATLAB: <br> - The method by which MATLAB chooses the best col ors for <br> an image whose number of col ors you are decreasing <br> - MATLAB's automatic choice of screen col ors when <br> displaying on a system with limited col or display capability |
| Screen bit depth | The number of bits per screen pixel |
| Screen color resolution | The number of distinct colors that can be produced by the <br> screen |

## Displaying Images with imshow

In MATLAB, the primary way to display images is by using the imge function. This function creates a Handle Graphics ${ }^{\circledR}$ image object, and it includes syntax for setting the various properties of the object. MATLAB al so includes the i magesc function, which is similar to i mage but which automatically scales the input data.

The I mage Processing Tool box includes an additional display routine called i ms how. Like i mage and i magesc, this function creates a Handle Graphics image object. However, i nゅ how also automatically sets various Handle Graphics properties and attributes of the image to optimize the display.

This section discusses displaying images using i ms how. In general, using i ms how for image processing applications is preferable to using i mage and i magesc. It is easier to use and in most cases, displays an image using one image pixel per screen pixel. (F or more information about i mage and i magesc, see their pages in the MATLAB F unction Reference or see the MATLAB graphics documentation.)

Note One of the most common tool box usage errors is using the wrong syntax of i ns howfor your image type. This chapter shows which syntax is appropriate for each type of image. If you need help determining what type of image you are working with, see "I mage Types in the Tool box" on page 2-5.

## Displaying Indexed Images

To display an indexed image with i nshow, specify both the image matrix and the colormap.
i nshow $X, \operatorname{map}$ )
For each pixel in X, inshow displays the color stored in the corresponding row of map. The relationship between the values in the image matrix and the col ormap depends on whether the image matrix is of class doubl e, ui nt 16, or ui nt 8 . If the image matrix is of class doubl e, the value 1 points to the first row in the colormap, the value 2 points to the second row, and so on. If the image matrix is of class ui nt 8 or ui nt 16 , there is an offset; the value 0 points to the first row in the colormap, the value 1 points to the second row, and so on. (The
offset is handled automatically by the image object, and is not controlled through a Handle Graphics property.)

Each pixel in an indexed image is directly mapped to its corresponding col ormap entry. If the colormap contains a greater number of colors than the image, the extra colors in the colormap will simply be ignored. If the col ormap contains fewer col ors than the image requires, all image pixels over the limits of the colormap's capacity will be set to the last col or in the col ormap, i.e., if an image of class ui nt 8 contains 256 colors, and you display it with a colormap that contains only 16 colors, all pixels with a value of 15 or higher are displayed with the last color in the colormap.

To change the default behavior of i mゅhow, set the tool box preferences. See "Setting the Preferences for imshow" on page 3-24 for more information.

## The Image and Axes Properties of an Indexed Image

In most cases, it is not necessary to concern yourself with the Handle Graphics property settings made when you call i nฐhow. Therefore, this section is not required reading, but rather information for those who really "want to know."

When you display an indexed image, i ns howsets the Handle Graphics properties that control how colors display, as follows:

- The image CDat a property is set to the data in $X$.
- The image CDat aMapping property is set to di rect .
- The axes CLi mproperty does not apply, because CDat aMappi ng is set to di rect.
- The figure Col or map property is set to the data in map.


## Displaying Intensity Images

To display a intensity (grayscale) image, the most basic syntax is
i mshow (I)
i ns how displays the image by scaling the intensity values to serve as indices into a grayscale colormap. If I is doubl e, a pixel value of 0.0 is displayed as black, a pixel value of 1.0 is displayed as white, and pixel values in between are displayed as shades of gray. If I is ui nt 8, then a pixel value of 255 is displayed as white. If I is ui nt 16, then a pixel value of 65535 is displayed as white.

Intensity images are similar to indexed images in that each uses an m-by-3 RGB colormap, but normally, you will not specify a col ormap for an intensity image. MATLAB displays intensity images by using a grayscale system colormap (where $\mathrm{R}=\mathrm{G}=\mathrm{B}$ ). By default, the number of levels of gray in the colormap is 256 on systems with 24 -bit color, and 64 or 32 on other systems. (See "Working with Different Screen Bit Depths" on page 11-4 for a detailed explanation.)

Another syntax form of i ns how for intensity images enables you to explicitly specify the number of gray levels to use. To display an image I with 32 gray levels, specify a value for $n$.
imshow (I, 32)
Because MATLAB scales intensity images to fill the colormap range, a colormap of any size can be used. Larger col ormaps enable you to see more detail, but they also use up more color slots. The availability of color slots is discussed further in "Displaying Multiple Images" on page 3-19, and also in "Working with Different Screen Bit Depths" on page 11-4.

To change the default behavior of inshow, set the tool box preferences. See "Setting the Preferences for imshow" on page 3-24 for more information.

## Displaying Intensity Images That Have Unconventional Ranges

In some cases, you may have data you want to display as an intensity image, even though the data is outside the conventional toolbox range (i.e., [0,1] for doubl e arrays, $[0,255]$ for ui nt 8 arrays, or $[0,65535]$ for ui nt 16 arrays). For example, if you filter an intensity image, some of the output data may fall outside the range of the original data.

To display unconventional range data as an image, you can specify the data range directly, using

```
i nshow(I,[l ow hi gh])
```

If you use an empty matrix ([ ] ) for the data range, i mฐhowscales the data automatically, setting I ow and hi gh to the minimum and maximum values in the array. The next example filters an intensity image, creating unconventional range data. ins how is then called using an empty matrix.

```
I = i mead('test pat1.tif');
J = filter2([1 2;-1 - 2],l);
min(J(:)) %i nd the mi ni mum pi xel val ue of the filtered image.
```

```
ans =
    -364
max(J(:)) %%ind the maxi mum pi xel val ue of the filtered image.
ans =
    7 2 3
i nshow(J,[]);
```



When you use this syntax, i ns howsets the axes CLi mproperty to [ I ow hi gh] . CDat aMapping is always scal ed for intensity images, so that I ow corresponds to the first row of the grayscale colormap and hi gh corresponds to the last row.

## The Image and Axes Properties of an Intensity Image

In most cases, it is not necessary to concern yourself with the H andle Graphics property settings made when you call i mฐhow. Therefore, this section is not required reading, but rather information for those who really "want to know."

When you display an intensity image, i ns how sets the Handle Graphics properties that control how colors display, as follows:

- The image CDat a property is set to the data in I
- The image CDat aMapping property is set to scal ed.
- The axes CLi mproperty is set to [0 1] if the image matrix is of class doubl e, [0 255] if the matrix is of class ui nt 8, or [0 65535] if it is of class ui nt 16.
- The figure Col or map property is set to a grayscale colormap whose values range from black to white.


## Displaying Binary Images

To display a binary image, the syntax is
i mshow BW)
In MATLAB, a binary image is a logical two-dimensional ui nt 8 or doubl e matrix that contains only 0's and 1's. (The tool box does not support ui nt 16 binary images.) All tool box functions that return a binary image, return them as ui nt 8 logical arrays.

Generally speaking, working with binary images with the tool box is very straightforward. In most cases you will load a 1-bit binary image, and MATLAB will create a logical ui nt 8 image in memory. You will normally not encounter doubl e binary images unless you create them yourself using MATLAB.

If you load an image with a bit depth greater than 1 bit per pixel, or use MATLAB to create a new doubl e or ui nt 8 image containing only 0's and 1's, you may encounter unexpected results. For example, the mere presence of all 0's and l's does not always indicate a binary image. For MATLAB to interpret the image as binary, it must be logical, meaning that its logical flag must be turned "on." Therefore, intensity images that happen to contain only 0's and I's are not binary images.

To change the default behavior of inshow, set the tool box preferences. See "Setting the Preferences for imshow" on page 3-24 for more information.

This example underscores the importance of having the logical flag turned on if you want your image to behave like a binary image.

Create an image of class doubl e that contains only 0's and 1's.

```
BVL = zeros(20, 20);
BVI ( 2: 2: 18, 2: 2: 18) =1;
i mshow( BW1, ' notruesi ze' );
```



```
whos
\begin{tabular}{lcrl} 
Name & Size & Bytes & Cl ass \\
BhZ & \(20 \times 20\) & 3200 & doubl e array
\end{tabular}
Grand total is 400 el ements using 3200 bytes
```

While this image may look like a binary image, it is really a grayscale imageit will not be recognized as a binary image by any tool box function. If you were to save this image to a file (without specifying a bit depth) it would be saved as an 8 -bit grayscale image containing 0 's and 255 's.

The fact that BVI is not really a binary image becomes evident when you convert it to class ui nt 8.

BVR=ui nt 8( BW1) ;
fi gure, i nshow BVR, ' not ruesi ze' )


BV1 still contains 0's and 1's, but since the dynamic range of an ui nt 8 intensity image is [0 255], the value 1 is very close to black.

To make BVI a true binary image use the NOT EQUAL (~=) operator, which will turn the logical flag on.

B B $=\mathrm{BVR} \sim=0$;
fi gure, i nฐhow (BVB, ' not ruesi ze' )

whos

| Name | Size | Bytes | Cl ass |
| :--- | :---: | ---: | :--- |
| BVR | $20 \times 20$ | 3200 | doubl e array |
| BVR | $20 \times 20$ | 400 | ui nt 8 array |
| BVB | $20 \times 20$ | 400 ui nt 8 array (l ogi cal) |  |
| Grand total is | 1225 | el ements using 4025 bytes |  |

Write BVB to a file using one of the formats that supports writing 1-bit images. You will not need to specify a bit depth, because MATLAB automatically saves logical ui nt 8 or doubl e images as 1-bit images if the file format supports it.
imwite(BVB, 'grid.tif'); \% MATLAB supports writing 1-bit TIFFs.
You can check the bit depth of grid. tif by calling infinfo. As you will see, the Bi t Dept h field indicates that it has been saved as a 1-bit image, with the beginning of your output looking something like this.

```
i nfinfo('BVL.tif')
ans =
```

```
            Filename: 'd:\mystuff\grid.tif'
```

            Filename: 'd:\mystuff\grid.tif'
            Fil eMbdDate: ' 25- Nov-1998 11: 36: 17'
            Fil eMbdDate: ' 25- Nov-1998 11: 36: 17'
            FileSi ze: 340
            FileSi ze: 340
            Format: 'tif'
            Format: 'tif'
    Format Versi on: [ ]
Format Versi on: [ ]
W dt h: }2

```
            W dt h: }2
```

Hei ght: 20
Bit Depth: 1
Col or Type: ' grayscal e'
Format Si gnat ure: [ 737342 0]
ByteOrder: 'little-endi an'
NewSubfileType: 0
BitsPer Sampl e: 1
Compressi on: ' CCl TT 1D'

Note You may have noticed that the Col orType field of the binary image queried above has a value of ' gr ayscal e' . MATLAB sets this field to one of three values: ' gr ayscal e' , 'i ndexed' , and 'truecol or' . When reading an image, MATLAB evaluates the image type by checking both the Bi t Dept h and the Col or Type fields.

## Changing the Display Colors of a Binary Image

You may prefer to invert binary images when you display them, so that 0 values display as white and 1 values display as black. To do this, use the NOT $(\sim)$ operator in MATLAB. For example,

```
BW = i mread(` ci rcles.tif');
i nshow -BW
```



You can also display a binary image using a colormap. If the image is of class ui nt 8, 0's display as the first color in the colormap, and 1's values display as
the second color. For example, the following command displays 0's as red and 1's as blue.

```
i nshow( BW[ 1 0 0; 0 0 1])
```



Figure 3-1: Binary Image Displayed with a Colormap
If the image is of class doubl e, you need to add 1 to each value in the image matrix, because there is no offset in the colormap indexing.

```
BW = doubl e( BW);
i nฐhow BW + 1,[lllllll
```


## The Image and Axes Properties of a Binary Image

In most cases, it is not necessary to concern yourself with the Handle Graphics property settings made when you call i ms how. Therefore, this section is not required reading, but rather information for those who really "want to know."
i ms howsets the Handle Graphics properties that control how colors display, as follows:

- The image CDat a is set to the data in BW
- The image CDat aMapping property is set to di rect .
- The axes CLi mproperty is set to [0 1].
- The figure Col or map property is set to a grayscale colormap whose values range from black to white.


## Displaying RGB Images

RGB images, also called truecol or images, represent col or values directly, rather than through a colormap.

To display an RGB image, the most basic syntax is
i mshow (RGB)
RGB is m-by-n-by-3 array. F or each pixel ( $r$, c) in RGB, i nshowdisplays the color represented by the triplet ( $r, c, 1: 3$ ).

Systems that use 24 bits per screen pixel can display truecolor images directly, because they allocate 8 bits ( 256 levels) each to the red, green, and blue col or planes. On systems with fewer colors, MATLAB displays the image using a combination of col or approximation and dithering. See "Working with Different Screen Bit Depths" on page 11-4 for more information.

To change the default behavior of i nshow, set the tool box preferences. See "Setting the Preferences for imshow" on page 3-24 for more information.

## The Image and Axes Properties of an RG B Image

In most cases, it is not necessary to concern yourself with the H andle Graphics property settings made when you call i mshow. Therefore, this section is not required reading, but rather information for those who really "want to know."

When you display an RGB image, i ns howsets the Handle Graphics properties that control how colors display, as follows.

- The image CDat a property is set to the data in RGB. The data will be three-dimensional. When CDat a is three-dimensional, MATLAB interprets the array as truecol or data, and ignores the values of the CDat aMappi ng, CLi m and Col or map properties.
- The image CDat aMappi ng property is ignored.
- The axes CLi mproperty is ignored.
- The figure Col or map property is ignored.


## Displaying Images Directly from Disk

Generally, when you want to display an image, you will first use i m ead to load it and the data is stored as one or more variables in the MATLAB workspace. However, if you do not want to load an image before displaying it, you can display a file directly using this syntax.
i nshow filename
The file must be in the current directory or on the MATLAB path.
For example, to display a file named fl ower s.tif,
i nshow fl owers.tif
If the image has multiple frames, i mshow will only display the first frame. For information on the display options for multiframe images, see "Displaying Multiframe Images" on page 3-15.

This syntax is very useful for scanning through images. Note, however, that when you use this syntax, the image data is not stored in the MATLAB workspace. If you want to bring the image into the workspace, use the get i mage function, which gets the image data from the current Handle Graphics image object. For example,
rgb = geti mage;
will assign fl owers. tif torgb if the figure window in which it is displayed is currently active.

## Special Display Techniques

In addition to imshow, the tool box includes functions that perform specialized display operations, or exercise more direct control over the display format. These functions, together with the MATLAB graphics functions, provide a range of image display options.

This section includes the following topics:

- "Adding a Col orbar" on page 3-14
- "Displaying Multiframe Images" on page 3-15
- "Displaying Multiple Images" on page 3-19
- "Zooming in on a Region of an Image" on page 3-26
- "Texture Mapping" on page 3-28


## Adding a Colorbar

Use the col or bar function to add a colorbar to an axes object. If you add a col orbar to an axes object that contains an image object, the col orbar indicates the data values that the different colors in the image correspond to.

Seeing the correspondence between data values and the colors displayed by using a col orbar is especially useful if you are displaying unconventional range data as an image, as described under "Displaying Intensity Images That Have Unconventional Ranges" on page 3-5.

In the example below, a grayscale image of class ui $n t 8$ is filtered, resulting in data that is no longer in the range $[0,255]$.

```
I = imead('saturn.tif');
h = [1 2 1; 0 0 0; -1-2-1];
l2 = filter2(h,l);
i mshow ( 2, []), col orbar
```



Figure 3-2: Image Displayed with Colorbar

## Displaying Multiframe Images

A multiframe image is an image file that contains more than one image. The MATLAB-supported formats that enable the reading and writing of multiframe images are HDF and TIFF. See "Multiframe Image Arrays" on page 2-11 for more information about reading and writing multiframe images.

Once read into MATLAB, the image frames of a multiframe image are always handled in the fourth dimension. Multiframe images can be loaded from disk using a special syntax of i mread, or created using MATLAB. Multiframe images can be displayed in several different ways; to display a multiframe image, you can

- Display the frames individually, using the i ns howfunction. See "Displaying the Frames of a Multiframe Image Individually" on page 3-16 below.
- Display all of theframes at once, using the mont age function. See "Displaying All Frames of a Multiframe Image at Once" on page 3-17.
- Convert the frames to a movie, using the i mmovi e function. See "Converting a Multiframe I mage to a Movie" on page 3-18.


## Displaying the Frames of a Multiframe Image Individually

In MATLAB, the frames of a multiframe image are handled in the fourth dimension. To view an individual frame, call i ns how and specify the frame using standard MATLAB indexing notation. F or example, to view the seventh frame in the intensity array I ,
inshowl(:,:,: 7) )
The following example loads mi i tif and displays the third frame.

```
%Initialize an array to hold the 27 frames of mi.tif
mmi = ui nt8(zeros(128,128,1,27));
for frame=1:27
    % Read each frame into the appropriate frame in memory
    [mi(:,:,:,frame),map] = imead('mi.tif',frame);
end
i mshow mmi(:, :, : , 3) , map);
```



Intensity, indexed, and binary multiframe images have a dimension of m-by-n-by-1-by-k, where $k$ represents the total number of frames, and 1 signifies that the image data has just one col or plane. Therefore, the following call,

```
i nshow mmi(: , : , : 3) , m⿴囗 );
```

is equivalent to,
i nshow mi ( : , : , 1, 3) , map) ;
RGB multiframe images have a dimension of m-by-n-by-3-by-k, where $k$ represents the total number of frames, and 3 signifies the existence of the three color planes used in RGB images. This example,

[^2]shows all three color planes of the seventh frame，and is not equivalent to i mゅhow RGB（ ：，：，3，7））；
which shows only the third col or plane（blue）of the seventh frame．These two calls will only yield the same results if the image is $R G B$ grayscale（ $R=G=B$ ）．

## Displaying All Frames of a Multiframe Image at 0 nce

To view all of the frames in a multiframe array at one time，use the nont age function．mont age divides a figure into multiple display regions and displays each image in a separate region．

The syntax for mont age is similar to the i ns howsyntax．To display a multiframe intensity image，the syntax is
mont age（I）
To display a multiframe indexed image，the syntax is
mont age（ $X$ ，map）

Note All of the frames in a multiframe indexed array must use the same colormap．

This example loads and displays all frames of a multiframe indexed image．

```
%Initialize an array to hold the 27 frames of mri.tif.
mmi = ui nt8(zeros(128, 128, 1, 27) );
for frame=1:27
    % Read each frame into the appropriate frame in menory.
    [mi(:,:,:,fram巴),m\not=] = immead('mi.tif',frame);
end
mont age( mri, m⿴囗) ;
```



Figure 3-3: All Frames of Multiframe Image Displayed in One Figure
Notice that mont age displays images in a row-wise manner. The first frame appears in the first position of the first row, the next frame in the second position of the first row, and so on. mont age arranges the frames so that they roughly form a square.

## Converting a Multiframe Image to a Movie

To create a MATLAB movie from a multiframe image array, use the i movi e function. This function works only with indexed images; if your images are of another type, you must first convert them using one of the conversion functions described in "Converting The I mage Type of Images" on page 2-16.

This call creates a movie from a multiframe indexed image $X$
nov = i movi e( $X, \operatorname{mpp}$ );
where $X$ is a four-dimensional array of structures that you want to use for the movie.

You can play the movie in MATLAB using the movi e function.
col or map( n¥p), novi e( mov);
Note that when you play the movie, you need to supply the col ormap used by the original image array.

This example loads the multiframe image mi . ti f and makes a movie out of it. It won't do any good to show the results here, so try it out; it's fun to watch.

```
%Initialize and array to hold the 27 frames of mi.tif.
mi = ui nt 8(zeros(128, 128, 1, 27) );
for frame=1: 27
    % Read each frame into the appropriate frame in memory.
    [mi(:,:,:,frame),map] = imead('mi.tif',frame);
end
nov = i mmovi e(mil,mp);
col ormmp(n@p), movi e(mov);
```

Note that i nmovi e displays the movie as it is being created, so you will actually see the movie twice. The movie runs much faster the second time (using movi e).

Note MATLAB movies require MATLAB in order to be run. To make a movie that can be run outside of MATLAB, you can use the MATLAB avi file and addf $r$ ane functions to create an AVI file. AVI files can be created using indexed and RGB images of classes ui nt 8 and doubl e, and don't require a multiframe image. For instructions on creating an AVI file, see the "Devel opment Environment."

## Displaying Multiple Images

MATLAB does not place any restrictions on the number of images you can display simultaneously. However, there are usually system limitations that
are dependent on the computer hardware you are using. The sections below describe how to display multiple figures separately, or within the same figure.

The main limitation is the number of colors your system can display. This number depends primarily on the number of bits that areused to storethe col or information for each pixel. Most systems use either 8,16 , or 24 bits per pixel.

If you are using a system with 16 or 24 bits per pixel, you are unlikely to run into any problems, regardless of the number of images you display. However, if your system uses 8 bits per pixel, it can only display a maximum of 256 different colors, and you can therefore quickly run out of color slots if you display multiple images. (Actually, the total number of col ors you can display is slightly fewer than 256, because some col or slots are reserved for Handle Graphics objects. The operating system usually reserves a few colors as well.)

To determine the number of bits per pixel on your system, enter this command.
get ( 0, ' ScreenDept h' )
See "Working with Different Screen Bit Depths" on page 11-4 for more information.

This section discusses

- Displaying each image in a separate figure
- Displaying multiple images in the same figure

It also includes information about working around system limitations.

## Displaying Each Image in a Separate Figure

The simplest way to display multiple images is to display them in different figure windows. i nshow always displays an image in the current figure, so if you display two images in succession, the second image replaces the first image. To avoid replacing the image in the current figure, use the fi gure command to explicitly create a new empty figure before calling ins howfor the next image. F or example,
i nshow (1)
figure, inshow( 12 )
figure, inshow( 13 )
When you use this approach, the figures you create are empty initially.

If you have an 8-bit display, you must make sure that the total number of col ormap entries does not exceed 256. F or example, if you try to display three images, each having a different colormap with 128 entries, at least one of the images will display with the wrong colors. (If all three images have identical colormaps, there will not be a problem, because only 128 color slots are used.) Remember that intensity images are also displayed using colormaps, so the color slots used by these images count toward the 256-color total.

In the next example, two indexed images are displayed on an 8-bit display. Since these images do not have similar col ormaps and due to the limitation of the screen col or resolution, the first image is forced to use the col ormap of the second image, resulting in an inaccurate display.
[ X1, map1] \#ं mead(' forest.tif');
[ X2, map2] \#i mead('trees.tif');
i mshow (X1, map1), fi gure, i nshow X2, map2) ;



Figure 3-4: Displaying Two Indexed Images on an 8-bit Screen
As X2 is displayed, X1 is forced to use X2's col ormap (and now you can't see the forest for the trees). Note that the actual display results of this example will vary depending on what other application windows are open and using up system col or slots.

One way to avoid these di splay problems is to manipulate the col ormaps to use fewer colors. There are various ways to do this, such as using the i mappr ox function. See "Reducing the Number of Colors in an Image" on page 11-6 for information.

Another solution is to convert images to RGB (truecol or) format for display, because MATLAB automatically uses dithering and color approximation to display these images. Use the i nd2rgb function to convert indexed images to RGB.
i nshow i nd2rgb( $X, n \not m p)$ )
Or, simply use the cat command to display an intensity image as an RGB image.

```
i mshow(cat(3,1,I,I))
```


## Displaying Multiple Images in the Same Figure

You can display multiple images in a single figure window with some limitations. This discussion shows you how to do this in one of two ways:

1 By using inshowin conjunction with subpl ot

2 By using subi mage in conjunction with subpl ot
subpl ot divides a figure into multiple display regions. The syntax of subpl ot is subpl ot ( $m n, p$ )

This syntax divides the figure into an m-by-n matrix of display regions and makes the pth display region active.
For example, if you want to display two images side by side, use

```
[ X1, mpp1] = m mead(' forest.tif' );
[ X2, map2] # mmead('trees.tif');
subpl ot (1, 2, 1), i mshow( X1, map2)
subpl ot (1, 2, 2), i mshow X2, map2)
```



Figure 3-5: Two Images in Same Figure Using the Same Colormap
If sharing a colormap (using the subpl ot function) produces unacceptable display results as Figure 3-5 shows, use the subi nage function (shown below). Or, as another alternative, you can map all images to the same col ormap as you load them. See "Colormap Mapping" on page 11-11 for more information.
subi mage converts images to RGB before displaying and therefore circumvents the col ormap sharing problem．This example displays the same two images shown in Figure 3－5 with better results．

```
[X1, map1] # mread(' forest.tif');
[ X2, map2] # mmead('trees.tif');
subpl ot (1, 2, 1), subi mage( X1, n⿴囗十()
subpl ot (1, 2, 2), subi mage( X2, n⿴p2)
```



Figure 3－6：Two Images in Same Figure Using Separate Colormaps

## Setting the Preferences for imshow

The behavior of i ms howis influenced in part by the current settings of the tool box preferences．Depending on the arguments you specify and the current settings of the tool box preferences，i nshow may
－Suppress the display of axes and tick marks．
－Include or omit a＂border＂around the image．
－Call the tr uesi ze function to display the image without interpolation．
－Set other figure and axes properties to tailor the display．

All of these settings can be changed by using the i pt set pr ef function, and the tr uesi ze preference, in particular, can also be changed by setting the di spl ay_opt i on parameter of i ns how. This section describes how to set the tool box preferences and how to use the di spl ay_opti on parameter.

When you display an image using the imshowfunction, MATLAB also sets the Handle Graphics figure, axes, and image properties, which control the way image data is interpreted. These settings are optimized for each image type. The specific properties set are described under the following sections:

- "The Image and Axes Properties of an Indexed Image" on page 3-4
- "The Image and Axes Properties of an Intensity Image" on page 3-6
- "The Image and Axes Properties of a Binary Image" on page 3-11
- "The Image and Axes Properties of an RGB I mage" on page 3-12


## Toolbox Preferences

The tool box preferences affect the behavior of $i$ nshow for the duration of the current MATLAB session. You can change these settings at any time by using thei pt set pr ef function. To preserve your preference settings from one session to the next, make your settings in your st ar t up. mfile. These are the preferences that you may set.

- The InshowBor der preference controls whether ins how displays the figure window as larger than the image (leaving a border between the image axes and the edges of the figure), or the same size as the image (leaving no border).
- The I ns howAxesVi si bl e preference controls whether i ms how displays images with the axes box and tick labels.
- Thel nshowTr uesi ze preference controls whether i mshowcalls thet ruesi ze function. This preference can be overridden for a single call to i ms how, see "The truesize Function" below for more details.
- TheTrueSi zeVar ni ng preference controls whether you will receive a warning message if an image is too large for the screen.

This examplecall to i pt set pr ef resizes the figure window so that it fits tightly around displayed images.
i pt set pref('I nshowBor der', 'tight');
To determine the current value of a preference, use the i pt get pr ef function.

F or more information about tool box preferences and the values they accept, see the reference entries for i pt get pr ef and i pt set pr ef.

## The truesize Function

Thet ruesi ze function assigns a single screen pixel to each image pixel, e.g., a $200-\mathrm{by}$ - 300 image will be 200 screen pixels in height and 300 screen pixels in width. This is generally the preferred way to display an image. In most situations, when the tool box is operating under default behavior, i ms how calls the $t r$ uesi ze command automatically before displaying an image.

In some cases, you may not want i ms how to automatically call truesi ze (for example, if you are working with a small image). If you display an image without calling tr uesi ze, the image displays at the default axis size. In such cases, MATLAB must use interpolation to determine the values for screen pixels that do not directly correspond to elements in the image matrix. (See "Interpolation" on page 4-4 for more information.)

There are two ways to affect whether or not MATLAB will automatically call truesize:

1 Set the preference for the current MATLAB session. This example sets the I ms howTr uesi ze preference to ' manual ' , meaning that truesi ze will not be automatically called by i mshow.
i pt set pr ef ('I nshowTr uesi ze' , ' manual ' )
2 Set the preference for a single i ns how command by setting the di spl ay_opt $i$ on parameter. This example sets the di spl ay_opt $i$ on parameter to truesi ze, so that truesi ze is called for the image displayed, regardless of the current preference setting.
i mshow (X, map,'truesize')
For more information see the reference descriptions for inshowand truesize.

## Zooming in on a Region of an Image

The simplest way to zoom in on a region of an image is to use the zoom buttons provided on the figure window. To enable zooming from the command line, use the zoomcommand. When you zoom in, the figure window remains the same size, but only a portion of the image is displayed, at a higher magnification.
(zoomworks by changing the axis limits; it does not change the image data in the figure.)

Once zooming in is enabled, there are two ways to zoom in on an image:
1 Single mouse click: click on a spot in the image by placing the cursor on the spot and the pressing the left mouse button. The image is magnified and the center of the new view is the spot where you clicked.

2 Click and drag the mouse: select a region by clicking on the image, holding down the left mouse button, and dragging the mouse. This creates a dotted rectangle. When you release the mouse button, the region enclosed by the rectangle is displayed with magnification.

## Zooming In or O ut W ith the Zoom Buttons

The zoom buttons in the MATLAB figure enable you to zoom in or out on an image using your mouse.

To zoom in, click the "magnifying glass" button with the plus sign in it. There are two ways to zoom in on an image after selecting the zoom in button. See "Zooming in on a Region of an Image" above.

To zoom out, click the "magnifying glass" button with the minus sign in it. Click your left mouse button over the spot in the image you would like to zoom out from.

## Zooming In or Out from the Command Line

The zoomcommand enables you to zoom in or out on an image using your mouse.

To enable zooming (in or out), type zoom on

There are two ways to zoom in on an image. See "Zooming in on a Region of an Image" above.
To zoom out, click on the image with the right mouse button. (If you have a single-button mouse, hold down the Shift key and click.)

To zoom out completely and restore the original view, enter
zoom out

To disable zooming, enter
$z o o m$ of $f$

## Texture Mapping

When you use the i mshow command, MATLAB displays the image in a two-dimensional view. However, it is also possible to map an image onto a parametric surface, such as a sphere, or below a surface plot. The war p function creates these displays by texture mapping the image. Texture mapping is a process that maps an image onto a surface grid using interpolation.

This example texture maps an image of a test pattern onto a cylinder.
[ $x, y, z$ ] = cylinder;
l =imead('testpat 1.tif');
war $p(x, y, z, l)$;


Figure 3-7: An Image Texture Mapped onto a Cylinder
The image may not map onto the surface in the way that you had expected. One way to modify the way the texture map appears is to change the settings of the Xdi $r$, Ydi $r$, and Zdi $r$ properties. For more information, see Changing Axis Direction in the MATLAB graphics documentation.

For more information about texture mapping, see the reference entry for the warp function.

## Printing Images

If you want to output a MATLAB image to use in another application (such as a word-processing program or graphics editor), use i mur it e to create a file in the appropriate format. See "Writing a Graphics I mage" on page 2-15 for details.

If you want to print the contents of a MATLAB figure (including nonimage elements such as labels), use the MATLAB pri int command, or choose the Print option from the File menu of the figure window. Notethat if you produce output in either of these ways, the results reflect the settings of various Handle Graphics properties. In some cases, you may need to change the settings of certain properties to get the results you want.

Here are some tips that may be hel pful when you print images.

- Image colors print as shown on the screen. This means that images are not affected by the I nvert Har dcopy figure property.
- To ensure that printed images have the proper size and aspect ratio, you should set the figure's Paper Posi ti onMbde property to aut o. When Paper Positi onMbde is set to aut o, the width and height of the printed figure are determined by the figure's dimensions on the screen. By default, the value of Paper Posi ti onMbde is manual. If you want the default value of Paper Positi onMbde to be aut o, you can add this line to your st art up. mfile.

```
set(0,' Def aul t Fi gur ePaper Posi ti onMbde',' auto' )
```

For detailed information about printing with File/Print or the pri int command (and for information about Handle Graphics), see "Printing and Exporting Figures with MATLAB" in in the MATLAB graphics documentation. For a complete list of options for the print command, enter hel p print at the MATLAB command line prompt or see print in the MATLAB Function Reference.

## Troubleshooting

This section contains three common scenarios (in bold text) which can occur unexpectedly, and what you can do to derive the expected results.

My color image is displaying as grayscale. Your image must be an indexed image, meaning that it should be displayed using a col ormap. Perhaps you did not use the correct syntax for loading an indexed image, which is,

```
[ \(\mathrm{X}, \mathrm{map}\) ] \(\ddagger \mathrm{mread}(\) ' fil ename. ext' \()\);
```

Also, be sure to use the correct form of $i$ ns how for an indexed image.
i nshow (X, nap) ;
See "Displaying I ndexed Images" on page 3-3 for more information about displaying indexed images.

My binary image displays as all black pixels. Check to see if its logical flag is "on."To do this, either use the i sl ogi cal command or call whos. If theimage is logical, the whos command will display the word "logical" after the word "array" under the class heading. If you have created your own binary image, chances are it is of class ui nt 8 , where a value of 1 is nearly black. Remember that the dynamic range of a ui nt 8 intensity image is [0 255], not [0 1]. For more information about valid binary images, see "Displaying Binary I mages" on page 3-7.

I have loaded a multiframe image but MATLAB only displays one frame. You must load each frame of a multiframe image separately. This can be done using a f or loop, and it may be helpful to first use i mf i nf o to find out how many frames there are, and what their dimensions are. To see an example that loads all of the frames of a multiframe image, go to "Displaying the Frames of a Multiframe Image Individually" on page 3-16.

## 3-32

## Geometric Operations

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Words You Need to Know ..... 4-2
Interpolation ..... 4-4
Image Types ..... 4-5
Image Resizing ..... 4-6
Image Rotation ..... 4-7
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## Overview

This chapter describes the geometric functions, which are basic image processing tools. Thesefunctions modify the geometry of an image by resizing, rotating, or cropping the image. They support all image types.

The chapter begins with a discussion of interpolation, an operation common to most of the geometric functions. It then discusses each of the geometric functions separately, and shows how to apply them to sample images.

## Words You Need to Know

An understanding of the following terms will help you to use this chapter. For more explanation of this table eand others likeit, see "Words Y ou Need to Know" in the Preface.

| Words | Definitions |
| :--- | :--- |
| Aliasing | Artifacts in an image that can appear as a result of reducing <br> an image's size. When the size of an image is reduced, original <br> pixels are downsampled to create fewer pixels. Aliasing that <br> occurs as a result of size reduction normally appears as <br> stair-step patterns (especially in high contrast images), or as <br> Moire (ripple-effect) patterns. |
| Anti-aliasing | Any method for preventing aliasing (see above). The method <br> discussed in this chapter is interpolation (see below). |
| Bicubic interpolation | Output pixel values are calculated from a weighted average of <br> pixels in the nearest 4-by-4 neighborhood. |
| Bilinear interpolation | Output pixel values are calculated from a weighted average of <br> pixels in the nearest 2-by-2 neighborhood. |
| Geometric operation | An operation that modifies the spatial relations between <br> pixels in an image. Examples include resizing (growing or <br> shrinking), rotating, and shearing. |


| Words | Definitions |
| :--- | :--- |
| Interpolation | The process by which we estimate an image value at a location <br> in between image pixels. |
| Nearest neighbor <br> interpolation | Output pixel values are assigned the value of the pixel that <br> the point falls within. No other pixels are considered. |

## Interpolation

Interpolation is the process by which we estimate an image value at a location in between image pixels. For example, if you resize an image so it contains more pixels than it did originally, the software obtains values for theadditional pixels through interpolation. The i mesi ze and i mot at e geometric functions use two-dimensional interpolation as part of the operations they perform. (The i mpr of i I e image analysis function also uses interpolation. See "Intensity Profile" on page 8-5 for information about this function.)

The Image Processing Tool box provides three interpol ation methods:

- Nearest neighbor interpolation
- Bilinear interpolation
- Bicubic interpolation

The interpolation methods all work in a fundamentally similar way. In each case, to determine the value for an interpolated pixel, you find the point in the input image that the output pixel corresponds to. You then assign a value to the output pixel by computing a weighted average of some set of pixels in the vicinity of the point. The weightings are based on the distance each pixel is from the point.
The methods differ in the set of pixels that are considered.

- For nearest neighbor interpolation, the output pixel is assigned the value of the pixel that the point falls within. No other pixels are considered.
- For bilinear interpolation, the output pixel value is a weighted average of pixels in the nearest 2-by-2 neighborhood.
- For bicubic interpolation, the output pixel value is a weighted average of pixels in the nearest 4-by-4 neighborhood.

The number of pixels considered affects the complexity of the computation. Therefore the bilinear method takes longer than nearest neighbor interpolation, and the bicubic method takes longer than bilinear. However, the greater the number of pixels considered, the more accurate the computation is, so there is a trade-off between processing time and quality.

## Image Types

The functions that use interpolation take an argument that specifies the interpolation method. F or these functions, the default method is nearest neighbor interpolation. This method produces acceptable results for all image types, and is the only method that is appropriate for indexed images. For intensity and RGB images, however, you should generally specify bilinear or bicubic interpolation, because these methods produce better results than nearest neighbor interpolation.
For RGB images, interpolation is performed on the red, green, and blue image planes individually.

F or binary images, interpolation has effects that you should be aware of. If you use bilinear or bicubic interpolation, the computed values for the pixels in the output image will not all be 0 or 1 . The effect on the resulting output image depends on the class of the input image.

- If the class of the input image is doubl e, the output image is a grayscale image of class doubl e. The output image is not binary, because it includes values other than 0 and 1.
- If the class of the input image is ui nt 8 , the output image is a binary image of class ui nt 8 . The interpolated pixel values are rounded off to 0 and 1 so the output image can be of class ui nt 8 .

If you use nearest neighbor interpol ation, the result is al ways binary, because the values of the interpolated pixels are taken directly from pixels in the input image.

## Image Resizing

The tool box function i mresi ze changes the size of an image using a specified interpolation method. If you do not specify an interpolation method, the function uses nearest neighbor interpolation.

You can use i mresi ze to resize an image by a specific magnification factor. To enlarge an image, specify a factor greater than 1. For example, the command below doubles the number of pixels in $X$ in each direction.

```
Y = i mesize( X, 2)
```

To reduce an image, specify a number between 0 and 1 as the magnification factor.

You can also specify the actual size of the output image. The command below creates an output image of size 100-by-150.
$Y=i m e s i z e\left(X,\left[\begin{array}{ll}100 & 150]\end{array}\right)\right.$
If the specified size does not produce the same aspect ratio as the input image has, the output image will be distorted.

If you reduce the image size and use bilinear or bicubic interpolation, i mesi ze applies a low-pass filter to the image before interpolation. This reduces the effect of $M$ oi ré patterns, ripple patterns that result from aliasing during resampling. N ote, however, that even with low-pass filtering, the resizing operation can introduce artifacts, because information is always lost when you reduce the size of an image.
i mesi ze does not apply a low-pass filter if nearest neighbor interpolation is used, unless you explicitly specify the filter. This interpolation method is primarily used for indexed images, and low-pass filtering is not appropriate for these images.

For information about specifying a different filter, see the reference page for i mesize.

## Image Rotation

The im ot at e function rotates an image, using a specified interpolation method and rotation angle. If you do not specify an interpolation method, the function uses nearest neighbor interpolation.

You specify the rotation angle in degrees. If you specify a positive value, i mot at e rotates the image counterclockwise; if you specify a negative value, i m ot at e rotates the image clockwise.

For example, these commands rotate an image $35^{\circ}$ counterclockwise.

```
| = imead('ic.tif');
J = imotate(I, 35,' bilinear');
i mshow(1)
figure, imshow(J)
```



In order to include the entire original image, i m ot ate pads the outside with 0 's. This creates the black background in J and results in the output image being larger than the input image.
i mrot at e has an option for cropping the output image to the same size as the input image. See the reference page for i mot at e for more information.

## Image Cropping

The function i mr op extracts a rectangular portion of an image. You can specify the crop rectangle through input arguments, or select it with a mouse.

If you call i mer op without specifying the crop rectangle, the cursor changes to a cross hair when it is over the image. Click on one corner of the region you want to select, and while holding down the mouse button, drag across the image. i mor op draws a rectangle around the area you are selecting. When you release the mouse button, i mer op creates a new image from the selected region.

In this example, you display an image and call i mer op. Therectangle you select is shown in red.
inshow ic.tif
l = imerop;


Now display the cropped image.
i mshow (I)


If you do not provide any output arguments, i mer op displays the image in a new figure.

## Neighborhood and Block Operations

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## Overview

Certain image processing operations involve processing an image in sections called blocks, rather than processing the entire image at once.
The Image Processing Tool box provides several functions for specific operations that work with blocks, for example, the di I ate function for binary image dilation. In addition, the tool box provides more generic functions for processing an image in blocks. This chapter discusses these generic block processing functions.
To use one of the functions described in this chapter, you supply information about the size of the blocks, and specify a separate function to use to process the blocks. The block processing function does the work of breaking the input image into blocks, calling the specified function for each block, and reassembling the results into an output image.

## Words You Need to Know

An understanding of the following terms will help you to use this chapter. For more explanation of this tableand others likeit, see "Words You Need to Know" in the Preface.

| Words | Definitions |
| :--- | :--- |
| Block operation | An operation in which an image is processed in blocks rather than <br> all at once. The blocks have the same size across the image. Some <br> operation is applied to one block at a time. The blocks are <br> reassembled to form an output image. |
| Border padding | Additional rows and columns temporarily added to the border(s) of <br> an image when some of the blocks extend outside the image. The <br> additional rows and columns normally contain zeros. |
| Center pixel | The pixel at the center of a neighborhood. |
| Column processing | An operation in which neighborhoods are reshaped into columns <br> before processing in order to speed up computation time. |
| Distinct block operation | A block operation in which the blocks do not overlap. |


| Words | Definitions |
| :--- | :--- |
| Inline function | A user-defined function created using the MATLAB function <br> i nl i ne. Tool box functions whose syntax includes a parameter called <br> FUN can take an inline function as an argument. |
| Neighborhood operation | An operation in which each output pixel is computed from a set of <br> neighboring input pixels. Convolution, dilation, and median <br> filtering are examples of neighborhood operations. A neighborhood <br> operation can also be called a sliding neighborhood operation. |
| Overlap | Extra rows and columns of pixels outside a block whose values are <br> taken into account when processing the block. These extra pixels <br> cause distinct blocks to overlap one another. The bl kproc function <br> enables you to specify an overlap. |

## Types of Block Processing Operations

Using these functions, you can perform various block processing operations, including sliding neighborhood operations and distinct bl ock operations.

- In a sliding neighborhood operation, the input image is processed in a pixel wise fashion. That is, for each pixel in the input image, some operation is performed to determine the value of the corresponding pixel in the output image. The operation is based on the values of a block of neighboring pixels.
- In a distinct block operation, the input image is processed a block at a time. That is, the image is divided into rectangular blocks, and some operation is performed on each block individually to determine the values of the pixels in the corresponding block of the output image.

In addition, the tool box provides functions for column processing operations. These operations are not actually distinct from block operations; instead, they are a way of speeding up block operations by rearranging blocks into matrix columns.

Notethat even if you do not usethe block processing functions described in this chapter, the information here may be useful to you, as it includes concepts fundamental to many areas of image processing. In particular, the discussion of sliding neighborhood operations is applicable to linear filtering and binary morphological operations. See Chapter 6, "Linear Filtering and Filter Design"
and Chapter 9, "Binary Image Operations" for information about these applications.

## Sliding Neighborhood Operations

A sliding neighborhood operation is an operation that is performed a pixel at a time, with the value of any given pixel in the output image being determined by applying some algorithm to the values of the corresponding input pixel's neighborhood. A pixel's neighborhood is some set of pixels, defined by their locations relative to that pixel, which is called the center pixel. The neighborhood is a rectangular block, and as you move from one element to the next in an image matrix, the neighborhood block slides in the same direction.

Figure 5-1 shows the neighborhood blocks for some of the elements in a 6-by-5 matrix with 2 -by- 3 sliding blocks. The center pixel for each neighborhood is marked with a dot.


Figure 5-1: 2-by-3 Sliding Blocks for Sliding Neighborhood Operations
The center pixel is the actual pixel in the input image being processed by the operation. If the neighborhood has an odd number of rows and columns, the center pixel is actually in the center of the neighborhood. If one of the dimensions has even length, the center pixel is just to the left of center or just above center. For example, in a 2-by-2 neighborhood, the center pixel is the upper left one.

For any mby-n neighborhood, the center pixel is
floor (([mn]+1)/2)
In the 2-by-3 block shown in Figure 5-1, the center pixel is (1,2), or, the pixel in the second column of the top row of the neighborhood.

To perform a sliding neighborhood operation
1 Select a single pixel.
2 Determine the pixel's neighborhood.
3 Apply a function to the values of the pixels in the neighborhood. This function must return a scalar.

4 Find the pixel in the output image whose position corresponds to that of the center pixel in the input image. Set this output pixel to the value returned by the function.

5 Repeat steps 1 through 4 for each pixel in the input image.
For example, suppose Figure 5-1 represents an averaging operation. The function might sum the values of the six neighborhood pixels and then divide by 6 . The result is the value of the output pixel.

## Padding of Borders

As Figure 5-1 shows, some of the pixels in a neighborhood may be missing, especially if the center pixel is on the border of the image. Notice that in the figure, the upper left and bottom right neighborhoods include "pixels" that are not part of the image.

To process these neighborhoods, sliding neighborhood operations pad the borders of the image, usually with 0's. In other words, these functions process the border pixels by assuming that the image is surrounded by additional rows and col umns of O's. These rows and columns do not become part of the output image and are used only as parts of the neighborhoods of the actual pixels in the image.

## Linear and Nonlinear Filtering

You can use sliding neighborhood operations to implement many kinds of filtering operations. One example of a sliding neighbor operation is convol ution, which is used to implement linear filtering. MATLAB provides the conv and filter 2 functions for performing convolution. SeeChapter 6, "Linear Filtering and Filter Design" for more information about these functions.

In addition to convolution, there are many other filtering operations you can implement through sliding neighborhoods. Many of these operations are nonlinear in nature. F or example, you can implement a sliding neighborhood operation where the value of an output pixel is equal to the standard deviation of the values of the pixels in the input pixel's neighborhood.

You can use thenlfilter function to implement a variety of sliding neighborhood operations. nl filter takes as input arguments an image, a neighborhood size, and a function that returns a scalar, and returns an image of the same size as the input image. The value of each pixel in the output image is computed by passing the corresponding input pixel's neighborhood to the function. F or example, this call computes each output pixel by taking the standard deviation of the values of the input pixel's 3-by-3 neighborhood (that is, the pixel itself and its eight contiguous neighbors).

```
I2 = nlfilter(I,[3 3],'std2');
```

You can write an M-file to implement a specific function, and then use this function with nl filter. For example, this command processes the matrixI in 2-by-3 neighborhoods with a function called myf un. m

```
nlfilter(l,[2 3],'myfun');
```

You can also use an inline function; in this case, the function name appears in thenlfilter call without quotation marks. For example,

```
f = inline('sqrt(min(x(:)))');
|2 = nlfilter(l,[2 2],f);
```

The example below uses nl filter to set each pixel to the maximum value in its 3-by-3 neighborhood.

```
| = imead('tire.tif');
f = inline('max(x(:))');
I2 = nlfilter(I,[3 3],f);
i nshow(1);
fi gure, i mshow(l2);
```



Figure 5-2: Each Output Pixel Set to Maximum Input Neighborhood Value
Many operations that nl filter can implement run much faster if the computations are performed on matrix columns rather than rectangular neighborhoods. F or information about this approach, seethe reference page for colfilt.

Note nl filter is an example of a "function function." For more information on how to use this kind of function, see Appendix A. For more information on inline functions, see i nl i ne in the MATLAB Function Reference.

## Distinct Block Operations

Distinct blocks are rectangular partitions that divide a matrix into mby-n sections. Distinct blocks overlay the image matrix starting in the upper-left corner, with no overlap. If the blocks don't fit exactly over the image, the tool box adds zero padding so that they do. Figure $5-3$ shows a 15 -by- 30 matrix divided into 4-by-8 blocks.


Figure 5-3: An Image Divided into Distinct Blocks
The zero padding process adds 0's to the bottom and right of the image matrix, as needed. After zero padding, the matrix is size 16-by-32.

The function bl kproc performs distinct block operations. bl kproc extracts each distinct block from an image and passes it to a function you specify. bl kproc assembles the returned blocks to create an output image.

For example, the command below processes the matrix I in 4-by-6 blocks with the function myf un.

```
|2 = bl kproc(I,[4 6],' myfun');
```

You can specify the function as an inline function; in this case, the function name appears in the bl kpr oc call without quotation marks. For example,

```
f = inl ine(' mean2(x)*ones(si ze(x))' );
I2 = bl kproc(I,[4 6],f);
```

The example bel ow uses bl kpr oc to set every pixel in each 8-by-8 block of an image matrix to the average of the elements in that block.

```
| = immead('tire.tif');
f = i nl i ne(' ui nt 8(round(mean2(x)*ones(si ze(x))))');
I2 = bl kproc(I,[8 8],f);
i nshow(1)
fi gure, inshow(12);
```



Notice that i nl i ne computes the mean of the block and then multiplies the result by a matrix of ones, so that the output block is the same size as the input block. As a result, the output image is the same size as the input image. bl kpr oc does not require that the images be the same size; however, if this is the result you want, you must make sure that the function you specify returns blocks of the appropriate size.

Note bl kproc is an example of a "function function." For more information on how to use this kind of function, see "Working with Function Functions" (Appendix A).

## Overlap

When you call bl kproc to define distinct blocks, you can specify that the blocks overlap each other, that is, you can specify extra rows and columns of pixels outside the block whose values are taken into account when processing the block. When there is an overlap, bl kpr oc passes the expanded block (including the overlap) to the specified function.

Figure 5-4 shows the overlap areas for some of the blocks in a 15-by-30 matrix with 1-by-2 overlaps. Each 4-by-8 block has a one-row overlap above and below, and a two-column overlap on each side. In the figure, shading indicates the overlap. The 4 -by- 8 blocks overlay the image matrix starting in the upper-left corner.


Figure 5-4: An Image Divided into Distinct Blocks With Specified Overlaps
To specify the overlap, you provide an additional input argument to bl kproc. To process the blocks in the figure above with the function myf un, the call is

```
B = bl kproc(A,[4 8],[ 1 2],' myfun')
```

Overlap often increases the amount of zero padding needed. For example, in Figure 5-3, the original 15-by-30 matrix became a 16-by-32 matrix with zero padding. When the 15-by-30 matrix includes a 1-by-2 overlap, the padded matrix becomes an 18-by- 36 matrix. The outermost rectangle in the figure delineates the new boundaries of the image after padding has been added to accommodate the overlap plus block processing. Noticethat in thefigureabove, padding has been added to the left and top of the original image, not just to the right and bottom.

## Column Processing

The tool box provides functions that you can use to process sliding neighborhoods or distinct blocks as columns. This approach is useful for operations that MATLAB performs columnwise; in many cases, column processing can reduce the execution time required to process an image.

F or example, suppose the operation you are performing involves computing the mean of each block. This computation is much faster if you first rearrange the blocks into columns, because you can compute the mean of every column with a single call to the mean function, rather than calling mean for each block individually.

You can use the col filt function to implement column processing. This function

1 Reshapes each sliding or distinct block of an image matrix into a column in a temporary matrix

2 Passes the temporary matrix to a function you specify
3 Rearranges the resulting matrix back into the original shape

## Sliding Neighborhoods

For a sliding neighborhood operation, col filt creates a temporary matrix that has a separate column for each pixel in the original image. The column corresponding to a given pixel contains the values of that pixel's neighborhood from the original image.

Figure 5-5 illustrates this process. In this figure, a 6-by-5 image matrix is processed in 2-by-3 neighborhoods. col filt creates one column for each pixel in the image, so there are a total of 30 columns in the temporary matrix. E ach pixel's column contains the value of the pixels in its neighborhood, so there are six rows. colfilt zero pads the input image as necessary. For example, the neighborhood of the upper left pixel in the figure has two zero-valued neighbors, due to zero padding.


Figure 5-5: colfilt Creates a Temporary Matrix for Sliding Neighborhood
Thetemporary matrix is passed to a function, which must return a single value for each column. (Many MATLAB functions work this way, for example, mean, medi an, st d, sum etc.) The resulting values are then assigned to the appropriate pixels in the output image.
colfilt can produce the sameresults as nlfilter with faster execution time; however, it may use more memory. The example below sets each output pixel to the maximum value in the input pixel's neighborhood, producing the same result as the nl fil ter example shown in Figure 5-2. Notice that the function is $\max (x)$ rather than $\max (x(:))$, because each neighborhood in the original image is a separate column in the temporary matrix.

```
f = inline('max(x)');
I2 = colfilt(I,[3 3],'sliding',f);
```


## Distinct Blocks

For a distinct block operation, col filt creates a temporary matrix by rearranging each block in the image into a column. col filt pads the original image with 0's, if necessary, before creating the temporary matrix.

Figure 5-6 illustrates this process. In this figure, a 6-by-16 image matrix is processed in 4-by-6 blocks. col filt first zero pads the image to make the size

8-by-18 (six 4-by-6 blocks), and then rearranges the blocks into 6 columns of 24 elements each.


Figure 5-6: colfilt Creates a Temporary Matrix for Distinct Block Operation
After rearranging the image into a temporary matrix, col filt passes this matrix to the function. The function must return a matrix of the same size as the temporary matrix. If the block size is mby-n, and the image is mmby-nn, the size of the temporary matrix is ( $n * n$ ) -by-(ceil $(m \times n) *$ cei $I(n n / n)$ ). After the function processes the temporary matrix, the output is rearranged back into the shape of the original image matrix.

This example sets all the pixels in each 8 -by-8 block of an image to the mean pixel value for the block, producing the same result as the bl kpr oc example in "Distinct Block Operations" on page 5-9.

$$
1=i m 2 d o u b l e(i m e a d(' t i r e . t i f ')) ;
$$

```
f = i nl i ne(' ones(64, 1) *mean(x)' );
I2 = colfilt(I,[8 8],'di stinct',f);
```

Notice that the inline function computes the mean of the block and then multiplies the result by a vector of ones, so that the output block is the same size as the input block. As a result, the output image is the same size as the input image.

## Restrictions

You can usecol filt to implement many of the same distinct block operations that bl kproc performs. However, col filt has certain restrictions that bl kproc does not.

- The output image must be the same size as the input image.
- The blocks cannot overlap.

For situations that do not satisfy these constraints, use bl kproc.

## Linear Filtering and Filter Design

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## Overview

The I mage Processing Tool box provides a number of functions for designing and implementing two-dimensional linear filters for image data. This chapter describes these functions and how to use them effectively.

The material in this chapter is divided into two parts:

- The first part is an explanation of linear filtering and how it is implemented in the tool box. This topic describes filtering in terms of the spatial domain, and is accessible to anyone doing image processing.
- The second part is a discussion about designing two-dimensional finite infinite response (FIR) filters. This section assumes you are familiar with working in the frequency domain.


## Words You Need to Know

An understanding of the following terms will help you to use this chapter. For more explanation of this table and others likeit, see "Words Y ou Need to K now" in the Preface. N ote that this tableincludes brief definitions of terms related to filter design; a detailed discussion of these terms and the theory behind filter design is outside the scope of this User Guide.

| Words | Definitions |
| :--- | :--- |
| Computational molecule | A filter matrix used to perform correlation. The filter design <br> functions in the Image Processing Tool box return computational <br> molecules. A computational mol ecule is a convolution kernel that <br> has been rotated 180 degrees. |
| Convolution | A neighborhood operation in which each output pixel is a weighted <br> sum of neighboring input pixels. The weights are defined by the <br> convolution kernel. Image processing operations implemented with <br> convolution include smoothing, sharpening, and edge enhancement. |
| Convolution kernel | A filter matrix used to perform convol ution. A convol ution kernel is <br> a computational molecule that has been rotated 180 degrees. |


| Words | Definitions |
| :--- | :--- |
| Correlation | A neighborhood operation in which each output pixel is a weighted <br> sum of neighboring input pixels. The weights are defined by the <br> computational molecule. Image processing operations implemented <br> with convolution include smoothing, sharpening, and edge <br> enhancement. Correlation is closely related mathematically to <br> convolution. |
| FIR filter | A filter whose response to a single point, or impulse, has finite <br> extent. FIR stands for finite impulse response. An FIR filter can be <br> implemented using convolution. All filter design functions in the <br> Image Processing Tool box return FIR filters. |
| Frequency response | A mathematical function describing the gain of a filter in response <br> to different input frequencies. |
| Reighborhood operation | An operation in which each output pixel is computed from a set of <br> neighboring input pixels. Convolution, dilation, and median <br> filtering are examples of neighborhood operations. |
| Separable filter | Oscillations around a constant value. The frequency response of a <br> practical filter often has ripples where the frequency response of an <br> ideal filter is flat. |
| A two-dimensional filter that can be implemented by a sequence of <br> two one-dimensional filters. Separable filters can be implemented <br> much faster than nonseparable filters. The function fi I ter 2 checks <br> a filter for separability before applying it to an image. |  |
| Window method | A filter design method that multiples the ideal impulse response by <br> a window function, which tapers the ideal impulse response. The <br> resulting filter's frequency response approximates a desired <br> frequency response. |

## Linear Filtering

Filtering is a technique for modifying or enhancing an image. For example, you can filter an image to emphasize certain features or remove other features.

Filtering is a neighborhood operation, in which the value of any given pixel in the output image is determined by applying some al gorithm to the values of the pixels in the neighborhood of the corresponding input pixel. A pixel's neighborhood is some set of pixels, defined by their locations relative to that pixel. (See Chapter 5, "Neighborhood and Block Operations", for a general discussion of neighborhood operations.)

Linear filtering is filtering in which the value of an output pixel is a linear combination of the values of the pixels in the input pixel's neighborhood. For example, an algorithm that computes a weighted average of the neighborhood pixels is one type of linear filtering operation.

This section discusses linear filtering in MATLAB and the I mage Processing Tool box. It includes

- A description of how MATLAB performs linear filtering, using convolution
- A discussion about using predefined filter types

See "Filter Design" on page 6-14 for information about how to design filters.

## Convolution

In MATLAB, linear filtering of images is implemented through two-dimensional convolution. In convolution, the value of an output pixel is computed by multiplying elements of two matrices and summing the results. One of these matrices represents the image itself, while the other matrix is the filter. F or example, a filter might be

$$
k=\left[\begin{array}{rrl}
4 & -3 & 1 \\
4 & 6 & 2
\end{array}\right]
$$

This filter representation is known as a convol ution kerned. The MATLAB function conv2 implements image filtering by applying your convolution kernel to an image matrix. conv2 takes as arguments an input image and a filter, and returns an output image. For example, in this call, k is the convolution kernel, $A$ is the input image, and $B$ is the output image.

$$
B=\operatorname{conv} 2(A, k) ;
$$

conv2 produces the output image by performing these steps:
1 Rotate the convolution kernel 180 degrees to produce a computational molecule.

2 Determine the center pixel of the computational molecule.
3 Apply the computational molecule to each pixel in the input image.
Each of these steps is explained below.

## Rotating the Convolution Kernel

In two-dimensional convolution, the computations are performed using a computational molecule This is simply the convolution kernel rotated 180 degrees, as in this call.

$$
\begin{aligned}
& \mathrm{h}=\mathrm{rot} 90(\mathrm{k}, 2) ; \\
& \mathrm{h}=
\end{aligned}
$$

$$
2 \quad 6 \quad 4
$$

$$
1-3 \quad 4
$$

## Determining the Center Pixel

Toapply the computational molecule, you must first determinethe center pixel. The center pixel is defined as f oor ( ( si ze( h$)+1$ ) / 2 ). For example, in a 5 -by-5 molecule, the center pixel is $(3,3)$. The moleculeh shown above is 2 -by- 3 , so the center pixel is $(1,2)$.

## Applying the Computational Molecule

The value of any given pixel in B is determined by applying the computational molecule $h$ to the corresponding pixel in A. Y ou can visualize this by overlaying $h$ on A, with the center pixel of $h$ over the pixel of interest in A. Y ou then multiply each element of $h$ by the corresponding pixel in $A$, and sum the results.

F or example, to determine the value of the pixel $(4,6)$ in B, overlay h on A, with the center pixel of $h$ covering the pixel $(4,6)$ in $A$. The center pixel is circled in Figure 6-1.


Figure 6-1: Overlaying the Computational Molecule for Convolution
Now, look at the six pixels covered by h. F or each of these pixels, multiply the value of the pixel by the value in $h$. Sum the results, and place this sum in $B(4,6)$.

$$
B(4,6)=2^{*} 2+3^{*} 6+3^{*} 4+3^{*} 1+2^{*}-3+0 * 4=31
$$

Perform this procedure for each pixel in A to determine the value of each corresponding pixel in B.

## Padding of Borders

When you apply a filter to pixels on the borders of an image, some of the elements of the computational molecule may not overlap actual image pixels. For example, if the molecule is 3-by-3 and you are computing the result for a pixel on the top row of the image, some of the elements of the molecule are outside the border of the image.

Figure 6-2 illustrates a 3-by-3 computational molecule being applied to the pixel $(1,3)$ of a 5 -by- 5 matrix. The center pixel is indicated by a filled circle.


Figure 6-2: Computational Molecule Overhanging Top Row of Image
In order to compute output values for the border pixels, conv2 pads the image matrix with zeroes. In other words, the output values are computed by assuming that the input image is surrounded by additional rows and columns of zeroes. In the figure shown above, the elements in the top row of the computational molecule are assumed to overlap zeroes.
Depending on what you are trying to accomplish, you may want to discard output pixels whose values depend on zero padding. To indicate what portion of the convolution to return, conv2 takes a third input argument, called the shape parameter, whose value is one of these three strings.

- ' val i d' - returns only the pixels whose values can be computed without using zero padding of the input image. Theresulting output image is smaller than the input image. In this example, the output image is 3-by-3.
- ' same' - returns the set of pixels that can be computed by applying the filter to all pixels that are actually part of the input image. Border pixels are computed using zero padding, but the center pixel of the computational kernel is applied only to pixels in the image. This results in an output image that is the same size as the input image.
- ' full' - returns the full convolution. This means conv2 returns all pixels for which any of the pixels in the computational molecule overlap pixels in the image, even when the center pixel is outside the input image. The resulting output image is larger than the input image. In this example, the output image is 7-by-7.
conv2 returns the full convolution by default.
Figure 6-3 below illustrates applying a computational molecule to three different places in an image matrix.


Figure 6-3: Computation Molecule Applied to Different Areas at Edge
If you use the ful I option, then the order of the first two input arguments is interchangeable, because full convolution is commutative. In other words, it does not matter which matrix is considered the convolution kernel, because the result is the same in either case. If you use the val id or same option, the operation is not commutative, so the convolution kernel must be the second argument.

## The filter2 Function

In addition to the conv2 function, MATLAB also provides thef il ter 2 function for two-dimensional linear filtering. filt er 2 can produce the same results as conv2, and differs primarily in that it takes a computational molecule as an input argument, rather than a convolution kernel. (fil ter 2 operates by forming the convolution kernel from the computational molecule and then calling conv2.) The operation that filter 2 performs is called correlation.

If $k$ is a convolution kernel, $h$ is the corresponding computational molecule, and $A$ is an image matrix, the following calls produce identical results

```
    B = conv2(A, k,'sane' );
```

and

```
B = filter2(h, A,'same');
```

The functions in the Image Processing Tool box that produce filters (f speci al, f sampl e, etc.) all return computational molecules. Y ou can use these filters directly with filter 2 , or you can rotate them 180 degrees and call conv2.

## Separability

If a filter has separability, meaning that it can be separated into two one-dimensional filters (one column vector and one row vector), the computation speed for the filter can be greatly enhanced. Before calling conv2 to perform two-dimensional convolution, filter 2 first checks whether the filter is separable. If the filter is separable, filt er 2 uses singular value decomposition to find the two vectors. fil ter 2 then calls conv2 with this syntax.
conv2(A, kcol, krow) ;
where kcol and kr oware the column and row vectors that the two-dimensional convolution kernel k separates into (that is, $\mathrm{k}=\mathrm{kcol}{ }^{*} \mathrm{krow}$ ).
conv2 filters the columns with the column vector, and then, using the output of this operation, filters the rows using the row vector. The result is equivalent to two-dimensional convolution but is faster because it requires fewer computations.

## Determining Separability

A filter is separable if its rank is 1 . F or example, this filter is separable.

```
k =
    1 2 3
    2 4 6
    4 8 12
rank(k)
```

1

If $k$ is separable (that is, it has rank 1), then you can determine the corresponding column and row vectors with

```
[u,s,v] = svd(k);
kcol = u(:, 1) * sqrt(s(1))
kcol =
            0.9036
            1. }807
            3. }614
krow = conj(v(:, 1))' * sqrt(s(1))
krow =
```

1. 1067
2. 2134
3. 3200

Perform array multiplication on the separated vectors to verify your results.

```
kcol * krow
ans =
\begin{tabular}{rrr} 
1. 0000 & 2.0000 & 3.0000 \\
2. 0000 & 4.0000 & 6.0000
\end{tabular}
```


## Higher-Dimensional Convolution

To perform two-dimensional convolution, you useconv2 or filter 2. To perform higher-dimensional convolution, you use the convn function. convn takes as arguments a data array and a convol ution kernel, both of which can be of any dimension, and returns an array whose dimension is the higher of the two input arrays' dimensions. convn also takes a shape parameter argument that accepts the same values as in conv2 and filter 2 , and which has analogous effects in higher dimensions.

One important application for the convn function is to filter image arrays that have multiple planes or frames. F or example, suppose you have an array A containing five RGB images that you want to filter using a two-dimensional convolution kernel $k$. The image array is a four-dimensional array of size mby-n-by-3-by-5. To filter this array with conv2, you would need to call the function 15 times, once for each combination of planes and frames, and assemble the results into a four-dimensional array. Using convn, you can filter the array in a single call.

$$
B=\operatorname{convn}(A, k) ;
$$

For more information, see convn in the MATLAB Function Reference

## Using Predefined Filter Types

Thefunction fspeci al produces several kinds of predefined filters, in the form of computational molecules. After creating a filter with f speci al , you can apply it directly to your image data using filter 2, or you can rotate it 180 degrees and use conv2 or convn.
One simplefilter fspeci al can produce is an averaging filter. This type of filter computes the value of an output pixel by simply averaging the values of its neighboring pixels.
The default size of the averaging filter f speci al creates is 3 -by-3, but you can specify a different size. The value of each element is $1 / I$ engt $h(h(:))$. For example, a 5 -by- 5 averaging filter would be

| 0.0400 | 0.0400 | 0.0400 | 0.0400 | 0.0400 |
| :--- | :--- | :--- | :--- | :--- |
| 0.0400 | 0.0400 | 0.0400 | 0.0400 | 0.0400 |
| 0.0400 | 0.0400 | 0.0400 | 0.0400 | 0.0400 |
| 0.0400 | 0.0400 | 0.0400 | 0.0400 | 0.0400 |
| 0.0400 | 0.0400 | 0.0400 | 0.0400 | 0.0400 |

Applying this filter to a pixel is equivalent to adding up the values of that pixel's 5-by-5 neighborhood and dividing by 25 . This has the effect of smoothing out local highlights and blurring edges in an image.

This example illustrates applying a 5-by-5 averaging filter to an intensity image.

```
| = i mmead(' bl ood1.tif');
h = fspeci al('average',5);
```

```
l2 = ui nt8(round(filter2(h,l)));
i mshow l)
figure, i nshow(l 2)
```



Figure 6-4: Blood.tif (left) and Blood.tif After Averaging Filter Applied (right)
Note that the output from filter 2 (and conv2 and convn) is always of class doubl e. In the example above, the input image is of class ui nt 8, so the output from filter 2 consists of double-precision values in the range [0,255]. The call to the ui nt 8 function converts the output to ui nt 8; the data is not in the proper range for an image of class doubl e.

Another relatively simple filter f speci al can produce is a 3-by-3 Sobel filter, which is effective at detecting the horizontal edges of objects in an image.

```
h = fspecial('sobel')
\(\mathrm{h}=\)
\(1 \quad 2 \quad 1\)
\(0 \quad 0 \quad 0\)
\(-1 \quad-2 \quad-1\)
```

Unlike an averaging filter, the Sobel filter produces values outside the range of the input data. F or example, if the input image is of class doubl e, the output array may include values outside the range [0,1]. To display the output as an image, you can use i nshow and specify the data range, or you can use the mat 2 gr ay function to convert the values to the range $[0,1]$.

Note that if the input image is of class ui nt 8 or ui nt 16, you should not simply convert the output array to the same class as the input image, because the output may contain values outside the range that the class can represent. For example, if the input image is of class ui nt 8 , the output may include values that cannot be represented as 8 -bit integers. Y ou can, however, rescale the output and then convert it. For example,

```
h = fspeci al('sobel');
I2 = filter 2(h,l);
J = ui nt 8(round(nat2gray(I2)*255));
```

You can also use ins howto display the output array without first rescaling the data. The following example creates a Sobel filter and uses fil t er 2 to apply the filter to the bl ood1 image. Notice that in the call to inshow, the intensity range is specified as an empty matrix ([ ] ). This instructs ins howto display the minimum value in 12 as black, the maximum value as white, and values in between as intermediate shades of gray, thus enabling you to display the filter 2 output without converting or rescaling it.

```
| = immead(' bl oodl.tif');
h = fspecial('sobel');
I2 = filter 2(h,l);
i mshow(1 2,[])
```



Figure 6-5: Blood.tif with Sobel Filter Applied
For a description of all the filter types fspeci al provides, see the reference page for f speci al.

## Filter Design

This section describes working in thefrequency domain to design filters. Topics discussed include:

- Finiteimpulseresponse(FIR) filters, the class of linear filter that thetool box supports
- The frequency transformation method, which transforms a one-dimensional FIR filter into a two-dimensional FIR filter
- The frequency sampling method, which creates a filter based on a desired frequency response
- The windowing method, which multiplies the ideal impulse response with a window function to generate the filter
- Creating the desired frequency response matrix
- Computing the frequency response of a filter

This section assumes you are familiar with working in the frequency domain. This topic is discussed in many signal processing and image processing textbooks.


#### Abstract

Note Most of the design methods described in this section work by creating a two-dimensional filter from a one-dimensional filter or window created using functions from the Signal Processing Tool box. Although this tool box is not required, you may find it difficult to design filters in the I mage Processing Toolbox if you do not have the Signal Processing Tool box as well.


## FIR Filters

The Image Processing Tool box supports one class of linear filter, the two-dimensional finite impulse response (FIR) filter. FIR filters have several characteristics that make them ideal for image processing in the MATLAB environment.

- FIR filters are easy to represent as matrices of coefficients.
- Two-dimensional FIR filters are natural extensions of one-dimensional FIR filters.
- There are several well-known, reliable methods for FIR filter design.
- FIR filters are easy to implement.
- FIR filters can be designed to have linear phase, which helps prevent distortion.

Another class of filter, the infinite impulse response (IIR) filter, is not as suitable for image processing applications. It lacks the inherent stability and ease of design and implementation of the FIR filter. Therefore, this tool box does not provide IIR filter support.

## Frequency Transformation Method

The frequency transformation method transforms a one-dimensional FIR filter into a two-dimensional FIR filter. The frequency transformation method preserves most of the characteristics of the one-dimensional filter, particularly the transition bandwidth and ripple characteristics. This method uses a transformation matrix, a set of elements that defines the frequency transformation.

The tool box function ftrans 2 implements the frequency transformation method. This function's default transformation matrix produces filters with nearly circular symmetry. By defining your own transformation matrix, you can obtain different symmetries. (Seej aeS. Lim, Two-Dimensional Signal and Image Processing, 1990, for details.)

The frequency transformation method generally produces very good results, as it is easier to design a one-dimensional filter with particular characteristics than a corresponding two-dimensional filter. F or instance, the next example designs an optimal equiripple one-dimensional FIR filter and uses it to create a two-dimensional filter with similar characteristics. The shape of the one-dimensional frequency response is clearly evident in the two-dimensional response.

```
b = renez(10,[0 0.4 0.6 1],[1 1 0 0]);
h = ftrans2(b);
[H,w] = freqz(b, 1, 64,' whol e' );
col orm@p(j et (64) )
pl ot(w pi-1,fftshift(abs(H) ))
figure, freqz2(h,[32 32])
```




Figure 6－6：A One－Dimensional Frequency Response（left）and the Corresponding Tw o－Dimensional Frequency Response（right）

## Frequency Sampling Method

The frequency sampling method creates a filter based on a desired frequency response．Given a matrix of points that defines the shape of the frequency response，this method creates a filter whose frequency response passes through those points．Frequency sampling places no constraints on the behavior of the frequency response between the given points；usually，the response ripples in these areas．

The tool box function f samp2 implements frequency sampling design for two－dimensional FIR filters．f samp2 returns a filter h with a frequency response that passes through the points in the input matrix Hd．The example below creates an 11－by－11 filter using f samp2，and plots the frequency response of the resulting filter．（The freqz2 function in this example calculates the two－dimensional frequency response of a filter．See＂Computing the F requency Response of a Filter＂on page 6－19 for more information．）

```
Hd = zeros(11,11); Hd(4:8,4:8) = 1;
[f1,f2] = freqspace( 11,' meshgrid');
mesh(f1,f2,Hd), axi s([-1 1-1 1 0 1. 2]), col orm⿴囗十(jet(64))
h = fsamp2(Hd);
figure, freqz2(h,[32 32]), axi s([-1 1 -1 1 0 1. 2])
```



Figure 6-7: Desired Two-Dimensional Frequency Response (left) and Actual Two-Dimensional Frequency Response (right)

Notice the ripples in the actual frequency response, compared to the desired frequency response. These ripples are a fundamental problem with the frequency sampling design method. They occur wherever there are sharp transitions in the desired response.

You can reduce the spatial extent of the ripples by using a larger filter. However, a larger filter does not reduce the height of the ripples, and requires more computation time for filtering. To achieve a smoother approximation to the desired frequency response, consider using the frequency transformation method or the windowing method.

## Windowing Method

The windowing method involves multiplying the ideal impulse response with a window function to generate a corresponding filter. Like the frequency sampling method, the windowing method produces a filter whose frequency response approximates a desired frequency response. The windowing method, however, tends to produce better results than the frequency sampling method.

The tool box provides two functions for window-based filter design, f wi nd1 and f wi nd2. f wi nd1 designs a two-dimensional filter by using a two-dimensional window that it creates from one or two one-dimensional windows that you specify. f wi nd2 designs a two-dimensional filter by using a specified two-dimensional window directly.
f wi nd1 supports two different methods for making the two-dimensional windows it uses:

- Transforming a single one-dimensional window to create a two-dimensional window that is nearly circularly symmetric, by using a process similar to rotation
- Creating a rectangular, separable window from two one-dimensional windows, by computing their outer product

The example bel ow uses f wi nd1 to create an 11-by-11 filter from the desired frequency response Hd. Here, the hammi ng function from the Signal Processing Tool box is used to create a one-dimensional window, which f wi nd1 then extends to a two-dimensional window.

```
Hd = zeros(11,11); Hd(4:8,4: 8) = 1;
[f1,f2] = freqspace( 11,' meshgrid');
mesh(f1,f2,Hd), axi s([-1 1-1 1 0 1. 2]), col orm@p(jet(64))
h = fwi ndl(Hd, hamming(11));
figure, freqz2(h,[32 32]), axis([-1 1-1 1 0 1. 2])
```



Figure 6-8: Desired Two-Dimensional Frequency Response (left) and Actual Two-Dimensional Frequency Response (right)

## Creating the Desired Frequency Response Matrix

The filter design functions f samp2, f wi nd2, and f wi nd2 all create filters based on a desired frequency response magnitude matrix. You can create an appropriate desired frequency response matrix using the $f r$ reqs pace function.
freqspace returns correct, evenly spaced frequency values for any size response. If you create a desired frequency response matrix using frequency points other than those returned by freqspace, you may get unexpected results, such as nonlinear phase.
For example, to create a circular ideal lowpass frequency response with cutoff at 0.5 use:

```
[f1,f2] = freqspace( 25,' meshgrid');
Hd = zeros(25, 25); d = sqrt(f1.^2 + f2. ^2) < 0.5;
Hd(d) = 1;
mesh(f 1, f 2, Hd)
```



Figure 6-9: Ideal Circular Low pass Frequency Response
N ote that for this frequency response, the filters produced by f samp2, f wi nd1, and $f$ wi nd2 are real. This result is desirable for most image processing applications. To achievethis in general, the desired frequency response should be symmetric about the frequency origin ( $\mathrm{f} 1=0, \mathrm{f} 2=0$ ).

## Computing the Frequency Response of a Filter

The freqz2 function computes the frequency response for a two-dimensional filter. With no output arguments, freqz2 creates a mesh plot of the frequency response. F or example, consider this FIR filter:
$h=0.1667$
0. 6667
0. 1667
0. 6667

- 3. 3333

0. 6667
1. 1667
2. 6667
3. 1667];

This command computes and displays the64-by-64 point frequency response of h:
freqz2(h)


Figure 6-10: The Frequency Response of a Tw o-Dimensional Filter
To obtain the frequency response matrix H and the frequency point vectors f 1 and f 2 , use output arguments:
[ $\mathrm{H}, \mathrm{f} 1, \mathrm{f} 2$ ] $=\mathrm{freqz2(h);}$
freqz2 normalizes the frequencies f 1 and f 2 so that the value 1.0 corresponds to half the sampling frequency, or $\pi$ radians.

For a simple mby-n response, as shown above, freqz 2 uses the two-dimensional fast Fourier transform function fft 2 . You can also specify vectors of arbitrary frequency points, but in this case freqz2 uses a slower algorithm.

See "F ourier Transform" on page 7-4 for more information about the fast Fourier transform and its application to linear filtering and filter design.

## Transforms

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## Overview

The usual mathematical representation of an image is a function of two spatial variables: $f(x, y)$. The value of the function at a particular location ( $x, y$ ) represents the intensity of the image at that point. The term transform refers to an alternative mathematical representation of an image.
For example, the F ourier transform is a representation of an image as a sum of complex exponentials of varying magnitudes, frequencies, and phases. This representation is useful in a broad range of applications, including (but not limited to) image analysis, restoration, and filtering.
The discrete cosine transform (DCT) also represents an image as a sum of sinusoids of varying magnitudes and frequencies. The DCT is extremely useful for image compression; it is the basis of the widely used J PEG image compression algorithm.

The Radon transform represents an image as a collection of projections along various directions. It is used in areas ranging from seismology to computer vision.

This chapter defines each of these transforms, describes related tool box functions, and shows examples of related image processing applications.

## Words You Need to Know

An understanding of the foll owing terms will help you to use this chapter. For more explanation of this tableand others likeit, see "Words Y ou Need to K now" in the Preface. Note that this table includes brief definitions of terms related to
transforms; a detailed discussion of these terms and the theory behind transforms is outside the scope of this User's Guide.

| Words | Definitions |
| :--- | :--- |
| Discrete transform | A transform whose input and output values are discrete samples, <br> making it convenient for computer manipulation. Discrete <br> transforms implemented by MATLAB and the I mage Processing <br> Tool box include the discrete Fourier transform (DFT) and the <br> discrete cosine transform (DCT). |
| Frequency domain | The domain in which an image is represented by a sum of periodic <br> signals with varying frequency. |
| Inverse transform | An operation that when performed on a transformed image, <br> produces the original image. |
| Spatial domain | The domain in which an image is represented by intensities at given <br> points in space. This is the most common representation for image <br> data. |
| Transform | An alternative mathematical representation of an image. For <br> example, the Fourier transform is a representation of an image as a <br> sum of complex exponentials of varying magnitudes, frequencies, <br> and phases. Transforms are useful for a wide range of purposes, <br> including convolution, enhancement, feature detection, and <br> compression. |

## Fourier Transform

The F ourier transform plays a critical role in a broad range of image processing applications, including enhancement, analysis, restoration, and compression. This section includes the following subsections:

- "Definition of Fourier Transform"
- "The Discrete Fourier Transform", including a discussion of fast Fourier transform
- "Applications" (sample applications using F ourier transforms)


## Definition of Fourier Transform

If $f(m, n)$ is a function of two discretespatial variables $m$ and $n$, then we define the two-dimensional Fourier transform of $f(m, n)$ by the relationship

$$
F\left(\omega_{1}, \omega_{2}\right)=\sum_{m=-\infty}^{\infty} \sum_{n=-\infty}^{\infty} f(m, n) e^{-j \omega_{1} m} e^{-j \omega_{2} n}
$$

The variables $\omega_{1}$ and $\omega_{2}$ are frequency variables; their units are radians per sample. $F\left(\omega_{1}, \omega_{2}\right)$ is often called the frequency-domain representation of $f(m, n) . F\left(\omega_{1}, \omega_{2}\right)$ is a complex-valued function that is periodic both in $\omega_{1}$ and $\omega_{2}$, with period $2 \pi$. Because of the periodicity, usually only the range $-\pi \leq \omega_{1}, \omega_{2} \leq \pi$ is displayed. Note that $F(0,0)$ is the sum of all the values of $f(m, n)$. For this reason, $F(0,0)$ is often called the constant component or DC component of the Fourier transform. (DC stands for direct current; it is an electrical engineering term that refers to a constant-voltage power source, as opposed to a power source whose voltage varies sinusoidally.)

The inverse two-dimensional Fourier transform is given by

$$
f(m, n)=\frac{1}{4 \pi^{2}} \int_{\omega_{1}=-\pi}^{\pi} \int_{\omega_{2}=-\pi}^{\pi} F\left(\omega_{1}, \omega_{2}\right) e^{j \omega_{1} m} e^{j \omega_{2} n} d \omega_{1} d \omega_{2}
$$

Roughly speaking, this equation means that $f(m, n)$ can be represented as a sum of an infinite number of complex exponentials (sinusoids) with different frequencies. The magnitude and phase of the contribution at the frequencies $\left(\omega_{1}, \omega_{2}\right)$ are given by $F\left(\omega_{1}, \omega_{2}\right)$.

## Example

Consider a function $f(m, n)$ that equals 1 within a rectangular region and 0 everywhere else.


Figure 7-1: A Rectangular Function
To simplify the diagram, $f(m, n)$ is shown as a continuous function, even though the variables $m$ and $n$ are discrete.

Figure 7-2 shows the magnitude of the Fourier transform, $\left|\mathrm{F}\left(\omega_{1}, \omega_{2}\right)\right|$, of Figure 7-1 as a mesh plot. The mesh plot of the magnitude is a common way to visualize the Fourier transform.


Figure 7-2: Magnitude Image of a Rectangular Function
The peak at the center of the plot is $F(0,0)$, which is the sum of all the values in $f(m, n)$. The plot also shows that $F\left(\omega_{1}, \omega_{2}\right)$ has more energy at high horizontal frequencies than at high vertical frequencies. This reflects the fact that horizontal cross sections of $f(m, n)$ are narrow pulses, while vertical cross sections are broad pulses. Narrow pulses have more high-frequency content than broad pulses.

Another common way to visualize the F ourier transform is to display $\log \left|F\left(\omega_{1}, \omega_{2}\right)\right|$ as an image, as in


Figure 7-3: The Log of the Fourier Transform of a Rectangular Function
Using the logarithm helps to bring out details of the F ourier transform in regions where $F\left(\omega_{1}, \omega_{2}\right)$ is very close to 0 .

Examples of the F ourier transform for other simple shapes are shown below.



Figure 7-4: Fourier Transforms of Some Simple Shapes

## The Discrete Fourier Transform

Working with the Fourier transform on a computer usually involves a form of the transform known as the discrete F ourier transform (DFT). There are two principal reasons for using this form:

- The input and output of the DFT are both discrete, which makes it convenient for computer manipulations.
- There is a fast algorithm for computing the DFT known as the fast Fourier transform (FFT).

The DFT is usually defined for a discrete function $f(m, n)$ that is nonzero only over the finite region $0 \leq \mathrm{m} \leq \mathrm{M}-1$ and $0 \leq \mathrm{n} \leq \mathrm{N}-1$. The two-dimensional M-by-N DFT and inverse M-by-N DFT relationships are given by

$$
\begin{array}{ll}
F(p, q)=\sum_{m=0}^{M-1} \sum_{n=0}^{N-1} f(m, n) e^{-j(2 \pi / M) p m} e^{-j(2 \pi / N) q n} & p=0,1, \ldots, M-1 \\
q=0,1, \ldots, N-1
\end{array}
$$

Thevalues $F(p, q)$ aretheDFT coefficients of $f(m, n)^{1}$. In particular, the value $F(0,0)$ is often called the DC coefficient. (Notethat matrix indices in MATLAB always start at 1 rather than 0 ; therefore, the matrix elements $f(1,1)$ and $F(1,1)$ correspond to the mathematical quantities $f(0,0)$ and $F(0,0)$, respectively.)

The MATLAB functions $f f t, f f t 2$, and $f f t n$ implement the fast F ourier transform algorithm for computing theone-dimensional DFT, two-dimensional DFT, and $N$-dimensional DFT, respectively. The functions ifft, ifft 2, and ifftn compute the inverse DFT.

[^3]
## Relationship to the Fourier Transform

The DFT coefficients $F(p, q)$ are samples of the Fourier transform $F\left(\omega_{1}, \omega_{2}\right)$.

$$
F(p, q)=\left.F\left(\omega_{1}, \omega_{2}\right)\right|_{\omega_{1}=2 \pi p / M} \quad \begin{array}{ll} 
& p=0,1, \ldots, M-1 \\
\omega_{2}=2 \pi q / N
\end{array} \quad q=0,1, \ldots, N-1
$$

## Example

Let's construct a matrix $f$ that is similar to the function $f(m, n)$ in the example in "Definition of Fourier Transform" on page 7-4. Remember that $f(m, n)$ is equal to 1 within the rectangular region and 0 elsewhere. We use a binary image to represent $f(m, n)$.

```
f = zeros(30, 30);
f( 5: 24, 13: 17) = 1;
i mshow(f,' not ruesize')
```



Compute and visualize the 30-by-30 DFT of $f$ with these commands

```
F = fft2(f);
F2 = Iog(abs(F));
i nshow F2,[-1 5],' notruesize' ); col ormap(j et); col orbar
```



Figure 7-5: A Discrete Fourier Transform Computed Without Padding
This plot differs from theF ourier transform displayed on Figure 7-3. First, the sampling of the F ourier transform is much coarser. Second, the zero-frequency coefficient is displayed in the upper-left corner instead of the traditional location in the center.

We can obtain a finer sampling of the F ourier transform by zero-padding f when computing its DFT. The zero-padding and DFT computation can be performed in a single step with this command:

$$
F=f f t 2(f, 256,256) ;
$$

This command zero-pads f to be 256 -by- 256 before computing the DFT.
i nshow log(abs(F)),[-1 5]); col ormp(jet); col orbar


Figure 7-6: A Discrete Fourier Transform Computed With Padding
The zero-frequency coefficient, however, is still displayed in the upper-left corner rather than the center. Y ou can fix this problem by using the function fft shi ft , which swaps the quadrants of $F$ so that the zero-frequency coefficient is in the center.

```
F = fft2(f, 256, 256);
F2 = fftshift(F);
i mshow(log(abs(F2)),[-1 5]); col ormap(j et); col orbar
```

The resulting plot is identical to the one on Figure 7-3.

## Applications

This section presents a few of the many image processing-related applications of the Fourier transform.

## Frequency Response of Linear Filters

The Fourier transform of the impulse response of a linear filter gives the frequency response of the filter. The function $f r e q z 2$ computes and displays a filter's frequency response. The frequency response of the Gaussian
convolution kernel shows that this filter passes low frequencies and attenuates high frequencies.


Figure 7-7: The Frequency Response of a Gaussian Filter
SeeChapter 6, "Linear Filtering and Filter Design" for more information about linear filtering, filter design, and frequency responses.

## Fast Convolution

A key property of the F ourier transform is that the multiplication of two Fourier transforms corresponds to the convolution of the associated spatial functions. This property, together with the fast Fourier transform, forms the basis for a fast convolution algorithm.

Suppose that $A$ is an $M$-by-N matrix and $B$ is a $P-b y-Q$ matrix. The convolution of $A$ and $B$ can be computed using the following steps:

1 Zero-pad $A$ and $B$ so that they are at least ( $M+P-1$ )-by-( $N+Q-1$ ). (Often $A$ and $B$ are zero-padded to a size that is a power of 2 becausefft 2 is fastest for these sizes.)

2 Compute the two-dimensional DFT of A and B using fft2.
3 Multiply the two DFTs together.
4 Usingifft2, compute the inverse two-dimensional DFT of the result from step 3.

For example,
$\mathrm{A}=$ magic (3);
B = ones(3);
$A(8,8)=0 ; \quad$ \% Zero-pad A to be 8-by-8
$B(8,8)=0 ; \quad$ \% Zero-pad B to be 8-by-8
$C=i f f t 2(f f t 2(A) . * f f t 2(B))$;
$C=C(1: 5,1: 5) ; \quad$ Extract the nonzero portion
$C=r e a l(C) \quad$ \% Remove imaginary part caused by roundof $f$ error
$C=$

| 8.0000 | 9.0000 | 15.0000 | 7.0000 | 6.0000 |
| ---: | ---: | ---: | ---: | ---: |
| 11.0000 | 17.0000 | 30.0000 | 19.0000 | 13.0000 |
| 15.0000 | 30.0000 | 45.0000 | 30.0000 | 15.0000 |
| 7.0000 | 21.0000 | 30.0000 | 23.0000 | 9.0000 |
| 4.0000 | 13.0000 | 15.0000 | 11.0000 | 2.0000 |

The FFT-based convolution method is most often used for large inputs. For small inputs it is generally faster to usefilter 2 or conv2.

## Locating Image Features

The F ourier transform can also be used to perform correlation, which is closely related to convolution. Correlation can be used to locate features within an image; in this context correlation is often called template matching.

For instance, suppose you want to locate occurrences of the letter "a" in an image containing text. This example reads in text . tif and creates a template image by extracting a letter " a " from it,

```
bw = imead('text.tif');
a=bw 59: 71, 81: 91); %Extract one of the I etters "a" fromthe i mage.
i mshow( bw);
figure, i nshow(a);
```


## Cross-Correlation Used <br> To Locate A Known <br> Target in an Image

Figure 7-8: An Image (left) and the Template to Correlate (right)
The correlation of the image of the letter " $a$ " with the larger image can be computed by first rotating the image of "a" by $180^{\circ}$ and then using the FFT-based convolution technique described above. (Note that convolution is equivalent to correlation if you rotate the convolution kernel by $180^{\circ}$.) To match the template to the image, you can use the fft 2 and ifft 2 functions,

```
C = real(ifft2(fft2(bw) .* fft2(rot 90(a, 2), 256, 256)));
figure, inshow(C,[])%ispl ay, scaling data to appropriate range.
max(C(:)) %%ind max pixel value in C.
ans =
51. 0000
thresh = 45; \%/se a threshol d that's a little less than max. figure, imshow C > thresh) \%®i spl ay showing pi xel s over threshol d.
```



Figure 7-9: A Correlated Image (left) and its Thresholded Result (right)

The left image above is the result of the correlation; bright peaks correspond to occurrences of the letter. The locations of these peaks are indicated by the white spots in the thresholded correlation image shown on the right.

Note that you could also have created the template image by zooming in on the image and using theinteractiveversion of i merop. For example, with text . tif displayed in the current figure window, enter

```
zoom on
a = imerop
```

To determine the coordinates of features in an image, you can use the pi xval function.

## Discrete Cosine Transform

The dct 2 function in the I mage Processing Toolbox computes the two-dimensional discretecosinetransform (DCT) of an image. TheDCT has the property that, for a typical image, most of the visually significant information about the image is concentrated in just a few coefficients of the DCT. F or this reason, the DCT is often used in image compression applications. F or example, the DCT is at the heart of the international standard lossy image compression al gorithm known as J PEG. (The name comes from the working group that devel oped the standard: the J oint Photographic Experts Group.)

The two-dimensional DCT of an M -by- N matrix A is defined as follows.

$$
\begin{aligned}
& \text { M-1 N-1 } \\
& B_{p q}=\alpha_{p} \alpha_{q} \sum_{m=0} \sum_{n=0} A_{m n} \cos \frac{\pi(2 m+1) p}{2 M} \cos \frac{\pi(2 n+1) q}{2 N}, \quad \begin{array}{l}
0 \leq p \leq M-1 \\
0 \leq q \leq N-1
\end{array} \\
& \alpha_{p}=\left\{\begin{array}{ll}
1 / \sqrt{M}, & p=0 \\
\sqrt{2 / M}, & 1 \leq p \leq M-1
\end{array} \quad \alpha_{q}= \begin{cases}1 / \sqrt{N}, & q=0 \\
\sqrt{2 / N}, & 1 \leq q \leq N-1\end{cases} \right.
\end{aligned}
$$

The values $\mathrm{B}_{\mathrm{pq}}$ are called the DCT coefficients of A . (Note that matrix indices in MATLAB always start at 1 rather than 0; therefore, the MATLAB matrix elements $A(1,1)$ and $B(1,1)$ correspond to the mathematical quantities $A_{00}$ and $B_{00}$, respectively.)
The DCT is an invertible transform, and its inverse is given by

$$
\begin{aligned}
& \text { M-1 N-1 } \\
& A_{m n}=\sum_{p=0} \sum_{q=0} \alpha_{p} \alpha_{q} B_{p q} \cos \frac{\pi(2 m+1) p}{2 M} \cos \frac{\pi(2 n+1) q}{2 N}, \quad \begin{array}{l}
0 \leq m \leq M-1 \\
0 \leq n \leq N-1
\end{array} \\
& \alpha_{p}=\left\{\begin{array}{ll}
1 / \sqrt{M}, & p=0 \\
\sqrt{2 / M}, & 1 \leq p \leq M-1
\end{array} \quad \alpha_{q}= \begin{cases}1 / \sqrt{N}, & q=0 \\
\sqrt{2 / N}, & 1 \leq q \leq N-1\end{cases} \right.
\end{aligned}
$$

The inverse DCT equation can be interpreted as meaning that any M-by-N matrix A can be written as a sum of $M N$ functions of the form

$$
\begin{array}{ll}
\alpha_{p} \alpha_{q} \cos \frac{\pi(2 m+1) p}{2 M} \cos \frac{\pi(2 n+1) q}{2 N}, & 0 \leq p \leq M-1 \\
0 \leq q \leq N-1
\end{array}
$$

These functions are called the basis functions of the DCT. The DCT coefficients $\mathrm{B}_{\mathrm{pq}}$, then, can be regarded as the weights applied to each basis function. For 8 -by-8 matrices, the 64 basis functions are illustrated by this image.


Figure 7-10: The 64 Basis Functions of an 8-by-8 Matrix
Horizontal frequencies increase from left to right, and vertical frequencies increase from top to bottom. The constant-valued basis function at the upper left is often called the DC basis function, and the corresponding DCT coefficient $B_{00}$ is often called the DC coefficient.

## The DCT Transform Matrix

The Image Processing Tool box offers two different ways to compute the DCT. The first method is to use thefunction dct 2. dct 2 uses an FFT-based algorithm for speedy computation with large inputs. The second method is to use theDCT transform matrix, which is returned by the function dct nt $x$ and may be more efficient for small square inputs, such as 8 -by- 8 or $16-b y-16$. The M-by-M transform matrix T is given by

$$
T_{p q}= \begin{cases}\frac{1}{\sqrt{M}} & p=0, \quad 0 \leq q \leq M-1 \\ \sqrt{\frac{2}{M}} \cos \frac{\pi(2 q+1) p}{2 M} & 1 \leq p \leq M-1, \quad 0 \leq q \leq M-1\end{cases}
$$

For an M-by-M matrix A, T*A is an M-by-M matrix whose columns contain the one-dimensional DCT of the columns of A. The two-dimensional DCT of A can be computed as $B=T^{*} A^{*} T^{\prime}$. Since $T$ is a real orthonormal matrix, its inverse is the same as its transpose. Therefore, the inverse two-dimensional DCT of B is given by $\mathrm{T}^{+}{ }^{*} \mathrm{~B}^{*} \mathrm{~T}$.

## The DCT and Image Compression

In the J PEG image compression algorithm, the input image is divided into 8 -by- 8 or 16-by-16 blocks, and the two-dimensional DCT is computed for each block. The DCT coefficients are then quantized, coded, and transmitted. The J PEG receiver (or J PEG file reader) decodes the quantized DCT coefficients, computes the inverse two-dimensional DCT of each block, and then puts the blocks back together into a single image. F or typical images, many of the DCT coefficients have values close to zero; these coefficients can be discarded without seriously affecting the quality of the reconstructed image.

The example codebel ow computes the two-dimensional DCT of 8-by-8 blocks in the input image; discards (sets to zero) all but 10 of the 64 DCT coefficients in each block; and then reconstructs the image using the two-dimensional inverse DCT of each block. The transform matrix computation method is used.

```
| = imead(' camerammn.tif');
I = im2doubl e(I);
T = dct nt x(8);
B = bl kproc(I,[8 8],'P1*x*P2',T,T');
mmsk =[[1 1 1 1 1 1 1 0
    1
    1
    1
    0
    0
    0
    0}00\mp@code{0
```

B2 = bl kproc(B, [ 8 8],' P1. *x', mask);
I 2 = bl kproc(B2, [ 8 8],' P1*x*P2', T', T) ;
i mshow(l), figure, i nshow(l)


Although there is some loss of quality in the reconstructed image, it is clearly recognizable, even though almost $85 \%$ of the DCT coefficients were discarded. To experiment with discarding more or fewer coefficients, and to apply this technique to other images, try running the demo function dct deno.

## Radon Transform

Ther adon function in thel mage Processing Tool box computes projections of an image matrix along specified directions. A projection of a two-dimensional function $f(x, y)$ is a line integral in a certain direction. For example, the line integral of $f(x, y)$ in the vertical direction is the projection of $f(x, y)$ onto the $x$-axis; the line integral in the horizontal direction is the projection of $f(x, y)$ onto the $y$-axis. Figure 7-11 shows horizontal and vertical projections for a simple two-dimensional function.


Figure 7-11: Horizontal and Vertical Projections of a Simple Function
Projections can be computed along any angle $\theta$. In general, the Radon transform of $f(x, y)$ is the line integral of $f$ parallel to the $y^{\prime}$ axis

$$
R_{\theta}\left(x^{\prime}\right)=\int_{-\infty}^{\infty} f\left(x^{\prime} \cos \theta-y^{\prime} \sin \theta, x^{\prime} \sin \theta+y^{\prime} \cos \theta\right) d y^{\prime}
$$

where

$$
\left[\begin{array}{l}
x^{\prime} \\
y^{\prime}
\end{array}\right]=\left[\begin{array}{r}
\cos \theta \\
\sin \theta \\
-\sin \theta \\
\cos \theta
\end{array}\right]\left[\begin{array}{l}
x \\
y
\end{array}\right]
$$

Figure 7-12 illustrates the geometry of the Radon transform.


Figure 7-12: The Geometry of the Radon Transform
This command computes the Radon transform of $I$ for the angles specified in the vector thet a
[ $\mathrm{R}, \mathrm{xp}$ ] = radon(I, thet a );

The columns of R contain the Radon transform for each angle in thet a. The vector xp contains the corresponding coordinates al ong the $x^{\prime}$-axis. The "center pixel" of I is defined to befloor ( (size(I)+1)/2); this is the pixel on the $x^{\prime}$-axis corresponding to $x^{\prime}=0$.

The commands below compute and plot the Radon transform at $0^{\circ}$ and $45^{\circ}$ of an image containing a single square object.

```
I = zeros(100, 100);
l(25: 75, 25: 75) = 1;
i mshow(I)
```



Figure 7-13: Two Radon Transforms of a Square Function

Note xp is the same for all projection angles.

The Radon transform for a large number of angles is often displayed as an image. In this example, the Radon transform for the squareimage is computed at angles from $0^{\circ}$ to $180^{\circ}$, in $1^{\circ}$ increments.
thet $\mathrm{a}=0$ : 180;
[ $\mathrm{R}, \mathrm{xp}$ ] = radon(I, thet a$)$;
i magesc( thet $a, x p, R$ );
title('R_\{\theta\} (XIprime)');
$x$ label ('\theta (degrees)');
yl abel (' X prime');
set ( gca, ' XTi ck', 0: 20: 180) ;
col or map( hot ) ;
col orbar


Figure 7-14: A Radon Transform Using 180 Projections

## Using the Radon Transform to Detect Lines

The Radon transform is closely related to a common computer vision operation known as the Hough transform. You can use the radon function to implement a form of the Hough transform used to detect straight lines. The steps are:

1 Compute a binary edge image using the edge function.
। = imead('ic.tif');
BW = edge(I);
i mshow I)
figure, inshow BW)


2 Compute the Radon transform of the edge image.
thet a = 0: 179;
[ R, xp] = radon( BW thet a) ;
figure, i magesc(thet a, xp, R); col ormap(hot);
xl abel('\theta (degrees)'); yl abel ('X prime');
title('R_\{\theta\} (X|prime)');
col or bar


Figure 7-15: Radon Transform of an Edge Image
3 Find the locations of strong peaks in the Radon transform matrix. The locations of these peaks correspond to the location of straight lines in the original image.

In this example, the strongest peak in R corresponds to $\theta=94^{\circ}$ and $x^{\prime}=-101$. The line perpendicular to that angle and located at $x^{\prime}=-101$ is
shown below, superimposed in red on the original image. The Radon transform geometry is shown in black.


Figure 7-16: The Radon Transform Geometry and the Strongest Peak (Red)
N otice that the other strong lines parallel to the red line also appear as peaks at $\theta=94^{\circ}$ in the transform. Also, the lines perpendicular to this line appear as peaks at $\theta=4^{\circ}$.

## The Inverse Radon Transform

The i r adon function performs the inverse Radon transform, which is commonly used in tomography applications. This transform inverts the Radon transform (which was introduced in the previous section), and can therefore be used to reconstruct images from projection data.

As discussed in the previous section "Radon Transform" on page 7-21, given an image I and a set of angles thet a, the function radon can be used to calculate the Radon transform.

$$
R=\operatorname{radon}(1, t \text { het } a) ;
$$

The function i radon can then be called to reconstruct the image $I$.
IR = iradon( R, thet a) ;

In the example above, projections are calculated from the original image I . In most application areas, there is no original image from which projections are formed. For example, in X-ray absorption tomography, projections are formed by measuring the attenuation of radiation that passes through a physical specimen at different angles. The original image can be thought of as a cross section through the specimen, in which intensity values represent the density of the specimen. Projections are collected using special purpose hardware, and then an internal image of the specimen is reconstructed by i radon. This allows for noninvasive imaging of the inside of a living body or another opaque object.
i radon reconstructs an image from parallel beam projections. In paralle beam geometry, each projection is formed by combining a set of line integrals through an image at a specific angle.

Figure 7-17 below illustrates how parallel beam geometry is applied in X-ray absorption tomography. Note that there is an equal number of $n$ emitters and n detectors. Each detector measures the radiation emitted from its corresponding emitter, and the attenuation in the radiation gives a measure of the integrated density, or mass, of the object. This corresponds to the line integral that is calculated in the Radon transform.

The parallel beam geometry used in thefigure is the same as the geometry that was described under "Radon Transform" on page 7-21. $f(x, y)$ denotes the brightness of the image and $R q\left(x^{\prime}\right)$ is the projection at angle $q$.


Figure 7-17: Parallel Beam Projections Through an Object
Another geometry that is commonly used is fan beam geometry, in which there is one emitter and $n$ detectors. Thereare methods for resorting sets of fan beam projections into parallel beam projections, which can then be used by i radon. (F or more information on these methods, see Kak \& Slaney, Principles of Computerized Tomographic I maging, IEEE Press, NY, 1988, pp. 92-93.)
i r adon uses thefiltered backprojection algorithm to computetheinverseR adon transform. This al gorithm forms an approximation to the image। based on the projections in the columns of R. A more accurateresult can be obtained by using
moreprojections in the reconstruction. As the number of projections (thelength of $t$ het a) increases, the reconstructed image I R more accurately approximates the original image I. The vector thet a must contain monotonically increasing angular values with a constant incremental angle $\Delta \theta$. When the scalar $\Delta \theta$ is known, it can be passed to i radon instead of the array of theta values. Here is an example.
I R = ir adon( R, Dt het a) ;

The filtered backprojection algorithm filters the projections in R and then reconstructs the image using the filtered projections. In some cases, noise can be present in the projections. To remove high frequency noise, apply a window to the filter to attenuate the noise. Many such windowed filters are available in i radon. The example call to i radon below applies a Hamming window to the filter. See the i r adon reference page for more information.
I R = i radon( R, thet a, ' Hamming' );
i radon also enables you to specify a normalized frequency, D, above which the filter has zero response. Dmust be a scalar in the range [0,1]. With this option, the frequency axis is rescaled, so that the whole filter is compressed to fit into the frequency range [ $0, \mathrm{D}$. This can be useful in cases where the projections contain little high frequency information but there is high frequency noise. In this case, the noise can be completely suppressed without compromising the reconstruction. The following call to i radon sets a normalized frequency value of 0.85 .

$$
I R=i \operatorname{radon}(R, t \text { het } a, 0.85) ;
$$

## Examples

The commands below illustrate how to use radon and i radon to form projections from a sample image and then reconstruct the image from the projections. The test image is the Shepp-Logan head phantom, which can be generated by the Image Processing Tool box function phant om The phantom image illustrates many of the qualities that are found in real-world tomographic imaging of human heads. The bright elliptical shell along the exterior is anal ogous to a skull, and the many ellipses inside are anal ogous to brain features or tumors.

$$
P=\text { phant om } 256 \text { ) ; }
$$

i nshow $(P)$


As a first step the Radon transform of the phantom brain is calculated for three different sets of theta values. R1 has 18 projections, R2 has 36 projections, and R3 had 90 projections.

```
thet al = 0: 10: 170; [ R1, xp] = radon( P, thet a1);
thet a2 = 0: 5: 175; [ R2, xp] = radon( P, thet a2);
thet a3 = 0: 2: 178; [ R3, xp] = radon(P, thet a3);
```

Now the Radon transform of the Shepp-Logan Head phantom is displayed using 90 projections (R3).
figure, i magesc(thet a3, xp, R3) ; col ormap( hot); col or bar $x$ l abel (' $\backslash$ thet $\mathrm{a}^{\prime}$ ); yl abel (' x ) prime') ;


Figure 7-18: Radon Transform of Head Phantom Using 90 Projections
When we look at Figure 7-18, we can see some of the features of the input image. The first column in the Radon transform corresponds to a projection at $0^{\circ}$ which is integrating in the vertical direction. The centermost column corresponds to a projection at $90^{\circ}$, which is integrating in the horizontal direction. The projection at $90^{\circ}$ has a wider profile than the projection at $0^{\circ}$ due to the larger vertical semi-axis of the outermost ellipse of the phantom.

Figure 7-19 shows the inverse Radon transforms of R1, R2, and R3, which were generated above. Image I 1 was reconstructed with the projections in R1, and it is the least accurate reconstruction, because it has the fewest projections. I 2 was reconstructed with the 36 projections in R2, and the quality of the reconstruction is better, but it is still not clear enough to discern clearly the three small ellipses in the lower portion of the test image. I 3 was reconstructed using the 90 projections in R3, and the result closely resembles the original image. Notice that when the number of projections is relatively small (as in I 1 and $I 2$ ), the reconstruction may include some artifacts from the back projection. To avoid this, use a larger number of angles.

```
| 1 = i radon(R1, 10);
I2 = iradon(R2,5);
I3 = iradon(R3, 2);
```



Figure 7-19: Inverse Radon Transforms of the Shepp-Logan Head Phantom

## Analyzing and Enhancing Images

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## Overview

The Image Processing Tool box supports a range of standard image processing operations for analyzing and enhancing images. Its functions simplify several categories of tasks, including:

- Obtaining pixel values and statistics, which are numerical summaries of data in an image
- Analyzing images to extract information about their essential structure
- Enhancing images to make certain features easier to see or to reduce noise

This section describes specific operations within each category, and shows how to implement each kind of operation using tool box functions.

## Words You Need to Know

An understanding of the following terms will help you to use this chapter. For more explanation of this tableand otherslikeit, see "Words Y ou Need to K now" in the Preface.

| Words | Definitions |
| :--- | :--- |
| Adaptive filter | A filter whose properties vary across an image depending on <br> the local characteristics of the image pixels. |
| Contour | A path in an image al ong which the image intensity values are <br> equal to a constant. |
| Edge | A curve that follows a path of rapid change in image intensity. <br> Edges are often associated with the boundaries of objects in a <br> scene. Edge detection is used to identify the edges in an <br> image. |
| Feature | A quantitative measurement of an image or image region. <br> Examples of image region features include centroid, bounding <br> box, and area. |


| Words | Definitions |
| :--- | :--- |
| Histogram | A graph used in image analysis that shows the distribution of <br> intensities in an image. The information in a histogram can be <br> used to choose an appropriate enhancement operation. For <br> example, if an image histogram shows that the range of <br> intensity values is small, you can use an intensity adjustment <br> function to spread the values across a wider range. |
| Noise | Errors in the image acquisition process that result in pixel <br> values that do not reflect the true intensities of the real scene. |
| Profile | A set of intensity values taken from regularly spaced points <br> along a line segment or multiline path in an image. For points <br> that do not fall on the center of a pixel, the intensity values <br> are interpolated. |
| Quadtree decomposition | An image analysis technique that partitions an image into <br> homogeneous blocks. |

## Pixel Values and Statistics

The Image Processing Tool box provides several functions that return information about the data values that make up an image. These functions return information about image data in various forms, including:

- The data values for selected pixels (pi xval , i mpi xel)
- The data values along a path in an image (i mpr of ile)
- A contour plot of the image data (i mcont our)
- A histogram of the image data (i min st)
- Summary statistics for the image data (nean2, st d2, corr 2)
- Feature measurements for image regions (i mf eat ur e)


## Pixel Selection

The tool box includes two functions that provide information about the color data values of image pixels you specify:

- The pi xval function interactively displays the data values for pixels as you move the cursor over the image. pi xval can also display the Euclidean distance between two pixels.
- The i mpi xel function returns the data values for a selected pixel or set of pixels. Y ou can supply the coordinates of the pixels as input arguments, or you can select pixels using a mouse.

To use pi xval , you first display an image and then enter the pi xval command. pi xval installs a black bar at the bottom of the figure, which displays the ( $x, y$ ) coordinates for whatever pixel the cursor is currently over, and the color data for that pixel.

If you click on the image and hold down the mouse button while you move the cursor, pi xval also displays the Euclidean distance between the point you clicked on and the current cursor location. pi xval draws a line between these points to indicate the distance being measured. When you release the mouse button, the line and the distance display disappear.
pi xval gives you more immediate results than i mpi xel, but i mpi xel has the advantage of returning its results in a variable, and it can be called either interactively or noninteractively. If you call i mpi xel with no input arguments, the cursor changes to a crosshair when it is over the image. Y ou can then click
on the pixels of interest; i mpi xel displays a small star over each pixel you select. When you are done selecting pixels, press Return. i mpi xel returns the color values for the selected pixels, and the stars disappear.

In this example, you call i mpi xel and click on three points in the displayed image, and then press Return.
inshow canoe.tif
vals = i mpi xel

val s =
0. 1294
0. 1294
0. 1294
0.5176
0
0
0. 7765
0. 6118
0. 4196

Notice that the second pixel, which is part of the canoe, is pure red; its green and blue values are both 0 .

For indexed images, pi xval and i mpi xel both show the RGB values stored in the col ormap, not the index values.

## Intensity Profile

The i mpr of ile function calculates and plots the intensity values along a line segment or a multiline path in an image. You can supply the coordinates of the line segments as input arguments, or you can define the desired path using a mouse. In either case, i mpr of il e uses interpolation to determine the values of equally spaced points along the path. (By default, i mpr of il e uses nearest
neighbor interpolation, but you can specify a different method. See Chapter 4, "Geometric Operations", for a discussion of interpolation.) i mpr of ile works best with intensity and RGB images.

For a single line segment, i mpr of il e plots the intensity values in a two-dimensional view. For a multiline path, i mpr of ile plots the intensity values in a three-dimensional view.

If you call i mpr of ile with no arguments, the cursor changes to a cross hair when it is over the image. You can then specify line segments by clicking on the endpoints; i mpr of il e draws a line between each two consecutive points you select. When you finish specifying the path, press Return. i mpr of ile displays the plot in a new figure.

In this example, you call i mpr of il e and specify a single line with the mouse. The line is shown in red, and is drawn from left to right.

```
i nshow debye1.tif
```

i mprof ile

i mpr of ile displays a plot of the data along the line.


Figure 8-1: A Plot of Intensity Values Along a Line Segment in an Intensity Image

Notice the peaks and valleys and how they correspond to the light and dark bands in the image.

The example below shows how i mpr of i l e works with an RGB image. The red line indicates where the line selection was made. Note that the line was drawn from top to bottom.
i mshow fl owers.tif
i mprofile

i mpr of il e displays a plot with separate lines for the red, green, and blue intensities.


Figure 8-2: A Plot of Intensity Values Along a Line Segment in an RGB Image
Notice how the lines correspond to the colors in the image. F or example, the central region of the pl ot shows high intensities of green and red, whiletheblue intensity is 0 . These are the values for the yellow flower.

## Image Contours

You can usethetool box function i moont our to display a contour plot of the data in an intensity image. This function is similar to the cont our function in MATLAB, but it automatically sets up the axes so their orientation and aspect ratio match the image.

This example displays an intensity image of grains of rice and a contour plot of the image data.

```
| = imread('rice.tif');
i nshow(1)
figure, imcontour(1)
```



Figure 8-3: Rice.tif and Its Contour Plot
You can use the cl abel function to label the levels of the contours. See the description of cl abel in the MATLAB F unction Reference for details.

## Image Histogram

An image histogram is a chart that shows the distribution of intensities in an indexed or intensity image. The image histogram function ini st creates this plot by making $n$ equally spaced bins, each representing a range of data values. It then calculates the number of pixels within each range. For example, the commands below display an image of grains of rice, and a histogram based on 64 bins.

```
| = imead('rice.tif');
i mshow(1)
figure, i nmi st(I,64)
```




Figure 8-4: Rice.tif and Its Histogram
The histogram shows a peak at around 100, due to the dark gray background in the image.

For information about how to modify an image by changing the distribution of its histogram, see "I ntensity Adjustment" on page 8-15.

## Summary Statistics

You can compute standard statistics of an image using the mean2, st d2, and cor 2 functions. mean2 and st d2 compute the mean and standard deviation of the elements of a matrix. corr 2 computes the correlation coefficient between two matrices of the same size.

These functions are two-dimensional versions of the rean, st d, and cor roef functions described in the MATLAB Function Reference.

## Feature Measurement

You can use the i nff eat ure function to compute feature measurements for image regions. F or example, i nf eat ur e can measure such features as the area, center of mass, and bounding box for a region you specify. See the reference page for i nf eat ure for more information.

## Image Analysis

Image analysis techniques return information about the structure of an image. This section describes tool box functions that you can use for these image analysis techniques:

- Edge detection
- Quadtree decomposition

The functions described in this section work only with intensity images.

## Edge Detection

You can use the edge function to detect edges, which are those places in an image that correspond to object boundaries. To find edges, this function looks for places in the image where the intensity changes rapidly, using one of these two criteria:

- Places where the first derivative of the intensity is larger in magnitude than some threshold
- Places where the second derivative of the intensity has a zero crossing
edge provides a number of derivative estimators, each of which implements one of the definitions above. For some of these estimators, you can specify whether the operation should be sensitive to horizontal or vertical edges, or both. edge returns a binary image containing 1's whereedges are found and 0's elsewhere.

The most powerful edge-detection method that edge provides is the Canny method. The Canny method differs from the other edge-detection methods in that it uses two different thresholds (to detect strong and weak edges), and includes the weak edges in the output only if they are connected to strong edges. This method is therefore less likely than the others to be "fooled" by noise, and more likely to detect true weak edges.

The example below illustrates the power of the Canny edge detector. It shows the results of applying the Sobel and Canny edge detectors to the rice. ti f image.

```
| = imead('rice.tif');
BVL = edge(I,'sobel');
BVZ = edge(I,' canny' );
i mshow( BVI)
```

fi gure, i mshow (BVD)


Sobel Filter


Canny Filter

For an interactive demonstration of edge detection, try running edgedem.

## Quadtree Decomposition

Quadtree decomposition is an analysis technique that invol ves subdividing an image into blocks that are more homogeneous than the image itself. This technique reveal sinformation about the structure of the image. It is also useful as the first step in adaptive compression algorithms.

You can perform quadtree decomposition using the qt decomp function. This function works by dividing a square image into four equal-sized square blocks, and then testing each block to see if it meets some criterion of homogeneity (e.g., if all of the pixels in the block are within a specific dynamic range). If a block meets the criterion, it is not divided any further. If it does not meet the criterion, it is subdivided again into four blocks, and thetest criterion is applied to those blocks. This process is repeated iteratively until each block meets the criterion. The result may have blocks of several different sizes.

For example, suppose you want to perform quadtree decomposition on a 128-by-128 intensity image. The first step is to divide the image into four 64 -by- 64 blocks. You then apply the test criterion to each block; for example, the criterion might be

```
max(bl ock(:)) - min(bl ock(:)) <= 0.2
```

If one of the blocks meets this criterion, it is not divided any further; it is 64 -by-64 in the final decomposition. If a block does not meet the criterion, it is
then divided into four 32-by-32 blocks, and the test is then applied to each of theseblocks. Theblocks that fail to meet thecriterion arethen divided into four 16-by-16 blocks, and so on, until all blocks "pass." Some of the blocks may be as small as 1-by-1, unless you specify otherwise.

The call to qt decomp for this example would be

$$
S=q t \operatorname{decomp}(1,0.2)
$$

$S$ is returned as a sparse matrix whose nonzero el ements represent the upper-left corners of theblocks; the value of each nonzero element indicates the block size. S is the same size as I.

Note The threshold value is specified as a value between 0 and 1 , regardless of the class of $I$. If $I$ is ui nt 8 , the threshold value you supply is multiplied by 255 to determine the actual threshold to use; if I is ui nt 16, the threshold value you supply is multiplied by 65535.

The example below shows an image and a representation of its quadtree decomposition. Each black square represents a homogeneous block, and the white lines represent the boundaries between blocks. Notice how the blocks are smaller in areas corresponding to large changes in intensity in the image.


Figure 8-5: An Image (left) and a Representation of its Quadtree Decomposition

You can also supply qt decomp with a function (rather than a threshold value) for deciding whether to split blocks; for example, you might base the decision
on the variance of the block. See the reference page for qt decomp for more information.

For an interactive demonstration of quadtree decomposition, try running qt demo.

## Image Enhancement

Image enhancement techniques are used to improve an image, where "improve" is sometimes defined objectively (e.g., increase the signal-to-noise ratio), and sometimes subjectively (e.g., make certain features easier to see by modifying the colors or intensities).

This section discusses these image enhancement techniques:

- "Intensity Adjustment"
- "Noise Removal"

The functions described in this section apply primarily to intensity images. However, some of these functions can be applied to color images as well. For information about how these functions work with col or images, see the reference pages for the individual functions.

## Intensity Adjustment

Intensity adjustment is a technique for mapping an image's intensity values to a new range. For example, look at ri ce. tif. It is a low contrast image. If you look at a histogram of ri ce. tif in Figure 8-4, it indicates that there are no values bel ow 40 or above 255 . If you remap the data values to fill the entire intensity range [0, 255], you can increase the contrast of the image.

You can do this kind of adjustment with the i madj ust function. F or example, this code performs the adjustment described above.

```
| = imead('rice.tif');
J = immdj ust(I,[0.15 0.9],[0 1]);
```

With the two vectors supplied, i madj ust scales pixel values of 0.15 to 0 and 0.9 to 1 . Notice that the intensities are specified as values between 0 and 1 regardless of the class of I . If I is ui nt 8, the values you supply are multiplied by 255 to determine the actual values to use; if I is ui nt 16, the values are multiplied by 65535.

Now display the adjusted image and its histogram.

## i mshow ( )

figure, i nmi st(J, 64)



Figure 8-6: Rice.tif After an Intensity Adjustment and a Histogram of Its Adjusted Intensities

Notice the increased contrast in theimage, and that thehistogram now fills the entire range.

Similarly, you can decrease the contrast of an image by narrowing the range of the data, as in this call.

$$
\mathrm{J}=\mathrm{i} \text { madj ust (I,[ } 0 \text { 1],[ } 0.30 .8]) \text {; }
$$

The general syntax is

```
J = i madj ust(I,[l ow hi gh],[bottom top])
```

where I ow and hi gh are the intensities in the input image, which are mapped to bot t omand top in the output image.

In addition to increasing or decreasing contrast, you can perform a wide variety of other image enhancements with i madj ust. In the example below, the man's coat is too dark to reveal any detail. The call to i madj ust maps the range [0,51] in the ui nt 8 input image to $[128,255]$ in the output image. This brightens the image considerably, and also widens the dynamic range of the dark portions of the original image, making it much easier to see the details in the coat.

```
| = immead('cameraman.tif');
J = i madj ust(I,[0 0. 2],[0.5 1]);
i mshow(1)
figure, i nshow(J)
```



Figure 8-7: Cameraman.tif Before and After Remapping, and Widening its Dynamic Range

Notice that this operation results in much of the image being washed out. This is because all values above 51 in the original image get mapped to 255 in the adjusted image.

## Gamma Correction

i madj ust maps I owto bot t om and hi gh tot op. By default, the values between I ow and hi gh are mapped linearly to values between bot t omand top. For example, the value halfway between I owand hi gh corresponds to the value halfway between bot tomand top.
i madj ust can accept an additional argument which specifies the gamma correction factor. Depending on the value of gamma, the mapping between values in the input and output images may be nonlinear. For example, the value halfway between I owand hi gh may map to a value either greater than or less than the value halfway between bot t omand top.

Gamma can be any value between 0 and infinity. If gamma is 1 (the default), the mapping is linear. If gamma is less than 1, the mapping is weighted toward higher (brighter) output values. If gamma is greater than 1 , the mapping is weighted toward lower (darker) output values.

The figure below illustrates this relationship. The threetransformation curves show how values are mapped when gamma is less than, equal to, and greater
than 1. (In each graph, the x-axis represents the intensity values in the input image, and the $y$-axis represents the intensity values in the output image.)


Figure 8-8: Plots Showing Three Different Gamma Correction Settings
The example bel ow illustrates gamma correction. Notice that in the call to i madj ust, the data ranges of the input and output images are specified as empty matrices. When you specify an empty matrix, i madj ust uses the default range of $[0,1]$. In the example, both ranges are left empty; this means that gamma correction is applied without any other adjustment of the data.

```
[X,n⿴p] = immead('forest.tif')
I = ind2gray(X, nap);
J = i madj ust(I,[],[],0.5);
i mshow(1)
figure, inshow(J)
```



Figure 8-9: Forest.tif Before and After Applying Gamma Correction of 0.5

## Histogram Equalization

The process of adjusting intensity values can be done automatically by the hi st eq function. hi st eq performs histogram equalization, which involves transforming the intensity values so that the histogram of the output image approximately matches a specified histogram. (By default, hi st eq tries to match a flat histogram with 64 bins, but you can specify a different histogram instead; see the reference page for hi st eq.)

This example illustrates using hi st eq to adjust an intensity image. The original image has low contrast, with most values in the middle of the intensity range. hi st eq produces an output image having values evenly distributed throughout the range.

```
I = imead(' pout.tif');
J = hi steq(I);
i mshow(I)
figure, inshow(J)
```



Figure 8-10: Pout.tif Before and After Histogram Equalization
The example below shows the histograms for the two images.
figure, i mist(I)
figure, i mmi st(J)



Figure 8-11: Histogram Before Equalization (left) and After Equalization (right)
hi st eq can return an additional 1-by-256 vector that shows, for each possible input value, the resulting output value. (The values in this vector are in the range [0,1], regardless of the class of the input image.) Y ou can plot this data to get the transformation curve. For example,

I =imead('pout.tif');
[J,T] = hi steq(I);
fi gure, pl ot ( (0:255)/255, T) ;


Notice how this curve reflects the histograms in the previous figure, with the input values being mostly between 0.3 and 0.6 , while the output values are distributed evenly between 0 and 1.

For an interactive demonstration of intensity adjustment, try running i madj demo.

## Noise Removal

Digital images are prone to a variety of types of noise. There are several ways that noise can be introduced into an image, depending on how the image is created. For example,

- If the image is scanned from a photograph made on film, the film grain is a source of noise. Noise can also be the result of damage to the film, or be introduced by the scanner itself.
- If the image is acquired directly in a digital format, the mechanism for gathering the data (such as a CCD detector) can introduce noise.
- Electronic transmission of image data can introduce noise.

The tool box provides a number of different ways to remove or reduce noise in an image. Different methods are better for different kinds of noise. The methods available include:

- Linear filtering
- Median filtering
- Adaptive filtering

Also, in order to simulate the effects of some of the problems listed above, the tool box provides the i moi se function, which you can use to add various types of noise to an image. The examples in this section use this function.

## Linear Filtering

You can use linear filtering to remove certain types of noise. Certain filters, such as averaging or Gaussian filters, are appropriate for this purpose. For example, an averaging filter is useful for removing grain noise from a photograph. Because each pixel gets set to the average of the pixels in its neighborhood, local variations caused by grain are reduced.

See "Linear Filtering" on page 6-4 for more information.

## Median Filtering

Median filtering is similar to using an averaging filter, in that each output pixel is set to an "average" of the pixel values in the neighborhood of the corresponding input pixel. However, with median filtering, the value of an output pixel is determined by the median of the neighborhood pixels, rather than the mean. The median is much less sensitive than the mean to extreme values (called outliers). Median filtering is therefore better able to remove these outliers without reducing the sharpness of the image.

The redf il t 2 function implements median filtering. The example bel ow compares using an averaging filter and medfil t 2 to remove salt and pepper noise. This type of noise consists of random pixels being set to black or white (the extremes of the data range). In both cases the size of the neighborhood used for filtering is 3-by-3.

First, read in the image and add noise to it.

```
| = imead('ei ght.tif');
J = immoi se(I,'salt & pepper',0.02);
i nshow(1)
figure, i nshow(J)
```



Figure 8-12: Eight.tif Before and After Adding Salt-and-Pepper Noise
Now filter the noisy image and display the results. Notice that medf il t 2 does a better job of removing noise, with less blurring of edges.

```
K = filter2(fspeci al(' average', 3), J)/ 255;
L = medfilt2(J,[3 3]);
fi gure, i mshow K)
figure, i mshow L)
```



Figure 8-13: N oisy Version of Eight.tif Filtered with Averaging Filter (left) and
Median Filter (right)
Median filtering is a specific case of order-statistic filtering, also known as rank filtering. For information about order-statistic filtering, see the reference page for the or df ilt 2 function.

## Adaptive Filtering

The wi ener 2 function applies a Wiener filter (a type of linear filter) to an image adaptively, tailoring itself to the local image variance. Where the variance is large, wi ener 2 performs little smoothing. Wherethe variance is small, wi ener 2 performs more smoothing.
This approach often produces better results than linear filtering. The adaptive filter is more selective than a comparable linear filter, preserving edges and other high frequency parts of an image. In addition, there are no design tasks; the wi ener 2 function handles all preliminary computations, and implements the filter for an input image. wi ener 2, however, does require more computation time than linear filtering.
wi ener 2 works best when the noise is constant-power ("white") additive noise, such as Gaussian noise. The example below applies wi ener 2 to an image of Saturn that has had Gaussian noise added.

```
| = imead('saturn.tif');
J = i mmoi se(I,'gaussi an', 0, 0.005);
K = wi ener2(J,[5 5]);
i mshow(J)
figure, i mshow(K)
```



Figure 8-14: Noisy Version of Saturn.tif Before and After Adaptive Filtering
For an interactive demonstration of filtering to remove noise, try running nrfiltdem.

## Binary I mage Operations

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Words Y ou Need to Know ..... 9-2
Neighborhoods ..... 9-3
Padding of Borders ..... 9-3
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## Overview

A binary image is an image in which each pixel assumes one of only two di screte values. Essentially, these two values correspond to on and of $f$. Looking at an image in this way makes it easier to distinguish structural features. For example, in a binary image, it is easy to distinguish objects from the background.

In the Image ProcessingTool box, a binary image is stored as a two-dimensional matrix of 0's (which represent of $f$ pixels) and 1's (which represent on pixels). The on pixels are the foreground of the image, and the of $f$ pixels are the background.

Binary image operations return information about the form or structure of binary images only. To perform these operations on another type of image, you must first convert it to binary (using, for example, the i m2bwfunction).

## Words You Need to Know

An understanding of the following terms will help you to use this chapter. For more explanation of this tableand otherslikeit, see "Words Y ou Need to K now" in the Preface.

| Words | Definitions |
| :--- | :--- |
| Background | The set of black (or of f ) pixels in a binary object. |
| Binary image | An image containing only black and white pixels. In MATLAB, <br> a binary image is represented by a ui nt 8 or doubl e logi cal <br> matrix containing 0's and l's (which usually represent black <br> and white, respectively). A matrix is logical when its "logical <br> flag" is turned "on." We often use the variable name BWto <br> represent a binary image in memory. |
| Connected component | A set of white pixels that form a connected group. A connected <br> component is "8-connected" if diagonally adjacent pixels are <br> considered to betouching, otherwise, it is "4-connected."In the <br> context of this chapter, "object" is a synonym for "connected <br> component." |
| Foreground | The set of white (or on) pixels in a binary object. |


| Words | Definitions |
| :--- | :--- |
| Morphology | A broad set of binary image operations that process images <br> based on shapes. M orphol ogical operations apply a <br> structuring element to an input image, creating an output <br> image of the same size. The most basic morphological <br> operations are dilation and erosion. |
| Neighborhood | A set of pixels that are defined by their locations relative to <br> the pixel of interest. In binary image operations, a <br> neighborhood can be defined by a structuring element or by <br> using the criterion for a 4- or 8-connected neighborhood. |
| Object | A set of white pixels that form a connected group. In the <br> context of this chapter, "object" and "connected component" <br> are basically equivalent. See "Connected component" above. |
| Structuring element | A matrix used to define a neighborhood shape and size for <br> binary image operations, including dilation and erosion. It <br> consists of only 0's and 1's and can have an arbitrary shape <br> and size. The pixels with values of 1 define the neighborhood. <br> By choosing a proper structuring element shape, you can <br> construct a morphol ogical operation that is sensitive to <br> specific shapes. |

## Neighborhoods

M ost binary image al gorithms work with groups of pixels called neighborhoods. A pixel's neighborhood is some set of pixels that are defined by their locations relativeto that pixel. The neighborhood can include or omit the pixel itself, and the pixels included in the neighborhood are not necessarily adjacent to the pixel of interest. Different types of neighborhoods are used for different binary operations.

## Padding of Borders

If a pixel is near the border of an image, some of the pixels in the image's neighborhood may be missing. F or example, if the neighborhood is defined to include the pixel directly above the pixel of interest, then a pixel in the top row of an image will be missing this neighbor.

In order to determine how to process these pixels, the binary image functions pad the borders of the image, usually with 0's. In other words, these functions process the border pixels by assuming that the image is surrounded by additional rows and columns of 0's. These rows and columns do not become part of the output image and are used only as parts of the neighborhoods of the actual pixels in the image. However, the padding can in some cases produce border effects, in which the regi ons near the borders of the output image do not appear to be homogeneous with the rest of the image. Their extent depends on the size of the neighborhood.

## Displaying Binary Images

When you display a binary image with inshow, by default the foreground (i.e., the on pixels) is white and the background is black. Y ou may prefer to invert these images when you display or print them, or else display them using a colormap. See "Displaying Binary Images" on page 3-7 for more information.

The remainder of this chapter describes the functions in the Image Processing Tool box that perform various types of binary image operations. These operations are described in the following sections:

- "Morphological Operations" on page 9-5
- "Object-Based Operations" on page 9-11
- "F eature Measurement" on page 9-19
- "Lookup Table Operations" on page 9-21


## Morphological Operations

Morphological operations are methods for processing binary images based on shapes. These operations take a binary image as input, and return a binary image as output. The value of each pixel in the output image is based on the corresponding input pixel and its neighbors. By choosing the neighborhood shape appropriately, you can construct a morphological operation that is sensitive to specific shapes in the input image.

## Dilation and Erosion

The main morphological operations are dilation and erosion. Dilation and erosion are related operations, although they produce very different results. Dilation adds pixels to the boundaries of objects (i.e., changes them from of $f$ to on), while erosion removes pixels on object boundaries (changes them from on to of $f$ ).

Each dilation or erosion operation uses a specified neighborhood. The state of any given pixel in the output image is determined by applying a rule to the neighborhood of the corresponding pixel in the input image. The rule used defines the operation as a dilation or an erosion.

- For dilation, if any pixel in the input pixel's neighborhood is on, the output pixel is on. Otherwise, the output pixel is of $f$.
- For erosion, if every pixel in the input pixel's neighborhood is on, the output pixel is on. Otherwise, the output pixel is of f .

The neighborhood for a dilation or erosion operation can be of arbitrary shape and size. The neighborhood is represented by a structuring element, which is a matrix consisting of only 0's and 1's. The center pixel in the structuring element represents the pixel of interest, while the elements in the matrix that are on (i.e., $=1$ ) define the neighborhood.

The center pixel is defined as fl oor ( ( si ze( SE) +1 ) / 2 ), where SE is the structuring element. For example, in a 4-by-7 structuring element, the center pixel is $(2,4)$. When you construct the structuring element, you should make sure that the pixel of interest is actually the center pixel. You can do this by adding rows or columns of 0's, if necessary. F or example, suppose you want the neighborhood to consist of a 3-by-3 block of pixels, with the pixel of interest in the upper-left corner of the block. The structuring element would not be
ones( 3) , becausethis matrix has the wrong center pixel. Rather, you could use this matrix as the structuring element.

| 0 | 0 | 0 | 0 |
| :--- | :--- | :--- | :--- |
| 0 | 1 | 1 | 1 |
| 0 | 1 | 1 | 1 |
| 0 | 1 | 1 | 1 |

For erosion, the neighborhood consists of the on pixels in the structuring element. For dilation, the neighborhood consists of the on pixels in the structuring element rotated 180 degrees. (The center pixel is still selected before the rotation.)

Suppose you want to perform an erosion operation. Figure 9-1 shows a sample neighborhood you might use. E ach neighborhood pixel is indicated by an $x$, and the center pixel is the one with a circle.

| x |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- |
|  | x |  |  |  |
|  |  | x |  |  |
|  |  |  | x |  |
|  |  |  |  | x |

Figure 9-1: A Neighborhood That Will Represented as a Structuring Element
The structuring element is therefore

| 1 | 0 | 0 | 0 | 0 |
| :--- | :--- | :--- | :--- | :--- |
| 0 | 1 | 0 | 0 | 0 |
| 0 | 0 | 1 | 0 | 0 |
| 0 | 0 | 0 | 1 | 0 |
| 0 | 0 | 0 | 0 | 1 |

The state (i.e., on or of f ) of any given pixel in the output image is determined by applying the erosion rule to the neighborhood pixels for the corresponding pixel in the input image. For example, to determine the state of the pixel $(4,6)$ in the output image:

- Overlay the structuring element on the input image, with the center pixel of the structuring element covering the pixel $(4,6)$.
- Look at the pixels in the neighborhood of the input pixel. These are the five pixels covered by 1's in the structuring element. In this case the pixels are: $(2,4),(3,5),(4,6),(5,7),(6,8)$. If all of these pixels are on, then set the pixel in the output image $(4,6)$ to on. If any of these pixels is of $f$, then set the pixel $(4,6)$ in the output image to of $f$.

You perform this procedure for each pixel in the input image to determine the state of each corresponding pixel in the output image.

N ote that for pixels on borders of the image, some of the 1's in the structuring element are actually outside the image. These elements are assumed to cover of $f$ pixels. (See the earlier section, "Padding of Borders" on page 9-3.) As a result, the output image will usually have a black border, as in the example below.

The Image Processing Tool box performs dilation through the di I at e function, and erosion through the er ode function. E ach of these functions takes an input image and a structuring element as input, and returns an output image.
This example illustrates the erosion operation described above.

```
BWA = imread('circbw.tif');
SE = eye(5);
BWR = er ode( BW\, SE);
i nshow( BVA)
fi gure, i nshow( BVD)
```



Figure 9-2: Circbw.tif Before and After Erosion with a Diagonal Structuring Element

Notice the diagonal streaks in the output image (on the right). These are due to the shape of the structuring element.

## Related Operations

There are many other types of morphol ogical operations in addition to dilation and erosion. H owever, many of these operations are just modified dilations or erosions, or combinations of dilation and erosion. F or example, closureconsists of a dilation operation followed by erosion with the same structuring element. A related operation, opening, is the reverse of closure; it consists of erosion followed by dilation.

F or example, suppose you want to remove all the circuit lines from the original circuit image, leaving only the rectangular outlines of microchips. Y ou can accomplish this through opening.

To perform the opening, you begin by choosing a structuring element. This structuring element should be largeenough to removethelines when you erode the image, but not large enough to remove the rectangles. It should consist of all 1's, so it removes everything but large continuous patches of foreground pixels. Therefore, you create the structuring element like this.

```
SE = ones(40, 30);
```

Next, you perform the erosion. This removes all of the lines, but also shrinks the rectangles.

```
BVR = er ode( BVI, SE);
```

i nshow BUR)


Finally, you perform dilation, using the same structuring element, to restore the rectangles to their original sizes.
$B W B=$ di $I$ ate( $B V R, S E)$;
i mshow (BVB)


## Predefined 0 perations

You can use di I at e and er ode to implement any morphol ogical operation that can be defined as a set of dilations and erosions. However, there are certain operations that are so common that the tool box provides them as predefined procedures. These operations are available through the burror ph function. bumor ph provides eighteen predefined operations, including opening and closure.

F or example, suppose you want to reduce all objects in the circuit image to lines, without changing the essential structure (topology) of the image. This process is known as skeletonization. You can use bunor ph to do this.

```
BV1 = i mread(' circbw.tif');
BVD = bumor ph( BKL,'skel',I nf );
i nshow( BVI)
fi gure, i nshow( BVR)
```



Figure 9-3: Circbw.tif Before and After Skeletonization
The third argument to bunror ph indi cates the number of times to perform the operation. F or example, if this valueis 2, the operation is performed twice, with the result of the first operation being used as the input for the second operation. In the example above, the value is I nf. In this case bumor ph performs the operation repeatedly until it no longer changes.

For more information about the predefined operations available, see the reference page for bwror ph.

## Object-Based Operations

In a binary image, an object is any set of connected pixels with the value 1. (meaning that they are "on"). For example, this matrix represents a binary image containing a single object, a 3-by-3 square. The rest of the image is background.

| 0 | 0 | 0 | 0 | 0 | 0 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 1 | 1 | 1 | 0 | 0 |
| 0 | 1 | 1 | 1 | 0 | 0 |
| 0 | 1 | 1 | 1 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 |

This section discusses the types of neighborhoods used for object-based operations, and describes how to use tool box functions to perform:

- Perimeter determination
- Binary flood fill
- Connected-components labeling
- Object selection


## 4- and 8-Connected Neighborhoods

For many operations, distinguishing objects depends on the convention used to decide whether pixels are connected. There are two different conventions typically used: 4-connected or 8-connected neighborhoods.

In an 8-connected neighborhood, all of the pixels that touch the pixel of interest are considered, including those on the diagonals. This means that if two adjoining pixels are on, they are part of the same object, regardless of whether they are connected along the horizontal, vertical, or diagonal direction.


Figure 9-4: An 8-Connected Neighborhood
In a 4-connected neighborhood, the pixels along the diagonals are not considered. This means that a pair of adjoining pixels are part of the same object only if they are both on and are connected al ong the horizontal or vertical direction.


Figure 9-5: A 4-Connected Neighborhood

The type of neighborhood you choose affects the number of objects found in an image and the boundaries of those objects. Therefore, the results of the object-based operations often differ for the two types of neighborhoods.

For example, this matrix represents a binary image that has one 8-connected object or two 4-connected objects.

| 0 | 0 | 0 | 0 | 0 | 0 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 0 | 1 | 1 | 0 | 0 | 0 |
| 0 | 1 | 1 | 0 | 0 | 0 |
| 0 | 0 | 0 | 1 | 1 | 0 |
| 0 | 0 | 0 | 1 | 1 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 |

## Perimeter Determination

The buper i mfunction determines the perimeter pixels of the objects in a binary image. Y ou can use either a 4- or 8-connected neighborhood for perimeter determination. A pixel is considered a perimeter pixel if it satisfies both of these criteria:

- It is an on pixel.
- One (or more) of the pixels in its neighborhood is of $f$.

This example finds the perimeter pixels in the circuit image.

```
BV1 = imread(' circbw.tif');
BVD = buperim( BVI);
i mshow( BV1)
fi gure, i nshow( BVD)
```



Figure 9-6: Circbw.tif Before and After Perimeter Determination

## Flood Fill

The buf ill function performs a flood-fill operation on a binary image. Y ou specify a background pixel as a starting point, and bwf ill changes connected background pixels (0's) to foreground pixels (1's), stopping when it reaches object boundaries. The boundaries are determined based on the type of neighborhood you specify.

This operation can be useful in removing irrel evant artifacts from images. For example, suppose you have a binary image, derived from a photograph, in which the foreground objects represent spheres. In the binary image, these objects should appear as circles, but instead are donut shaped because of reflections in the original photograph. Before doing any further processing of the image, you may want to first fill in the "donut holes" using buf ill.
buf ill differs from the other object-based operations in that it operates on background pixels, rather than the foreground. If the foreground is 8 -connected, the background is 4-connected, and vice versa. Note, however, that as with the other object-based functions, you specify the connectedness of the foreground when you call bwfill.

The implications of 4- vs. 8-connected foreground can be illustrated with flood-fill operation matrix.

BVI =

| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 0 | 1 | 1 | 1 | 1 | 1 | 0 | 0 |
| 0 | 1 | 0 | 0 | 0 | 1 | 0 | 0 |
| 0 | 1 | 0 | 0 | 0 | 1 | 0 | 0 |
| 0 | 1 | 0 | 0 | 0 | 1 | 0 | 0 |
| 0 | 1 | 1 | 1 | 1 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |

Regardless of whether the foreground is 4-connected or 8-connected, this image contains a single object. However, the topology of the object differs depending on the type of neighborhood. If the foreground is 8-connected, the object is a closed contour, and there are two separate background el ements (the part inside the loop and the part outside). If the foreground is 4-connected, the contour is open, and there is only one background element.

Suppose you call buf ill, specifying the pixel BVI (4,3) as the starting point.

| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 1 | 1 | 1 | 1 | 1 | 0 | 0 |
| 0 | 1 | 1 | 1 | 1 | 1 | 0 | 0 |
| 0 | 1 | 1 | 1 | 1 | 1 | 0 | 0 |
| 0 | 1 | 1 | 1 | 1 | 1 | 0 | 0 |
| 0 | 1 | 1 | 1 | 1 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |

buf ill fills in just the inside of the loop, because buf ill uses an 8 -connected foreground by default. If you specify a 4-connected foreground instead, buf i I I fills in the entire image, because the entire background is a single 8-connected element.

For example,
buf ill( BVL, 4, 3, 4)
ans $=$

| 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |

Note that unlike other binary image operations, buf ill pads with l's rather than 0's along the image border. This prevents the fill operation from wrapping around the border.

You can also use bufill interactively, selecting starting pixels with a mouse. See the reference page for bwill for more information.

## Connected-Components Labeling

The bw abel function performs connected-components labeling, which is a method for indicating each discrete object in a binary image. You specify an input binary image and the type of neighborhood, and bw abel returns a matrix of the same size as the input image. The different objects in the input image are distinguished by different integer values in the output matrix.

For example, suppose you have this binary image.

```
BV1 =
```

| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 0 | 1 | 1 | 0 | 0 | 1 | 1 | 1 |
| 0 | 1 | 1 | 0 | 0 | 0 | 1 | 1 |
| 0 | 1 | 1 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 1 | 1 | 0 | 0 | 0 |
| 0 | 0 | 0 | 1 | 1 | 0 | 0 | 0 |
| 0 | 0 | 0 | 1 | 1 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |

You call bw abel, specifying 4-connected neighborhoods.
bul abel (BV1, 4)
ans $=$

| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 0 | 1 | 1 | 0 | 0 | 3 | 3 | 3 |
| 0 | 1 | 1 | 0 | 0 | 0 | 3 | 3 |
| 0 | 1 | 1 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 2 | 2 | 0 | 0 | 0 |
| 0 | 0 | 0 | 2 | 2 | 0 | 0 | 0 |
| 0 | 0 | 0 | 2 | 2 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |

In the output matrix, the 1's represent one object, the 2's a second object, and the 3's a third. Notice that if you had used 8-connected neighborhoods (the default), there would be only two objects, because the first and second objects would be a single object, connected al ong the diagonal.

The output matrix is not a binary image, and its class is doubl e. A useful approach to viewing it is to display it as a pseudocolor indexed image, first adding 1 to each element, so that the data is in the proper range. Each object displays in a different col or, so the objects are easier to distinguish than in the original image.

The example below illustrates this technique. Notice that this example uses a col ormap in which the first color (the background) is black and the other col ors are easily distinguished.

```
X = bw abel (BVI, 4);
map = [0 0 0;j et(3)];
i mshow( X+1, map, ' notruesi ze' )
```



Figure 9-7: A Binary Image Displayed with a Colormap After Connected-Components Labeling

## Object Selection

You can use the busel ect function to select individual objects in a binary image. You specify pixels in the input image, and bwsel ect returns a binary image that includes only those objects from the input image that contain one of the specified pixels.

You can specify the pixels either noninteractively or with a mouse. F or example, suppose you want to select 8-connected objects in theimagedisplayed in the current axes. You type
BVR = bwsel ect (8);

The cursor changes to a cross-hair when it is over the image. Click on the objects you want to select; bwsel ect displays a small star over each pixel you click on. When you are done, press Return. busel ect returns a binary image consisting of the objects you selected, and removes the stars.

See the reference page for busel ect for more information.

## Feature Measurement

When you process an image, you may want to obtain information about how certain features of the image change. F or example, when you perform dilation, you may want to determine how many pixels are changed from of $f$ to on by the operation, or to see if the number of objects in the image changes. This section describes two functions, bwar ea and bweul er, that return two common measures of binary images: the image area and the Euler number.

In addition, you can use thei nf eat ure function, in combination with bul abel, to compute measurements of various features in a binary image. See the reference page for i nff eat ur e for more information.

## Image Area

The bwar ea function returns the area of a binary image. The area is a measure of the size of the foreground of the image. Roughly speaking, the area is the number of on pixels in the image.
bwar ea does not simply count the number of on pixels, however. Rather, bwar ea weights different pixel patterns unequally when computing the area. This weighting compensates for the distortion that is inherent in representing a continuous image with discrete pixels. For example, a diagonal line of 50 pixels is longer than a horizontal line of 50 pixels. As a result of the weighting bwar ea uses, the horizontal line has area of 50 , but the diagonal line has area of 62.5.

This example uses bwar ea to determine the percentage area increase in ci rcbw. tif that results from a dilation operation.

```
BV1 = i mread(' ci rcbw.tif');
SE = ones(5);
BVR = di I at e( BVI, SE);
i ncrease = (bwarea(BV\mathbb{D}) - bwarea(BKI))/bwarea(BML);
increase =
```

0. 3456

The dilation increases the area by about 35\%.
See the reference page for bwar ea for more information about the weighting pattern.

## Euler Number

The bweul er function returns the Euler number for a binary image. The Euler number is a measure of the topology of an image. It is defined as the total number of objects in the image minus the number of holes in those objects. You can use either 4 - or 8 -connected neighborhoods.

This example computes the Euler number for the circuit image, using 8 -connected neighborhoods.

```
BWL \(=\) imead(' circbw.tif');
eul = bweul er(BV1, 8)
eul =
```

    \(-85\)
    In this example, the Euler number is negative, indicating that the number of holes is greater than the number of objects.

## Lookup Table Operations

Certain binary image operations can be implemented most easily through lookup tables. A lookup table is a column vector in which each element represents the value to return for one possible combination of pixels in a neighborhood.

You can use the makel ut function to create lookup tables for various operations. makel ut creates lookup tables for 2-by-2 and 3-by-3 neighborhoods. This figure illustrates these types of neighborhoods. Each neighborhood pixel is indicated by an $x$, and the center pixel is the one with a circle.


2-by-2 neighborhood


3-by-3 neighborhood

For a 2-by-2 neighborhood, there are 16 possible permutations of the pixels in the neighborhood. Therefore, the lookup table for this operation is a 16-element vector. For a 3-by-3 neighborhood, there are 512 permutations, so the lookup table is a 512-element vector.

Once you create a lookup table, you can use it to perform the desired operation by using the appl yl ut function.

The example below illustrates using lookup-table operations to modify an image containing text. Y ou begin by writing a function that returns 1 if three or more pixels in the 3-by-3 neighborhood are 1, and 0 otherwise. Y ou then call makel ut, passing in this function as the first argument, and using the second argument to specify a 3-by-3 lookup table.

```
f = inline('sum(x(:)) >= 3' );
I ut = nakel ut(f,3);
```

I ut is returned as a 512-element vector of 1's and 0's. E ach value is the output from the function for one of the 512 possible permutations.

You then perform the operation using appl yl ut .

```
BV1 = imead('text.tif');
BVR = appl yl ut(BVI,I ut);
```


## i nshow BKL)

fi gure, i mshow BVZ)


Figure 9-8: Text.tif Before and After Applying a Lookup Table Operation
For information about how appl yl ut maps pixel combinations in the image to entries in the lookup table, see the reference page for appl yl ut.

Note You cannot use makel ut and appl yl ut for neighborhoods of sizes other than 2-by-2 or 3-by-3. These functions support only 2-by-2 and 3-by-3 neighborhoods, because lookup tables are not practical for neighborhoods larger than 3-by-3. For example, a lookup table for a 4-by-4 neighborhood would have 65,536 entries.

## Region-Based Processing

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Filtering a Region ..... 10-7
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## Overview

This chapter describes operations that you can perform on a selected region of an image. It discusses these topics:

- "Specifying a Region of Interest" on page 10-4
- "Filtering a Region" on page 10-7
- "Filling a Region" on page 10-9

For an interactive demonstration of region-based processing, try running roi deno.

## Words You Need to Know

An understanding of the following terms will help you to use this chapter. For more explanation of this tableand otherslikeit, see "Words Y ou Need to K now" in the Preface.

| Words | Definitions |
| :--- | :--- |
| Binary mask | A binary image with the same size as the image you want to <br> process. The mask contains l's for all pixels that are part of <br> the region of interest, and 0's everywhere else. |
| Filling a region | A process that "fills" a region of interest by interpolating the <br> pixel values from the borders of the region. This process can <br> be used to make objects in an image seem to disappear as they <br> are replaced with values that blend in with the background <br> area. |
| Filtering a region | The process of applying a filter to a region of interest. For <br> example, you can apply an intensity adjustment filter to <br> certain regions of an image. |
| Interpolation | The process by which we estimate an image value at a location <br> in between image pixels. |


| Words | Definitions |
| :--- | :--- |
| Masked filtering | An operation that applies filtering only to the regions of <br> interest in an image that are identified by a binary mask. <br> Filtered values are returned for pixels where the binary mask <br> contains 1's; unfiltered values are returned for pixels where <br> the binary mask contains 0's. |
| Region of interest | A portion of an image that you want to filter or perform some <br> other operation on. You define a region of interest by creating <br> a binary mask. There can be more than one region defined in <br> an image. The regions can be "geographic" in nature, such as <br> polygons that encompass contiguous pixels, or they can be <br> defined by a range of intensities. In the latter case, the pixels <br> are not necessarily contiguous. |

## Specifying a Region of Interest

A region of interest is a portion of an image that you want to filter or perform some other operation on. Y ou define a region of interest by creating a binary mask, which is a binary image with the same size as the image you want to process. The mask contains l's for all pixels that are part of the region of interest, and 0's everywhere else.

The following subsections discuss methods for creating binary masks:

- "Selecting a Polygon" on page 10-4
- "Other Selection Methods" on page 10-5 (using any binary mask or the roicol or function)


## Selecting a Polygon

You can use the r oi pol y function to specify a polygonal region of interest. If you call roi pol $y$ with no input arguments, the cursor changes to a cross hair when it is over the image displayed in the current axes. You can then specify the vertices of the polygon by clicking on points in the image with the mouse. When you are done selecting vertices, press Return; r oi pol y returns a binary image of the same size as the input image, containing l's inside the specified polygon, and 0's everywhere else.

The example bel ow illustrates using the interactive syntax of roi pol y to create a binary mask. The border of the selected region in Figure 10-1, which was created using a mouse, is shown in red.

```
I = imread('pout.tif');
i mshow(I)
BW = roi pol y;
```



Figure 10-1: A Polygonal Region of Interest Selected Using roipoly
i nshow BW)


Figure 10-2: A Binary Mask Created for the Region Show n in Figure 10-1.
You can also use roi pol y noninteractively. See the reference page for roi pol y for more information.

## Other Selection Methods

roi pol y provides an easy way to create a binary mask. However, you can use any binary image as a mask, provided that the binary image is the same size as the image being filtered.

F or example, suppose you want to filter the intensity image I , filtering only those pixels whose values are greater than 0.5 . Y ou can create the appropriate mask with this command.

$$
B W=(1>0.5) ;
$$

You can also usether oi col or function to definetheregion of interest based on a color or intensity range. For more information, see the reference page for roi col or .

## Filtering a Region

You can use the roi filt 2 function to process a region of interest. When you call roi filt 2 , you specify an intensity image, a binary mask, and a filter. roifilt 2 filters the input image and returns an image that consists of filtered values for pixels where the binary mask contains 1's, and unfiltered values for pixels where the binary mask contains 0's. This type of operation is called masked filtering.

This example uses themask created in the example in "Sel ecting a Polygon" on page $10-4$ to increase the contrast of the logo on the girl's coat.

```
h = fspeci al('unsharp');
I2 = roifilt2(h,I,BW);
i mshow(I)
figure, i nshow(l 2)
```



Figure 10-3: An Image Before and After Using an Unsharp Filter on the Region of Interest.
roi filt 2 also enables you to specify your own function to operateon the region of interest. In the examplebelow, thei madj ust function is used tolighten parts of an image. The mask in the example is a binary image containing text. The resulting image has the text imprinted on it.

```
BW = imead('text.tif');
| = imead(' camer anmn.tif');
f = i nl i ne('i mmdj ust(x,[],[],0.3)');
I2 = roifilt2(I,BWf);
```

imshow (12)


Figure 10-4: An Image Brightened Using a Binary Mask Containing Text
Note that roifilt 2 is best suited to operations that return data in the same range as in the original image because the output image takes some of its data di rectly from the input image. Certain filtering operations can result in values outside the normal image data range (i.e., $[0,1]$ for images of class doubl e, [ 0,255 ] for images of class ui nt $8,[0,65535]$ for images of class ui nt 16). For more information, see the reference page for roifilt 2.

## Filling a Region

You can usether oi fill function tofill a region of interest, interpolating from the borders of the region. This function is useful for image editing, including removal of extraneous details or artifacts.
roifill performs the fill operation using an interpolation method based on Laplace's equation. This method results in the smoothest possiblefill, given the values on the boundary of the region.

As with roi pol y, you select the region of interest with the mouse. When you completetheselection, roifill returns an image with the selected region filled in.

This example uses roifill to modify thet rees image. The border of the selected region is shown in red on the original image.


Figure 10-5: A Region of Interest Selected for Filling
i mshow (I2)


Figure 10-6: The Region of Interest Show $n$ in Figure 10-5 Has Been Filled

## Color

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## Overview

This chapter describes the tool box functions that help you work with color image data. Note that "col or" includes shades of gray; therefore much of the discussion in this chapter applies to grayscale images as well as color images. The following topics are discussed:

- "Working with Different Screen Bit Depths" on page 11-4
- "Reducing the Number of Colors in an Image" on page 11-6
- "Converting to Other Color Spaces" on page 11-15

For additional information about how MATLAB handles color, see the MATLAB graphics documentation.

## Words You Need to Know

An understanding of the following terms will help you to use this chapter. For more explanation of this table and others likeit, see "Words You Need to Know" in the Preface.

| Words | Definitions |
| :--- | :--- |
| Approximation | The method by which the software chooses replacement col ors in the <br> event that direct matches cannot be found. The methods of <br> approximation discussed in this chapter are col ormap mapping, <br> uniform quantization, and minimum variance quantization. |
| Indexed image | An image whose pixel values are direct indices into an RGB <br> col ormap. In MATLAB, an indexed image is represented by an array <br> of class ui nt 8, ui nt 16, or doubl e. The col ormap is always an m-by-3 <br> array of class doubl e. We often use the variable name X to represent <br> an indexed image in memory, and map to represent the col ormap. |
| Intensity image | An image consisting of intensity (grayscale) values. In MATLAB, <br> intensity images are represented by an array of class ui nt 8, ui nt 16, <br> or doubl e. While intensity images are not stored with colormaps, <br> MATLAB uses a system colormap to display them. We often use the <br> variable name I to represent an intensity image in memory. This <br> term is synonymous with the term "grayscale". |


| Words | Definitions |
| :--- | :--- |
| RGB image | An image in which each pixel is specified by three values - one <br> each for the red, blue, and green components of the pixel's col or. In <br> MATLAB, an RGB image is represented by an m-by-n-by-3 array of <br> class ui nt 8, ui nt 16, or doubl e. We often use the variable name RGB <br> to represent an RGB image in memory. |
| Screen bit depth | The number of bits per screen pixel. |
| Screen color resolution | The number of distinct col ors that can be produced by the screen. |

## Working with Different Screen Bit Depths

Most computer displays use 8, 16, or 24 bits per screen pixel. The number of bits per screen pixel determines the display's screen bit depth. The screen bit depth determines the screen col or resol ution, which is how many distinct col ors the display can produce. Regardless of the number of col ors your system can di splay, MATLAB can store and process images with very high bit depths: $2^{24}$ colors for ui nt 8 RGB images, $2^{48}$ colors for ui nt 16 RGB images, and $2^{159}$ for doubl e RGB images. These images display best on systems with 24 -bit color, but usually look fine on 16 -bit systems as well. This section describes the different screen bit depths and how to determine the screen bit depth of your display.
To determine your system's screen bit depth, enter this command at the MATLAB prompt.

```
get(0, ' ScreenDept h' )
```

MATLAB returns an integer representing the number of bits per screen pixel.
A 24-bit display provides optimal color resolution. It uses 8 bits for each of the three col or components, resulting in 256 (i.e., $2^{8}$ ) levels each of red, green, and blue. This supports $16,777,216$ (i.e., $2^{24}$ ) different col ors. (Of these colors, 256 areshades of gray. Shades of gray occur where $R=G=B$.) The 16 million possible colors supported by 24-bit display can render a life-like image.

16-bit displays also support a large number of colors. They usually use 5 bits for each col or component, resulting in 32 (i.e., $2^{5}$ ) levels each of red, green, and blue. This supports 32,768 (i.e., $2^{15}$ ) distinct colors (of which 32 are shades of gray). Alternatively, the extra bit can be used to increase the number of levels of green displayed. In this case, the number of different colors supported by a 16 -bit display is actually 64,536 (i.e. $2^{16}$ ).

8-bit displays support a more limited number of col ors. An 8-bit display can produce any of the colors available on a 24-bit display, but only 256 distinct col ors can appear at onetime. (There are 256 shades of gray available, but if all 256 shades of gray are used, they take up all of the available color slots.)

> Note It is possible that your system's screen bit depth is 32 bits per pixel. Normally, 32 -bit displays use 24 bits for color information and 8 bits for transparency data (alpha channel). So, although the command, get ( 0 , ' Scr eenDept h ' ) returns the value 32, MATLAB does not currently support transparency data.

Depending on your system, you may be able to choose the screen bit depth you want to use. (Theremay betrade-offs between screen bit depth and screen col or resolution.) In general, 24-bit display mode produces the best results. If you need to use a lower screen bit depth, 16 -bit is generally preferable to 8 -bit. However, keep in mind that a 16-bit display has certain limitations, such as:

- An image may have finer gradations of col or than a 16-bit display can represent. If a color is unavailable, MATLAB uses the closest approximation.
- There are only 32 shades of gray available. If you are working primarily with grayscale images, you may get better display results using 8-bit display mode, which provides up to 256 shades of gray.

The next section shows how to reduce the number of colors used by an image.

## Reducing the Number of Colors in an Image

This section describes how to reduce the number of col ors in an indexed or RGB image. A discussion is also included about dithering, which is used by the tool box's col or-reduction functions (seebelow.) Dithering is used to increase the apparent number of colors in an image.

The table below summarizes the Image Processing Tool box functions for color reduction.

| Function | Purpose |
| :--- | :--- |
| i mapprox | Reduces the number of col ors used by an indexed image, <br> enabling you specify the number of col ors in the new <br> col ormap. |
| rgb2i nd | Converts an RGB image to an indexed image, enabling you <br> to specify the number of colors to store in the new <br> col ormap. |

.On systems with 24-bit color displays, RGB (truecolor) images can display up to $16,777,216$ (i.e., $2^{24}$ ) colors. On systems with lower screen bit depths, RGB images still displays reasonably well, because MATLAB automatically uses col or approximation and dithering if needed.

Indexed images, however, may cause problems if they have a Iarge number of colors. In general, you should limit indexed images to 256 col ors for the following reasons.

- On systems with 8-bit display, indexed images with morethan 256 colors will need to be dithered or mapped and, therefore, may not display well.
- On some platforms, col ormaps cannot exceed 256 entries.
- If an indexed image has more than 256 colors, MATLAB cannot store the image data in a ui nt 8 array, but generally uses an array of class doubl e instead, making the storage size of the image much larger (each pixel uses 64 bits).
- M ost image file formats limit indexed images to 256 colors. If you write an indexed image with more than 256 colors (using i mwrite) to a format that does not support more than 256 colors, you will receive an error.


## Using rgb2ind

rgb2i nd converts an RGB image to an indexed image, reducing the number of col ors in the process. This function provides the following methods for approximating the col ors in the original image:

- Quantization
- Uniform quantization
- Minimum variance quantization
- Colormap mapping

The quality of the resulting image depends on the approximation method you use, the range of colors in the input image, and whether or not you use dithering. Note that different methods work better for different images. See "Dithering" on page 11-13 for a description of dithering and how to enable or disableit.

## Quantization

Reducing the number of colors in an image involves quantization. The function rgb2i nd uses quantization as part of its color reduction algorithm. rgb2i nd supports two quantization methods: uniform quantization and minimum variance quantization.
An important term in discussions of image quantization is RGB color cube, which is used frequently throughout this section. The RGB color cube is a three-dimensional array of all of the colors that are defined for a particular data type. Since RGB images in MATLAB can be of type ui nt 8 , ui nt 16, or doubl e, three possible col or cube definitions exist. For example, if an RGB image is of class ui nt 8,256 values are defined for each color plane (red, blue, and green), and, in total, there will be $2^{24}$ (or $16,777,216$ ) colors defined by the color cube. This color cube is the same for all ui nt 8 RGB images, regardless of which colors they actually use.

The ui nt 8, ui nt 16, and doubl e col or cubes all have the same range of col ors. In other words, the brightest red in an ui nt 8 RGB image displays the same as the brightest red in a doubl e RGB image. The difference is that the doubl e RGB color cube has many more shades of red (and many more shades of all colors). Figure 11-1, below, shows an RGB col or cube for a ui nt 8 image.


Figure 11-1: RGB Color Cube for uint8 Images
Quantization involves dividing the RGB color cube into a number of smaller boxes, and then mapping all colors that fall within each box to the color value at the center of that box.

Uniform quantization and minimum variance quantization differ in the approach used to divide up the RGB col or cube. With uniform quantization, the color cube is cut up into equal-sized boxes (smaller cubes). With minimum variance quantization, the color cube is cut up into boxes (not necessarily cubes) of different sizes; the sizes of the boxes depend on how the colors are distributed in the image.

Uniform Quantization. To perform uniform quantization, call rgb2i nd and specify a tolerance. The tolerance determines the size of the cube-shaped boxes into which the RGB color cube is divided. The allowable range for a tolerance setting is $[0,1]$. F or example, if you specify a tolerance of 0.1 , the edges of the boxes are one-tenth the length of the RGB color cube and the maximum total number of boxes is

$$
n=(\mathrm{fl} \text { oor }(1 / \mathrm{tol})+1)^{\wedge} 3
$$

The commands below perform uniform quantization with a tolerance of 0.1.

```
RGB = imead('fl owers.tif');
[x,m&p] = rgb2i nd(RGB, 0.1);
```

Figure 11-2 illustrates uniform quantization of a ui nt 8 image. For clarity, the figure shows a two-dimensional slice (or col or plane) from the col or cube where Red=0, and Green and Blue range from 0 to 255. The actual pixel values are denoted by the centers of the x's.


Figure 11-2: Uniform Quantization on a Slice of the RGB Color Cube
After the color cube has been divided, all empty boxes are thrown out. Therefore, only one of the boxes in Figure 11-2 is used to produce a col or for the col ormap. As shown earlier, the maximum length of a col ormap created by uniform quantization can be predicted, but the colormap can be smaller than the prediction because rgb2i nd removes any colors that do not appear in the input image.

Minimum Variance Quantization. To perform minimum variance quantization, call rgb2i nd and specify the maximum number of colors in the output image's colormap. The number you specify determines the number of boxes into which the RGB col or cube is divided. These commands use minimum variance quantization to create an indexed image with 185 colors.

```
RGB = imead('fl owers.tif');
```

[ X, n⿴囗十p] = rgb2i nd( RGB, 185) ;

Minimum variance quantization works by associating pixels into groups based on the variance between their pixel values．For example，a set of blue pixel values may be grouped together because none of their values is greater than 5 from the center pixel of the group．

In minimum variance quantization，the boxes that divide the col or cube vary in size，and do not necessarily fill the col or cube．If some areas of the col or cube do not have pixels，there are no boxes in these areas．

While you set the number of boxes，$n$ ，to be used by rgb2i nd，the placement is determined by the algorithm as it analyzes the color data in your image．Once the image is divided into $n$ optimally located boxes，the pixels within each box are mapped to the pixel value at the center of the box，as in uniform quantization．

The resulting colormap usually has the number of entries you specify．This is because the col or cube is divided so that each region contains at least one col or that appears in the input image．If the input image uses fewer col ors than the number you specify，the output col ormap will have fewer than n col ors，and the output image will contain all of the colors of the input image．

Figure 11－3 shows the sametwo－dimensional slice of the col or cube as was used in Figure 11－2（for demonstrating uniform quantization）．Eleven boxes have been created using minimum variance quantization．


Figure 11-3: Minimum Variance Quantization on a Slice of the RGB Color Cube

For a gi ven number of colors, minimum variance quantization produces better results than uniform quantization, because it takes into account the actual data. Minimum variance quantization allocates more of the col ormap entries to colors that appear frequently in the input image. It allocates fewer entries to col ors that appear infrequently. As a result, the accuracy of the col ors is higher than with uniform quantization. For example, if the input image has many shades of green and few shades of red, there will be more greens than reds in the output col ormap. Note that the computation for minimum variance quantization takes longer than that for uniform quantization.

## Colormap Mapping

If you specify an actual colormap to use, rgb2i nd uses colormap mapping (instead of quantization) to find the colors in the specified col ormap that best match the colors in the RGB image. This method is useful if you need to create images that use a fixed col ormap. For example, if you want to display multiple indexed images on an 8-bit display, you can avoid color problems by mapping them all to the same col ormap. Col ormap mapping produces a good approximation if the specified col ormap has similar col ors to those in the RGB image. If the colormap does not have similar colors to those in the RGB image, this method produces poor results.

This example illustrates mapping two images to the same colormap. The col ormap used for the two images is created on the fly using the MATLAB function col or cube, which creates an RGB colormap containing the number of col ors that you specify. (col or cube always creates the same col ormap for a given number of colors.) Because the colormap includes colors all throughout the RGB color cube, the output images can reasonably approximate the input images.

```
RGB1 = imread(' autum.tif');
RGB2 = imread('fl owers.tif');
X1 = rgb2i nd(RGB1,col or cube(128) );
X2 = rgb2i nd(RGB2, col or cube( 128) );
```

Note The function subi mage is also hel pful for displaying multiple indexed images. For more information see "Displaying Multiple Images in the Same Figure" on page 3-22 or the reference page for subi mage.

## Using imapprox

Use i mappr ox when you need to reduce the number of colors in an indexed image. i mappr ox is based on rgb2i nd and uses the same approximation methods. Essentially, i mappr ox first callsi nd2r gb to convert theimageto RGB format, and then calls rgb2i nd to return a new indexed image with fewer colors.

For example, these commands create a version of the trees image with 64 colors, rather than the original 128.

I oad trees
[ Y , newmp] = impprox(X, mp, 64) ;
i ms how (Y, newnap) ;
The quality of the resulting image depends on the approximation method you use, the range of colors in the input image, and whether or not you use dithering. Note that different methods work better for different images. See "Dithering" on page 11-13 for a description of dithering and how to enable or disable it.

## Dithering

When you user gb2i nd or i mappr ox to reduce the number of colors in an image, the resulting image may look inferior to the original, because some of the col ors are lost. rgb2i nd and i mappr ox both perform dithering to increase the apparent number of col ors in the output image. Dithering changes the colors of pixels in a neighborhood so that the average color in each neighborhood approximates the original RGB color.
For an example of how dithering works, consider an image that contains a number of dark pink pixels for which there is no exact match in the colormap. To create the appearance of this shade of pink, the I mage Processing Toolbox selects a combination of col ors from the col ormap, that, taken together as a six-pixel group, approximate the desired shade of pink. From a distance, the pixels appear to be correct shade, but if you look up close at the image, you can see a blend of other shades, perhaps red and pale pink pixels. The commands bel ow load a 24-bit image, and then use rgb2i nd to create two indexed images with just eight colors each.

```
rgb=i mead('lily.tif');
i nshow(rgb);
[ X_no_di ther, map] =rgb2i nd(rgb, 8, ' nodi t her ' );
[ X_di ther, map] = gb2i nd(rgb, 8, ' di ther' ) ;
fi gure, i nshow(X_no_di ther, map);
figure, i nshow(X_dither, map);
```



Figure 11-4: Examples of Color Reduction with and Without Dithering
Notice that the dithered image has a larger number of apparent col ors but is somewhat fuzzy-looking. The image produced without dithering has fewer apparent colors, but an improved spatial resolution when compared to the
dithered image. One risk in doing color reduction without dithering is that the new image my contain false contours (see the rose in the upper-right corner).

## Converting to Other Color Spaces

The I mage Processing Tool box represents col ors as RGB values, either directly (in an RGB image) or indirectly (in an indexed image, where the colormap is stored in RGB format). However, there are other models besides RGB for representing col ors numerically. F or example, a col or can be represented by its hue, saturation, and value components (HSV) instead. The various models for col or data are called color spaces.

The functions in the I mage Processing Toolbox that work with col or assume that images use the RGB col or space. However, thetool box provides support for other col or spaces though a set of conversion functions. Y ou can use these functions to convert between RGB and the following color spaces:

- National Television Systems Committee (NTSC)
- YCbCr
- Hue, saturation, value (HSV)

These section describes these col or spaces and the conversion routines for working with them

- "NTSC Color Space"
- "YCbCr Color Space"
- "HSV Color Space"


## NTSC Color Space

The NTSC col or space is used in televisions in the United States. One of the main advantages of this format is that grayscale information is separated from color data, so the same signal can be used for both color and black and white sets. In the NTSC format, image data consists of three components: Iuminance $(\mathrm{Y})$, hue (I), and saturation $(\mathrm{Q})$. The first component, luminance, represents grayscale information, while the last two components make up chrominance (col or information).

The function rgb2nt sc converts col ormaps or RGB images to the NTSC color space. nt sc $2 r$ gb performs the reverse operation.
For example, these commands convert the fl ower s image to NTSC format.

```
RGB = imead('flowers.tif');
YIQ = rgb2ntsc(RGB);
```

Because luminance is one of the components of the NTSC format, the RGB to NTSC conversion is also useful for isolating the gray level information in an image. In fact, the tool box functions rgb2gray and i nd2gr ay use the rgb2nt sc function to extract the grayscale information from a color image.

For example, these commands are equivalent to calling rgb2gray.

```
YI Q = rgb2nt sc( RGB) ;
I = YIQ :,:,1);
```

Note In YIQ color space, I is one of the two color components, not the grayscale component.

## YCbCr Color Space

The YCbCr color space is widely used for digital video. In this format, luminance information is stored as a single component ( Y ), and chrominance information is stored as two col or-difference components ( Cb and Cr ). Cb represents the difference between the blue component and a reference value. Cr represents the difference between the red component and a reference value.

YCbCr data can be double precision, but the color space is particularly well suited to ui nt 8 data. F or ui nt 8 images, the data range for Y is [16, 235], and the range for Cb and Cr is [16, 240]. YCbCr leaves room at the top and bottom of the full ui nt 8 range so that additional (nonimage) information can be included in a video stream.

Thefunction rgb2ycbcr converts col ormaps or RGB images to the YCbCr color space. ycbcr $2 r$ gb performs the reverse operation.

F or example, these commands convert the fI owers image to YCbCr format.

```
RGB = imead('fl owers.tif');
YCBCR = rgb2ycbcr(RGB);
```


## HSV Color Space

The HSV col or space (hue, saturation, value) is often used by people who are selecting colors (e.g., of paints or inks) from a col or wheel or palette, because it corresponds better to how people experience col or than the RGB col or space
does. The functions rgb2hsv and hsv2rgb convert images between the RGB and HSV color spaces.

As hue varies from 0 to 1.0, the corresponding col ors vary from red, through yellow, green, cyan, blue, and magenta, back to red, so that there are actually red values both at 0 and 1.0. As saturation varies from 0 to 1.0, the corresponding colors (hues) vary from unsaturated (shades of gray) to fully saturated (no white component). As value, or brightness, varies from 0 to 1.0, the corresponding col ors become increasingly brighter.
Figure 11-5 illustrates the HSV col or space.


Figure 11-5: Illustration of the HSV Color Space
The function rgb2hsv converts colormaps or RGB images to the HSV color space. hsv2r gb performs the reverse operation. These commands convert an RGB image to HSV col or space.

```
RGB = imead('flowers.tif');
HSV = rgb2hsv(RGB);
```

F or closer inspection of the HSV color space, the next block of code displays the separate color planes (hue, saturation, and value) of an HSV image.

```
RGB=r eshape( ones( 64, 1) *reshape( j et ( 64) , 1, 192) , [ 64, 64, 3] ) ;
HSV=r gb2hsv( RGB) ;
H=HSV(:, :, 1);
S=HSV(:, :, 2);
V=HSV(:, :, 3);
i nshow(H)
fi gure, i nshow(S);
fi gure, i nshow(V);
fi gure, i n$how( RGB) ;
```



Figure 11-6: The Separated Color Planes of an HSV Image
The images in Figure 11-6 can be scrutinized for a better understanding of how the HSV col or space works. As you can see by looking at the hue plane image, hue values make a nice linear transition from high to low. If you compare the hue plane image against the original image, you can see that shades of deep
blue have the highest values, and shades of deep red have the lowest values. (In actuality, there are values of red on both ends of the hue scale, which you can see if you look back at the model of the HSV col or space in Figure 11-5. To avoid confusion, our sample image uses only the red values from the beginning of the hue range.) Saturation can be thought of as the purity of a color. As the saturation plane image shows, the colors with the highest saturation have the highest values and are represented as white. In the center of the saturation image, notice the various shades of gray. These correspond to a mixture of colors; the cyans, greens, and yellow shades are mixtures of true colors. Value is roughly equivalent to brightness, and you will noticethat thebrightest areas of the value plane image correspond to the brightest colors in the original image.

11 color

Function Reference

This chapter provides detailed descriptions of the functions in the Image Processing Tool box. It begins with a list of functions grouped by subject area and continues with the reference entries in alphabetical order.

## Functions by Category

The tables below list all functions in the Image Processing Tool box, plus a few functions in MATLAB that are especially useful for image processing. All of the functions listed have reference entries in this User's Guide, with the following exceptions:

- M ost MATLAB functions. To see the reference entries for most of the MATLAB functions listed here, see the MATLAB F unction Reference. The MATLAB functions i mread, i mf i nfo, and i mwrite have entries in this reference because they are essential to image file I/O.
- The Image Processing Tool box demo functions and slideshow functions. For information about any of these functions, see "I mage Processing Demos" in the Preface.

| Image Display |  |
| :--- | :--- |
| col or bar | Display col orbar. (This is a MATLAB function. See the <br> online MATLAB Function Reference for its reference page.) |
| get i mage | Get image data from axes |
| i mage | Create and display image object. (This is a MATLAB <br> function. See the online MATLAB Function Reference for <br> its reference page.) |
| i nagesc | Scale data and display as image. (This is a MATLAB <br> function. See the online MATLAB Function Reference for <br> its reference page.) |
| i mmovi e | Make movie from multiframe indexed image |
| i nฐ how | Display image |


| Image Display (Continued) |  |
| :--- | :--- |
| mont age | Display multiple image frames as rectangular montage |
| subi nage | Display multiple images in single figure |
| truesi ze | Adjust display size of image |
| warp | Display image as texture-mapped surface |
| zoom | Zoom in and out of image or 2-D plot. (This is a MATLAB <br> function. See the online MATLAB Function Reference for <br> its reference page.) |

## Image File I/ O

| i mfinfo | Return information about image file. (This is a MATLAB <br> function. See the online MATLAB Function Reference for <br> its reference page.) |
| :---: | :--- |
| i m ead | Read image file. (This is a MATLAB function. See the <br> online MATLAB Function Reference for its reference page.) |
| i murite | Write image file. (This is a MATLAB function. See the <br> online MATLAB Function Reference for its reference page.) |

Geometric Operations

| i morop | Crop image |
| :--- | :--- |
| i mresi ze | Resize image |


| Geometric Operations (Continued) |  |
| :--- | :--- |
| i m ot at e | Rotate image |
| i nt er p2 | 2-D data interpolation. (This is a MATLAB function. See <br> the online MATLAB Function Reference for its reference <br> page.) |
| Pixel Values and Statistics |  |
| cor r2 | Compute 2-D correlation coefficient |
| i meont our | Create contour plot of image data |
| i nf eat ure | Compute feature measurements for image regions |
| i nmi st | Display histogram of image data |
| i mpi xel | Determine pixel color values |
| i mpr of i le | Compute pixel-value cross-sections along line segments |
| mean2 | Compute mean of matrix elements |
| pi xval | Display information about image pixels |
| st d2 | Compute standard deviation of matrix elements |


| Image Analysis |  |
| :--- | :--- |
| edge | Find edges in intensity image |
| qt decomp | Perform quadtree decomposition |
| qt get bl $k$ | Get block values in quadtree decomposition |
| qt set bl $k$ | Set block values in quadtree decomposition |


| Image Enhancement |  |
| :--- | :--- |
| hi st eq | E nhance contrast using histogram equalization |
| i madj ust | Adjust image intensity values or col ormap |
| i moi se | Add noise to an image |
| medf i l t 2 | Perform 2-D median filtering |
| or df i l t 2 | Perform 2-D order-statistic filtering |
| wi ener 2 | Perform 2-D adaptive noise-removal filtering |


| Linear Filtering |  |
| :--- | :--- |
| conv2 | Perform 2-D convolution. (This is a MATLAB function. See <br> the online MATLAB Function Reference for its reference <br> page.) |
| convntx2 | Compute 2-D convolution matrix |
| convn | Perform N-D convolution. (This is a MATLAB function. See <br> the online MATLAB Function Reference for its reference <br> page.) |
| fi I t er 2 | Perform 2-D filtering. (This is a MATLAB function. See the <br> online MATLAB Function Reference for its reference page.) |
| f speci al | Create predefined filters |

## Linear 2-D Filter Design

| freqspace | Determine 2-D frequency response spacing. (This is a <br> MATLAB function. See the online MATLAB Function <br> Reference for its reference page.) |
| :--- | :--- |
| freqz2 | Compute 2-D frequency response |
| f samp2 | Design 2-D FIR filter using frequency sampling |
| ftrans2 | Design 2-D FIR filter using frequency transformation |
| fwi nd1 | Design 2-D FIR filter using 1-D window method |
| fwi nd2 | Design 2-D FIR filter using 2-D window method |


| Image Transforms |  |
| :--- | :--- |
| dct 2 | Compute 2-D discrete cosine transform |
| dct ntx | Compute discrete cosine transform matrix |
| fft 2 | Compute 2-D fast Fourier transform. (This is a MATLAB <br> function. See the online MATLAB Function Reference for <br> its reference page.) |
| fftn | Compute N-D fast Fourier transform. (This is a MATLAB <br> function. See the online MATLAB Function Reference for <br> its reference page.) |
| fftshift | Reverse quadrants of output of FFT. (This is a MATLAB <br> function. See the online MATLAB Function Reference for <br> its reference page.) |
| i dct 2 | Compute 2-D inverse discrete cosine transform |
| ifft 2 | Compute 2-D inverse fast Fourier transform. (This is a <br> MATLAB function. See the online MATLAB Function <br> Reference for its reference page.) |
| ifftn | Compute N-D inverse fast Fourier transform. (This is a <br> MATLAB function. See the online MATLAB Function <br> Reference for its reference page.) |
| ir adon | Compute inverse Radon transform |
| phant om | Generate a head phantom image <br> radon |


| Neighborhood and Block Processing |  |
| :--- | :--- |
| best bl k | Choose block size for block processing |
| bl kproc | Implement distinct block processing for image |
| col 2i m | Rearrange matrix columns into blocks |
| col filt | Perform neighborhood operations using columnwise <br> functions |
| i m2col | Rearrange image blocks into columns |
| nl filter | Perform general sliding-neighborhood operations |


| Binary Image Operations |  |
| :--- | :--- |
| appl yl ut | Perform neighborhood operations using lookup tables |
| bwar ea | Compute area of objects in binary image |
| bweul er | Compute Euler number of binary image |
| buf ill | Fill background regions in binary image |
| bwl abel | Label connected components in binary image |
| bumorph | Perform morphological operations on binary image |


| Binary Image Operations (Continued) |  |
| :--- | :--- |
| bwperi m | Determine perimeter of objects in binary image |
| bwsel ect | Select objects in binary image |
| di l ate | Perform dilation on binary image |
| er ode | Perform erosion on binary image |
| makel ut | Construct lookup table for use with appl yl ut |

## Region-Based Processing

| roi col or | Select region of interest, based on color |
| :--- | :--- |
| roifill | Smoothly interpolate within arbitrary region |
| roifilt2 | Filter a region of interest |
| roi poly | Select polygonal region of interest |

## Colormap Manipulation

| bri ght en | Brighten or darken colormap. (This is a MATLAB function. <br> See the online MATLAB Function Reference for its <br> reference page.) |
| :--- | :--- |
| cmper mut e | Rearrange colors in colormap |


| Colormap Manipulation (Continued) |  |
| :--- | :--- |
| cmuni que | Find unique col ormap col ors and corresponding image |
| col or map | Set or get col or lookup table. (This is a MATLAB function. <br> See the online MATLAB Function Reference for its <br> reference page.) |
| i mapprox | Approximate indexed image by one with fewer col ors |
| rgbpl ot | Plot RGB col ormap components. (This is a MATLAB <br> function. See the online MATLAB F unction Reference for <br> its reference page.) |

Color Space Conversions

| hsv2rgb | Convert HSV values to RGB col or space. (This is a <br> MATLAB function. See the online MATLAB Function <br> Reference for its reference page.) |
| :--- | :--- |
| ntsc2rgb | Convert NTSC values to RGB col or space |
| rgb2hsv | Convert RGB values to HSV col or space. (This is a <br> MATLAB function. See the online MATLAB Function <br> Reference for its reference page.) |
| rgb2nt sc | Convert RGB values to NTSC color space |
| rgb2ycbcr | Convert RGB values to YCbCr col or space |
| ycbcr 2rgb | Convert YCbCr values to RGB color space |


| Image Types and Type Conversions |  |
| :--- | :--- |
| di ther | Convert image using dithering |
| doubl e | Convert data to double precision. (This is a MATLAB <br> function. See the online MATLAB Function Reference for <br> its reference page.) |
| gr ay2i nd | Convert intensity image to indexed image |
| gr aysl i ce | Create indexed image from intensity image by threshol ding |
| i m2bw | Convert image to binary image by thresholding |
| i m2doubl e | Convert image array to double precision |
| i m2ui nt 16 | Convert image array to 16-bit unsigned integers |
| i m2ui nt 8 | Convert image array to 8-bit unsigned integers |
| i nd2gr ay | Convert indexed image to intensity image |
| i nd2rgb | Convert indexed image to RGB image |
| i sbw | Return true for binary image |
| i sgray | Return true for intensity image |
| i si nd | Return true for indexed image |
| i sr gb | Return true for RGB image |


| Image Types and Type Conversions (Continued) |  |
| :--- | :--- |
| mat 2gray | Convert matrix to intensity image |
| rgb2gray | Convert RGB image or col ormap to grayscale |
| rgb2i nd | Convert RGB image to indexed image |
| ui nt 16 | Convert data to unsigned 16-bit integers. (This is a <br> MATLAB function. See the online MATLAB Function <br> Reference for its reference page.) |
| ui nt 8 | Convert data to unsigned 8-bit integers. (This is a <br> MATLAB function. See the online MATLAB Function <br> Reference for its reference page.) |

## Toolbox Preferences

| i pt get pr ef | Get value of Image Processing Tool box preference |
| :--- | :--- |
| i pt set pr ef | Set value of Image Processing Tool box preference |


| Demos |  |
| :--- | :--- |
| dct den® | 2-D DCT image compression demo |
| edgedem | Edge detection demo |
| firden® | 2-D FIR filtering and filter design demo |
| i madj dem® | Intensity adjustment and histogram equalization demo |

## Demos (Continued)

| nrfilt dem | N oise reduction filtering demo |
| :--- | :--- |
| qt demo | Quadtree decomposition demo |
| r oi demo | Region-of-interest processing demo |

## Slide Shows

| i pss001 | Region labeling of steel grains |
| :---: | :--- |
| i pss002 | Feature-based logic |
| i pss003 | Correction of nonuniform illumination |

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| Purpose | Perform neighborhood operations on binary images, using lookup tables |
| :---: | :---: |
| Syntax | A = appl yl ut (BWlut) |
| Description | $\mathrm{A}=\mathrm{appl}$ yl ut (BWI ut ) performs a 2-by-2 or 3-by-3 neighborhood operation on binary image BWby using a lookup table (I ut ). I ut is either a 16-element or 512-element vector returned by makel ut. The vector consists of the output values for all possible 2-by-2 or 3-by-3 neighborhoods. |
|  | The values returned in A depend on the values in I ut. For example, if I ut consists of all 1's and 0's, A will be a binary image. |
| Class Support | BWand I ut can be of class ui nt 8 or doubl e. If the elements of I ut are all integers between 0 and 255 (regardless of the class of $I$ ut), then the class of $A$ is ui nt 8 ; otherwise, the class of $A$ is doubl e. |
| Algorithm | appl yl ut performs a neighborhood operation on a binary image by producing a matrix of indices intol ut, and then replacing the indices with the actual values in I ut. The specific algorithm used depends on whether you use 2-by-2 or 3-by-3 neighborhoods. |
|  | 2-by-2 Neighborhoods |
|  | For 2-by-2 neighborhoods, I engt h (I ut) is 16. There are four pixels in each neighborhood, and two possible states for each pixel, so the total number of permutations is $2^{4}=16$. |
|  | To produce the matrix of indices, appl yl ut convolves the binary image BWwith this matrix. |
|  | $8 \quad 2$ |
|  | 41 |
|  | Theresulting convolution contains integer values in the range [0,15]. appl yl ut uses the central part of the convolution, of the same size as BW and adds 1 to each value to shift the range to [1,16]. It then constructs A by replacing the values in the cells of the index matrix with the values in I ut that the indices point to. |

## 3-by-3 Neighborhoods

For 3-by-3 neighborhoods, I engt h ( I ut) is 512 . There are nine pixels in each neighborhood, and 2 possible states for each pixel, so the total number of permutations is $2^{9}=512$.

To produce the matrix of indices, appl yl ut convolves the binary image BWwith this matrix.

| 256 | 32 | 4 |
| ---: | ---: | ---: |
| 128 | 16 | 2 |
| 64 | 8 | 1 |

The resulting convolution contains integer values in the range [0,511]. appl yl ut uses the central part of the convolution, of the same size as BW and adds 1 to each value to shift the range to [1,512]. It then constructs A by replacing the values in the cells of the index matrix with the values in I ut that the indices point to.

Example
In this example, you perform erosion using a 2-by-2 neighborhood. An output pixel is on only if all four of the input pixel's neighborhood pixels are on.

```
I ut = makel ut('sumbx(:)) = 4',2);
BVL = imead('text.tif');
BVR = appl yl ut(BV1, I ut);
i mshow( BWL)
fi gure, i mshow( BVR)
```



See Also
makel ut

| Purpose | Determine block size for block processing |
| :---: | :---: |
| Syntax | $\begin{aligned} & \text { si } z=\text { best bl } k([\mathrm{mn}], k) \\ & {[\mathrm{mb}, \mathrm{nb}]=\text { bestbl } \mathrm{k}([\mathrm{mn} \mathrm{n}], \mathrm{k})} \end{aligned}$ |
| Description | si $z=$ best bl $k([m n], k)$ returns, for an mby-n image, the optimal block size for block processing. $k$ is a scalar specifying the maximum row and column dimensions for the block; if the argument is omitted, it defaults to 100. si z is a 1-by-2 vector containing the row and column dimensions for the block. <br> [ $\mathrm{nb}, \mathrm{nb}$ ] = best bl $\mathrm{k}([\mathrm{mn}$ ],k) returns the row and column dimensions for the block in nto and nb, respectively. |
| Algorithm | best bl $k$ returns the optimal block size given $m n$, and $k$. The al gorithm for determining siz is: <br> - If mis less than or equal to $k$, return $m$ <br> - If mis greater than $k$, consider all values between $\mathrm{min}(\mathrm{m} / 10, \mathrm{k} / 2)$ and k . Return the value that minimizes the padding required. <br> The same al gorithm is then repeated for $n$. |
| Example | $\begin{aligned} \text { siz } & =\text { best bl } k\left(\left[\begin{array}{ll} 640 & 800 \end{array}\right], 72\right) \\ \text { siz } & = \\ & 64 \end{aligned}$ |
| See Also | bl kproc |

## blkproc

Purpose

## Syntax

Description

Class Support

Implement distinct block processing for an image

```
B = bl kproc(A,[mn],fun)
B = bl kproc(A, [mn],fun, P1, P2,...)
B = bl kproc(A,[mn],[mborder nborder],fun,...)
B = bl kproc(A,'i ndexed',...)
```

$B=b l \operatorname{kproc}(A,[m n], f u n)$ processes the image $A$ by applying the function $f$ un to each distinct mby-n block of A, padding A with zeros if necessary. $f$ un is a function that accepts an mby-n matrix, $x$, and return a matrix, vector, or scalar $y$.

$$
y=f u n(x)
$$

bl kpr oc does not require that $y$ be the same size as $x$. However, $B$ is the same size as $A$ only if $y$ is the same size as $x$.
$B=b l \operatorname{kproc}(A,[m n], f u n, P 1, P 2, \ldots)$ passes the additional parameters P1, P2, ..., to fun.
$B=b l \operatorname{kproc}(A,[m \mathrm{n}],[$ mborder nbor der], fun, ...) defines an overlapping border around the blocks. bl kpr oc extends the original mby-n blocks by nbor der on the top and bottom, and nbor der on the left and right, resulting in blocks of size ( m+2* nbor der ) -by-( n+2* nbor der ). bl kpr oc pads the border with zeros, if necessary, on the edges of A. f un should operate on the extended block.

The line below processes an image matrix as 4-by-6 blocks, each having a row border of 2 and a column border of 3. Because each 4-by-6 block has this 2-by-3 border, f un actually operates on blocks of size 8-by-12.

$$
B=\operatorname{bl} \operatorname{kproc}\left(A,\left[\begin{array}{ll}
4 & 6
\end{array}\right],\left[\begin{array}{ll}
2 & 3
\end{array}\right], f \text { un, } \ldots\right)
$$

$B=b l$ kproc( $A$, ' i ndexed' , . . . ) processes A as an indexed image, padding with zeros if the class of $A$ is ui nt 8 or ui nt 16 , or ones if the class of $A$ is doubl $e$.

The input image A can be of any class supported by $f$ un. The class of $B$ depends on the class of the output from $f$ un.

## Example

fun can be a f unct i on_handl e created using @ This example uses bl kpr oc to compute the 2-D DCT of each 8-by-8 block to the standard deviation of the elements in that block.

```
l = i mmead(' camer amæn.tif');
fun = @dct 2;
J = bl kproc(I,[ % 8],fun);
i magesc(J), col ormap( hot )
```

f un can also be an inline object. This example uses bl kpr oc to set the pixels in each 8 -by- 8 block to the standard deviation of the elements in that block.

```
I = i mead(' al ungrns.tif');
fun = i nl i ne('std2(s)*ones(size(x))');
I 2 = bl kproc(l,[ 8 8],'std2(x)*ones(size(x) )');
i n$how(l)
fi gure, i nshow(l 2,[]);
```



See Also
colfilt, nlfilter,inline

## brighten

## Purpose Brighten or darken a col ormap

| Syntax | brighten( bet a) |
| :---: | :---: |
|  | newmap = brighten( beta) |
|  | newmap = bright en( map, beta) |
|  | brighten( fig , bet a) |

Description bri ght en( bet a) replaces the current colormap with a brighter or darker map that has essentially the same colors. The map is brighter if $0<$ bet $\mathrm{a} \leq 1$ and darker if $-1 \leq$ bet a $<0$.
bri ght en( bet a) followed by bri ght en( -bet a) restores the original map.
newnmp = bri ght en(bet a) returns a brighter or darker version of the current colormap without changing the display.
newmap = bri ght en(map, bet a) returns a brighter or darker version of the specified colormap without changing the display.
bri ghten(fig, beta) brightens all of the objects in the figurefig.
Remarks bright en is a function in MATLAB.
See Also i madj ust, rgbpl ot
col ormap in the MATLAB Function Reference

| Purpose | Compute the area of the objects in a binary image |
| :---: | :---: |
| Syntax | total = bwarea(BW) |
| Description | t ot al = bwar ea(BW) estimates the area of the objects in binary image BW tot al is a scalar whose value corresponds roughly to the total number of on pixels in the image, but may not be exactly the same because different patterns of pixels are weighted differently. |
| Class Support | BWcan be of class ui nt 8 or doubl e. tot al is of class double. |
| Algorithm | bwar ea estimates the area of all of the on pixels in an image by summing the areas of each pixel in the image. The area of an individual pixel is determined by looking at its 2-by-2 neighborhood. There are six different patterns distinguished, each representing a different area: <br> - Patterns with zero on pixels (area $=0$ ) <br> - Patterns with one on pixel (area =1/4) <br> - Patterns with two adjacent on pixels (area $=1 / 2$ ) <br> - Patterns with two diagonal on pixels (area =3/4) <br> - Patterns with three on pixels (area $=7 / 8$ ) <br> - Patterns with all four on pixels (area =1) <br> Keep in mind that each pixel is part of four different 2-by-2 neighborhoods. This means, for example, that a single on pixel surrounded by of $f$ pixels has a total area of 1. |
| Example | This example computes the area in the objects of a 256 -by-256 binary image. <br> BW = imead(' circles.tif'); <br> i nshow BW) ; |



```
bwarea( BW)
ans =
```

15799

## See Also bweul er, bwper im

References [1] Pratt, William K. Digital Image Processing. New York: J ohn Wiley \& Sons, Inc., 1991. p. 634.

## Purpose

## Syntax

Description

## Class Support

Example

Compute the Euler number of a binary image
eul $=$ bweul er $(B W n)$
eul = bweul er (BW n) returns the Euler number for the binary image BW eul is a scalar whose value is the total number of objects in the image minus the total number of holes in those objects. n can have a value of either 4 or 8 , where 4 specifies 4 -connected objects and 8 specifies 8 -connected objects; if the argument is omitted, it defaults to 8 .

BWcan be of class ui nt 8 or double. eul is of class doubl e.
$B W=i m e a d(' c i r c l e s . t i f ') ;$
i mshow BW) ;

bweul er (BW)
ans $=$
-2

Algorithm bweul er computes the Euler number by considering patterns of convexity and concavity in local 2-by-2 neighborhoods. See[2] for a discussion of the algorithm used.

See Also buwor ph, buperim

## bw euler

References [1] Horn, Berthold P. K., Robot Vision. New York: McGraw-Hill, 1986. pp. 73-77.
[2] Pratt, William K. Digital ImageProcessing. New York: J ohn Wiley \& Sons, Inc., 1991. p. 633.

## Purpose

 Fill background regions in a binary image$\begin{array}{ll}\text { Syntax } & B V R=\text { buf } i l l(B V 1, c, r, n) \\ & B V R=\operatorname{buf} i l l(B V 1, n) \\ {[B V R, i d x]=b w f i l l(\ldots)}\end{array}$
BVR $=$ bufill $(x, y, B W$, $x i, y i, n)$
$[x, y, B V Z, i d x, x i, y i]=\operatorname{bwfill}(\ldots)$

BVR = bufill(BV1,' hol es', n)
[BVD, idx] = bufill(BVI,' hol es', n)

## Description

BVR $=$ bufill ( BK1, $\mathrm{c}, \mathrm{r}, \mathrm{n}$ ) performs a flood-fill operation on the input binary image $B V 1$, starting from the pixel ( $r, c$ ). If $r$ and $c$ are equal-length vectors, the fill is performed in parallel from the starting pixels $(r(k), c(k)) . n$ can have a value of either 4 or 8 (the default), where 4 specifies 4 -connected foreground and 8 specifies 8 -connected foreground. The foreground of BVI comprises the on pixels (i.e., having value of 1 ).

BVR = buf ill( BVI, n) displays the image BVI on the screen and lets you select the starting points using the mouse. If you omit BV1, bwf ill operates on the image in the current axes. Use normal button clicks to add points. Press Backspace or Delete to remove the previously selected point. A shift-click, right-dick, or double-dick selects a final point and then starts the fill; pressing Return finishes the selection without adding a point.
[ BUR, idx] = bwfill(...) returns the linear indices of all pixels filled by bufill.

BVR $=$ bufill $(x, y$, BVZ, $x i, y i, n)$ uses the vectors $x$ and $y$ to establish a nondefault spatial coordinate system for BV1. xi and yi are scalars or equal-length vectors that specify locations in this coordinate system.
$[x, y, B V Z, i d x, x i, y i]=$ buf ill(...) returns the XDat a and YDat a in $x$ and $y$; the output image in BVR; linear indices of all filled pixels in idx; and the fill starting points in xi and yi.

BVR = bwfill(BV1, ' hol es', n) fills theholes in the binary image BV1. buf ill automatically determines which pixels are in object holes, and then changes the value of those pixels from 0 to 1 . n defaults to 8 if you omit the argument.

## Remarks

## Class Support

[ $B V R, i d x]=$ bwfill(BV1,' hol es', n) returns the linear indices of all pixels filled in by buf ill.
If buf ill is used with no output arguments, the resulting image is displayed in a new figure.
buf ill differs from many other binary image operations in that it operates on background pixels, rather than foreground pixels. If the foreground is 8 -connected, the background is 4-connected, and vice versa. Note, however, that you specify the connectedness of the foreground when you call bwfill.

The input image BVI can be of class doubl e or ui nt 8. The output image BVR is of class ui nt 8 .

## Example

BWL = [ 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| ---: | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 1 | 1 | 1 | 1 | 1 | 0 | 0 | 0 |
| 1 | 0 | 0 | 0 | 1 | 0 | 1 | 0 |
| 1 | 0 | 0 | 0 | 1 | 1 | 1 | 0 |
| 1 | 1 | 1 | 1 | 0 | 1 | 1 | 1 |
| 1 | 0 | 0 | 1 | 1 | 0 | 1 | 0 |
| 1 | 0 | 0 | 0 | 1 | 0 | 1 | 0 |
| 1 | 0 | 0 | 0 | 1 | 1 | 1 | $0]$ |

BVR $=$ bufill(BVI, 3, 3, 8)
BVD $=$

| 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 1 | 1 | 1 | 1 | 1 | 0 | 0 | 0 |
| 1 | 1 | 1 | 1 | 1 | 0 | 1 | 0 |
| 1 | 1 | 1 | 1 | 1 | 1 | 1 | 0 |
| 1 | 1 | 1 | 1 | 0 | 1 | 1 | 1 |
| 1 | 0 | 0 | 1 | 1 | 0 | 1 | 0 |
| 1 | 0 | 0 | 0 | 1 | 0 | 1 | 0 |
| 1 | 0 | 0 | 0 | 1 | 1 | 1 | 0 |

I = imread(' bl ood1.tif');
$\mathrm{BVB}=-\dot{\mathrm{m}} \mathrm{mbw}(\mathrm{I}) ;$
BWA $=$ bwfill(BVB,' hol es');
i mshow (BVB)
figure, inshow( BWA)


See Also bwsel ect, roifill

Purpose Label connected components in a binary image

| Syntax | $L=$ bw abel $(B W n)$ |
| :--- | :--- |
| $[L$, num $]=b w$ abel $(B W n)$ |  |

Description $\quad L=b W$ abel ( $B W n$ ) returns a matrix $L$, of the same sizeas $B W$ containing labels for the connected objects in BW $n$ can have a value of either 4 or 8 , where 4 specifies 4 -connected objects and 8 specifies 8 -connected objects; if the argument is omitted, it defaults to 8.

The elements of $L$ are integer values greater than or equal to 0 . The pixels labeled 0 are the background. The pixels labeled 1 make up one object, the pixels labeled 2 make up a second object, and so on.
[ L , num] = bW abel ( BW n ) returns in numthe number of connected objects found in BW

Class Support The input image BWcan be of class doubl e or ui nt 8. The output matrix $L$ is of class doubl e.

## Remarks

## Example

You can use the MATLAB fi nd function in conjunction with bw abel to return vectors of indices for the pixels that make up a specific object. For example, to return the coordinates for the pixels in object 2

$$
[r, c]=\text { find( bw abel }(B W=2)
$$

You can display the output matrix as a pseudocolor indexed image. E ach object appears in a different col or, so the objects are easier to distinguish than in the original image. To do this, you must first add 1 to each element in the output matrix, so that the data is in the proper range. Also, it is good idea to use a colormap in which the first few colors are very distinct.

This example illustrates using 4-connected objects. Notice objects 2 and 3; with 8 -connected labeling, bw abel would consider these a single object rather than two separate objects.
$\mathrm{BW}=\left[\begin{array}{rllll}1 & 1 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 1 & 1 & 1 & 0 & 1 \\ 1 & 1 & 1 & 0 & 1 \\ 1 & 1 & 0 & 0 \\ 1 & 1 & 1 & 0 & 0 \\ 1 & 1 & 1 & 0 & 0 \\ 0 & 1 & 0 \\ & & & & \end{array}\right]$

See Also
Reference
bweul er, bwsel ect
[1] Haralick, Robert M., and Linda G. Shapiro. Computer and Robot Vision, Volumel. Addison-Wesley, 1992. pp. 28-48.

## bw morph

Purpose
Syntax

Description

Perform morphological operations on binary images
BVZ $=$ bunor ph(BKL, oper at i on)
$B V \mathbb{R}=$ burror ph(BKL, oper at $i$ on, $n$ )
BVR $=$ bumorph(BV1, oper ati on) applies a specific morphological operation to the binary image BVI.

BUR $=$ bunor ph( BV1, oper at $i$ on, $n$ ) applies the operation $n$ times. $n$ can bel $n f$, in which case the operation is repeated until the image no longer changes.
oper at $i$ on is a string that can have one of the values listed bel ow.

| ' bothat' | ' erode' | ' shrink' |
| :--- | :--- | :--- |
| ' bri dge' | 'fill' | ' skel ' |
| ' cl ean' | ' hbreak' | ' spur' |
| ' cl ose' | ' maj ority' | 'thi cken' |
| ' di ag' | ' open' | 'thi n' |
| ' dil at e' | 'remøve' | ' t ophat ' |

' bot hat ' ("bottom hat") performs binary closure (dilation followed by erosion) and subtracts the original image.
' bri dge' bridges previously unconnected pixels. For example,

| 1 | 0 | 0 |  | 1 | 0 | 0 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 1 | 0 | 1 | becomes | 1 | 1 | 1 |
| 0 | 0 | 1 |  | 0 | 0 | 1 |

' cl ean' removes isolated pixels (individual 1's that are surrounded by 0's), such as the center pixel in this pattern.
$0 \quad 0 \quad 0$
$0 \quad 1 \quad 0$
$0 \quad 0 \quad 0$
' cl ose' performs binary closure (dilation followed by erosion).
' di ag' uses diagonal fill to eliminate 8-connectivity of the background. F or example,

| 0 | 1 | 0 |  | 0 | 1 | 0 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 1 | 0 | 0 | becomes | 1 | 1 | 0 |
| 0 | 0 | 0 |  | 0 | 0 | 0 |

' dil at e' performs dilation using the structuring element ones(3).
' er ode' performs erosion using the structuring element ones(3).
' fill' fills isolated interior pixels (individual 0's that are surrounded by 1's), such as the center pixel in this pattern.

| 1 | 1 | 1 |
| :--- | :--- | :--- |
| 1 | 0 | 1 |
| 1 | 1 | 1 |

' hbr eak' removes H-connected pixels. F or example,

| 1 | 1 | 1 |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 0 | 1 | 0 | becomes | 1 | 1 |
| 1 |  |  |  |  |  |
| 1 | 1 | 1 |  | 1 |  |
| 0 | 0 | 0 |  |  |  |
| 1 | 1 | 1 |  |  |  |

' maj or ity' sets a pixel to 1 if five or more pixels in its 3-by-3 neighborhood are 1 's; otherwise, it sets the pixel to 0.
' open' implements binary opening (erosion followed by dilation).
' remove' removes interior pixels. This option sets a pixel to 0 if all of its 4-connected neighbors are 1, thus leaving only the boundary pixels on.
' shri nk', with $n=1 \mathrm{nf}$, shrinks objects to points. It removes pixels so that objects without holes shrink to a point, and objects with holes shrink to a connected ring halfway between each hole and the outer boundary. This option preserves the Euler number.
' skel ' , with $\mathrm{n}=\mathrm{I} \mathrm{nf}$, removes pixels on the boundaries of objects but does not allow objects to break apart. The pixels remaining make up the image skel eton. This option preserves the Euler number.
' spur ' removes spur pixels. For example,
$0 \quad 0 \quad 0 \quad 0$
$\begin{array}{llll}0 & 0 & 0 & 0\end{array}$
$0 \quad 0 \quad 0 \quad 0$
$0 \quad 0 \quad 0 \quad 0$

| 0 | 0 | 1 | 0 | becomes | 0 | 0 | 0 | 0 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 0 | 1 | 0 | 0 |  | 0 | 1 | 0 | 0 |
| 1 | 1 | 0 | 0 |  | 1 | 1 | 0 | 0 |

' thi cken', with $\mathrm{n}=\mathrm{I} \mathrm{nf}$, thickens objects by adding pixels to the exterior of objects until doing so would result in previously unconnected objects being 8 -connected. This option preserves the Euler number.
' thin', with $n=1 \mathrm{nf}$, thins objects to lines. It removes pixels so that an object without holes shrinkstoa minimally connected stroke, and an object with holes shrinks to a connected ring halfway between each hole and the outer boundary. This option preserves the Euler number.
' tophat ' ('top hat") returns the image minus the binary opening of the image.
Class Support The input image BVI can be of class doubl e or ui nt 8. The output image BVR is of class ui nt 8 .

## Example

```
BW1 = imead('circles.tif');
```

i mshow BKL) ;


BVR $=$ bunor ph( BKL, ' renove' );
BVB $=$ bumor ph(BVI, 'skel',I nf );
i mshow BVR)
figure, inshow (BVB)

## bw morph



See Also bweul er, bwperim di lat e, er ode
References
[1] Haralick, Robert M., and Linda G. Shapiro. Computer and Robot Vision, Volumel. Addison-Wesley, 1992.
[2] Pratt, William K. Digital Image Processing. J ohn Wiley \& Sons, Inc., 1991.

## bw perim

Purpose Determine the perimeter of the objects in a binary image

## Syntax $\quad B V R=$ buperim $\mathrm{BV}, \mathrm{n}$ )

Description

Class Support The input image BVI can be of class double or ui nt 8. The output image BVR is of class ui nt 8 .

## Example

BVR = bwper im(BV1, n) returns a binary image containing only the perimeter pixels of objects in the input image BVI. A pixel is part of the perimeter if its value is 1 and there is at least one zero-valued pixel in its neighborhood. n can have a value of either 4 or 8 , where 4 specifies 4 -connected neighborhoods and 8 specifies 8-connected neighborhoods; if the argument is omitted, it defaults to 4.


See Also

| Purpose | Select objects in a binary image |
| :---: | :---: |
| Syntax | $B W D=$ busel ect ( $B W 1, c, r, n$ ) |
|  | BVR = busel ect (BVI, n) |
|  | [ BVR, idx] = busel ect (...) |
|  | BVR $=$ busel ect ( $\mathrm{x}, \mathrm{y}, \mathrm{BVI}, \mathrm{xi}, \mathrm{yi}, \mathrm{n}$ ) |
|  | [ $x, y, B V L, i d x, x i, y i]=$ busel ect ( $\ldots$ ) |
| Description | $B V D=$ bwsel ect ( $B W 1, c, r, n$ ) returns a binary image containing the objects that overlap the pixel ( $r, c$ ). $r$ and $c$ can be scalars or equal-length vectors. If $r$ and $c$ are vectors, BVR contains the sets of objects overlapping with any of the pixels $(r(k), c(k)) . n$ can have a value of either 4 or 8 (the default), where 4 specifies 4 -connected objects and 8 specifies 8 -connected objects. Objects are connected sets of on pixels (i.e., pixels having a value of 1 ). |
|  | BVD = busel ect ( BVI, n) displays the image BVI on the screen and lets you select the ( $r, c$ ) coordinates using the mouse. If you omit BV1, busel ect operates on the image in the current axes. Use normal button clicks to add points. Pressing Backspace or Delete removes the previously selected point. A shift-click, right-click, or double-click selects the final point; pressing Return finishes the selection without adding a point. |
|  | [ BVR, idx ] = bwsel ect (...) returns the linear indices of the pixels belonging to the selected objects. |
|  | BVD $=$ busel ect $(\mathrm{x}, \mathrm{y}, \mathrm{BVI}, \mathrm{xi}, \mathrm{yi}, \mathrm{n})$ uses the vectors x and y to establish a nondefault spatial coordinate system for BW1. xi and yi are scal ars or equal-length vectors that specify locations in this coordinate system. |
|  | $[\mathrm{x}, \mathrm{y}, \mathrm{BVR}, \mathrm{idx}, \mathrm{xi}, \mathrm{yi}]=$ bwsel ect (. . . ) returns the XDat a and YDat a in x and $y$; the output image in BUR; linear indices of all the pixels bel onging to the selected objects in idx; and the specified spatial coordinates in xi and yi. |
|  | If bwsel ect is called with no output arguments, the resulting image is displayed in a new figure. |
| Example | $\begin{aligned} & \text { BVI = imead('text.tif'); } \\ & c=\left[\begin{array}{lll} 16 & 90 & 144 \end{array}\right] ; \\ & r=[85 \\ & \hline \end{aligned}$ |

## bw select

```
BVD = busel ect(BW1, c, r, 4);
i mshow( BVI)
fi gure, i mshow( BVZ)
```

Cross-Correlation Used To Locate A Known Target in an Image



Class Support The input image BVI can be of class doubl e or ui nt 8. The output image BVR is of class ui nt 8 .

See Also bufill, bw abel, i mpixel, roi poly, roifill

| Purpose | Rearrange the colors in a colormap |
| :---: | :---: |
| Syntax | [ $Y$, newnæp] = cmper mute $(X, n \not a p)$ |
|  | [ $Y$, newnıp] = cmper mute( X , map, i ndex) |
| Description | [ Y, newnmp] $=$ cmper mut $e(X, n \not a p)$ randomly reorders the colors in map to produce a new col ormap newmap. cmper mute also modifies the values in $X$ to maintain correspondence between the indices and the colormap, and returns the result in Y. The image $Y$ and associated col ormap newnmp produce the same image as $X$ and map. |
|  | [ Y , newmp] = cmpermute ( X , map, index) uses an ordering matrix (such as the second output of sort) to define the order of colors in the new colormap. |
| Class Support | The input image $X$ can be of class ui nt 8 or doubl e. $Y$ is returned as an array of the same class as $X$. |
| Example | To order a colormap by luminance, use |
|  | ntsc = rgb2ntsc(mp) ; |
|  | [dum index] = sort(ntsc(:, 1) ) ; |
|  | [ Y, newmap] = cmper mite( X , map, i ndex) ; |
| See Also | randperm sort in the MATLAB Function Reference |


| Purpose | Find unique colormap col ors and the corresponding image |
| :---: | :---: |
| Syntax |  |
|  | $[\mathrm{Y}$, newmap] $=$ cmuni que( RGB ) |
|  | [ $\mathrm{Y}, \mathrm{newrap}$ ] = cmuni que( I ) |
| Description | [ Y , newmap] = cmuni que $(X, n \nsim p)$ returns the indexed image $Y$ and associated colormap neumap that produce the same image as ( $X, n \not a p$ ) but with the smallest possible col ormap. cmuni que removes duplicate rows from the colormap and adjusts the indices in the image matrix accordingly. |
|  | [ Y , newnmp] = cmuni que( RGB) converts the truecol or image RGB to the indexed image $Y$ and its associated col ormap newmap. newmp is the smallest possible col ormap for theimage, containing one entry for each unique col or in RGB. (Note that newrap may be very large, because the number of entries can be as many as the number of pixels in RGB.) |
|  | [ Y , newrmp] = cmuni que(I) converts theintensity image I toan indexed image $Y$ and its associated col ormap neummp. newmap is the smallest possible col ormap for the image, containing one entry for each unique intensity level in I. |
| Class Support | The input image can be of class ui nt 8 , ui nt 16 , or doubl e. The class of the output image $Y$ is ui nt 8 if the length of newmap is less than or equal to 256 . If the length of newrap is greater than $256, Y$ is of class doubl $e$. |
| See Also | gray2i nd, rgb2i nd |


| Purpose | Rearrange matrix columns into blocks |
| :---: | :---: |
| Syntax | $A=\operatorname{col} 2 \mathrm{im}(\mathrm{B},[\mathrm{mn}],[\mathrm{mm} \mathrm{nn}], \mathrm{bl}$ ock_type $)$ |
|  | $A=\operatorname{col} 2 \mathrm{im}(\mathrm{B},[\mathrm{mn}],[\mathrm{mmnn}])$ |
| Description | col 2i mrearranges matrix columns into blocks. bl ock_t ype is a string with one of these values: |
|  | - 'di sti nct' for maby-n distinct blocks |
|  | - 'sl i di ng' for mby-n sliding blocks (default) |
|  |  into a distinct mby-n block to create the matrix A of size mmby-nn. If |
|  | $B=[$ A11( : ) A12(: ) A21(: ) A22(: ) ], where each column has length n*n, then $A=\left[\begin{array}{lll}A 11 & A 12 ; & A 21 \\ A 22\end{array}\right]$ where each $A i j$ is mby-n. |
|  | $A=\operatorname{col} 2 i m(B,[m n],[m m n], ' s l i d i n g ')$ rearranges the row vector $B$ into a matrix of size ( $n m+m+1$ ) -by-( $n n-n+1$ ). B must be a vector of size |
|  | 1-by-( $m m+m+1$ ) *( $n n-n+1$ ). B is usually the result of processing the output of i m2col (. . ., 'sliding') using a column compression function (such as sum). |
|  | $A=\operatorname{col} 2 \mathrm{im}(\mathrm{B},[\mathrm{mm}],[\mathrm{mm} \mathrm{nn}])$ uses the default bl ock_type of 'slidi ng ' . |
| Class Support | $B$ can be of class doubl e or of any integer class. $A$ is of the same class as $B$. |
| See Also | bl kproc, colfilt, im2col, nlfilter |

Purpose Perform neighborhood operations using columnwise functions

```
Syntax \(\quad B=\operatorname{colfilt}\left(A,[m n], b l o c k \_t y p e, f u n\right)\)
\(B=\) colfilt \(\left(A,[m n], b l o c k \_t y p e, f u n, P 1, P 2, \ldots\right)\)
\(B=\) colfilt (A, [mn],[nbl ock nbl ock], bl ock_type, fun,....)
B = colfilt(A,'indexed',...)
```

Description
colfilt processes distinct or sliding blocks as columns. colfilt can perform similar operations to bl kproc and nl filter, but often executes much faster.
$B=\operatorname{col} f i l t\left(A,[m n], b l o c k \_t y p e, f u n\right)$ processes the imageA by rearranging each mby-n block of A into a column of a temporary matrix, and then applying the function fun to this matrix. fun can be a f uncti on_handl e, created using @ or an inline object. col filt zero pads A, if necessary.

Before calling fun, col filt calls im2col to create the temporary matrix. After calling fun, col filt rearranges the columns of the matrix back into mby-n blocks using col 2i m
bl ock_t ype is a string with one of these values:

- ' di stinct' for mby-n distinct blocks
- ' sl i di ng' for mby-n sliding neighborhoods
$B=$ colfilt(A, [mn],' di stinct', fun) rearranges each mby-n distinct block of A into a column in a temporary matrix, and then applies the function $f$ un to this matrix. f un must return a matrix of the same size as the temporary matrix. col filt then rearranges the columns of the matrix returned by fun into mby-n distinct blocks.
$B=\operatorname{colfilt}(A,[m n], ' s l i d i n g ', f u n)$ rearranges each mby-n sliding neighborhood of A into a column in a temporary matrix, and then applies the function $f$ un to this matrix. $f$ un must return a row vector containing a single valuefor each column in thetemporary matrix. (Column compression functions such as sumreturn the appropriate type of output.) col filt then rearranges the vector returned by f un into a matrix of the same size as A.
$B=$ colfilt $(A,[m n]$, bl ock_type, fun, P1, P2, ... ) passes the additional parameters P1, P2, ... to fun. colfilt calls fun using,

$$
y=f u n(x, P 1, P 2, \ldots)
$$

where x is the temporary matrix before processing, and y is the temporary matrix after processing.
$B=$ colfilt (A, [mn],[ mbl ock nbl ock], bl ock_type, fun, ...) processes the matrix A as above, but in blocks of size mbl ock-by-nbl ock to save memory. N ote that using the [ mbl ock nbl ock] argument does not change the result of the operation.
$B=$ colfilt( $A$, 'indexed', ... ) processes $A$ as an indexed image, padding with zeros if the class of $A$ is ui nt 8 or ui nt 16 , or ones if the class of $A$ is doubl e.

## Class Support The input image A can be of any class supported by fun. The class of B depends

 on the class of the output from $f$ un.Example This example sets each output pixel to the mean value of the input pixel's 5-by-5 neighborhood.

```
l = imead('tire.tif')
i mshow(1)
I2 = ui nt 8(colfilt(I,[5 5],'sliding',@nean));
figure, i nshow(l 2)
```

See Also bl kproc, col $2 \mathrm{imim2col}$, nlfilter

## colorbar

Purpose Display a colorbar
Syntax col orbar('vert')
col orbar(' horiz')
col orbar (h)
col or bar
h = col or bar(...)

Description

Remarks
Example
col or bar(' vert' ) appends a vertical col orbar to the current axes, resizing the axes to make room for the col orbar. col or bar works with both two-dimensional and three-dimensional plots.
col or bar(' horiz' ) appends a horizontal col orbar to the current axes.
col or bar (h) places the colorbar in the axes $h$. The col orbar is horizontal if the width of the axes is greater than its height.
col or bar with no arguments adds a new vertical colorbar or updates an existing one.
$\mathrm{h}=\mathrm{col}$ or bar(...) returns a handle to the colorbar axes.
col or bar is a function in MATLAB.
Display a colorbar to view values for a filtered image.
I = imread(' bl ood1.tif');
h = fspecial('log');
I2 = filter2(h,l);
inshow( 2,[],' not ruesize'), col ormp(jet(64)), col orbar


See Also imagesc
Purpose Perform two-dimensional convolution

Syntax $\quad$| $\mathrm{C}=\operatorname{conv} 2(\mathrm{~A}, \mathrm{~B})$ |
| :--- |
| $\mathrm{C}=\operatorname{conv} 2($ hcol, hrow, A$)$ |
| $\mathrm{C}=\operatorname{conv} 2(\ldots$, shape $)$ |

Description

## Class Support

Remarks
Example
$A=\operatorname{magic}(5)$
$A=$

```
\begin{tabular}{rrrrr}
17 & 24 & 1 & 8 & 15 \\
23 & 5 & 7 & 14 & 16 \\
4 & 6 & 13 & 20 & 22 \\
10 & 12 & 19 & 21 & 3 \\
11 & 18 & 25 & 2 & 9
\end{tabular}
B = [1 2 1;0 2 0; 3 1 3]
B =
            1 2 1
            0 2 
            3 1 3
C = conv2(A,B)
C =
\begin{tabular}{rrrrrrr}
17 & 58 & 66 & 34 & 32 & 38 & 15 \\
23 & 85 & 88 & 35 & 67 & 76 & 16 \\
55 & 149 & 117 & 163 & 159 & 135 & 67 \\
79 & 78 & 160 & 161 & 187 & 129 & 51 \\
23 & 82 & 153 & 199 & 205 & 108 & 75 \\
30 & 68 & 135 & 168 & 91 & 84 & 9 \\
33 & 65 & 126 & 85 & 104 & 15 & 27
\end{tabular}
```

See Also
xcorr, xcorr 2 in the Signal Processing Tool box User's Guide conv, deconv in the MATLAB Function Reference

Purpose Compute two-dimensional convolution matrix

Syntax $\quad T=$ convmt $\times 2(H, m n)$<br>$\mathrm{T}=$ convint $\mathrm{x} 2(\mathrm{H},[\mathrm{mn}])$<br>\(\begin{array}{ll}Description \& \begin{array}{l}T=convmt \times 2(H, m n) or T=convit \times 2(H,[m n]) returns the<br>convolution matrix T for the matrix H . If X is an mby-n matrix, then\end{array}<br>\& reshape\left(T^{*} X(:) , si ze(H)+[m n]-1\right) is the same as conv 2(X, H) .\end{array}\)

## Class Support The inputs are all of class doubl e. The output matrix $T$ is of class sparse. The number of nonzero elements in T is no larger than $\operatorname{prod}(\operatorname{size}(H)) * n * n$.

## See Also conv2

convnt x in the Signal Processing Tool box U ser's Guide
Purpose Perform N-dimensional convolution
Syntax $C=\operatorname{convn}(A, B)$
$C=\operatorname{convn}(A, B$, shape $)$
Description $C=\operatorname{convn}(A, B)$ computes the $N$-dimensional convolution of matrices $A$ and $B$.
C $=$ convn( $A, B$, shape) returns a subsection of the $N$-dimensional convolution, as specified by the shape parameter. shape is a string with one of these values:

- ' full' (the default) returns the full convolution.
- ' same' returns the central part of the convolution of the same size as A.
- ' val i d' returns only those parts of the convolution that are computed without zero-padded edges.
Class Support The input matrices A and B can be of class doubl e or of any integer class. The output matrix C is of class doubl e .
Remarks convn is a function in MATLAB.
See Also ..... conv2


## Purpose

## Syntax

Description

Class Support
$A$ and $B$ can be of class doubl $e$ or of any integer class. $r$ is a scalar of class double.

## Algorithm

cor $r 2$ computes the correl ation coefficient using

$$
r=\frac{\sum_{m} \sum_{n}\left(A_{m n}-\bar{A}\right)\left(B_{m n}-\bar{B}\right)}{\sqrt{\left(\sum_{m} \sum_{n}\left(A_{m n}-\bar{A}\right)^{2}\right)\left(\sum_{m} \sum_{n}\left(B_{m n}-\bar{B}\right)^{2}\right)}}
$$

where $\bar{A}=\operatorname{mean} 2(A)$, and $\bar{B}=\operatorname{mean2}(B)$.

## See Also

std2
cor rcoef in the MATLAB Function Reference

Description $\quad B=\operatorname{dct} 2(A)$ returns the two-dimensional discrete cosine transform of $A$. The

## Purpose

Syntax

## Class Support

## Algorithm

Compute two-dimensional discrete cosine transform
$B=\operatorname{dct} 2(A)$
$B=\operatorname{dct} 2(A, m n)$
$B=\operatorname{dct} 2(A,[m n])$ matrix $B$ is the same size as A and contains the discrete cosine transform coefficients $B\left(k_{1}, k_{2}\right)$.
$B=\operatorname{dct} 2(A, m n)$ or $B=\operatorname{dct} 2(A,[m n])$ pads the matrix $A$ with zeros to size mby-n before transforming. If mor $n$ is smaller than the corresponding dimension of $A$, dct 2 truncates $A$.

A can be of class doubl e or of any integer class. The returned matrix B is of class double.

The discrete cosine transform (DCT) is closely rel ated to the discrete F ourier transform. It is a separable, linear transformation; that is, the two-dimensional transform is equivalent to a one-dimensional DCT performed along a single dimension followed by a one-dimensional DCT in the other dimension. The definition of the two-dimensional DCT for an input image A and output image $B$ is

$$
\begin{aligned}
& \text { M-1 N-1 } \\
& B_{p q}=\alpha_{p} \alpha_{q} \sum_{m=0} \sum_{n=0} A_{m n} \cos \frac{\pi(2 m+1) p}{2 M} \cos \frac{\pi(2 n+1) q}{2 N}, \begin{array}{l}
0 \leq p \leq M-1 \\
0 \leq q \leq N-1
\end{array} \\
& \alpha_{p}=\left\{\begin{array}{ll}
1 / \sqrt{M}, & p=0 \\
\sqrt{2 / M}, & 1 \leq p \leq M-1
\end{array} \quad \alpha_{q}= \begin{cases}1 / \sqrt{N}, & q=0 \\
\sqrt{2 / N}, & 1 \leq q \leq N-1\end{cases} \right.
\end{aligned}
$$

where M and N are the row and column size of A , respectively. If you apply the DCT to real data, the result is also real. The DCT tends to concentrate information, making it useful for image compression applications.

This transform can be inverted using i dct 2.

The commands below compute the discrete cosine transform for the aut um image. Notice that most of the energy is in the upper-left corner.

```
RGB = i mead(' aut umm.tif');
| = rgb2gray(RGB);
J = dct2(I);
i mshow(log(abs(J)),[]), col ormap(j et(64)), col or bar
```



Now set values less than magnitude 10 in the DCT matrix to zero, and then reconstruct the image using the inverse DCT function i dct 2.

```
J(abs(J) < 10) = 0;
K = idct 2(J)/ 255;
i mshow( K)
```



## See Also fft2,idct2,ifft2

References [1]J ain, Anil K. Fundamentals of Digital Image Processing. Englewood Cliffs, NJ : Prentice Hall, 1989. pp. 150-153.
[2] Pennebaker, William B., and J oan L. Mitchell. J PEG: Still Image Data Compression Standard. Van Nostrand Reinhold, 1993.
Purpose Compute discrete cosine transform matrix
Syntax ..... $D=\operatorname{dctnt} x(n)$
Description $D=\operatorname{dct} n t x(n)$ returns then-by-n DCT (discrete cosine transform) matrix. $D^{*} A$ is the DCT of the columns of $A$ and $D^{*} A$ is the inverse DCT of the columns of $A$ (when A is n-by-n).
Class Support n is a scalar of class doubl e. Dis returned as a matrix of class doubl e.
Remarks
See Also ..... dct 2

Purpose $\quad$ Perform dilation on a binary image

Syntax<br>Description

Class Support The input image BV1 can be of class doubl e or ui nt 8. The output image BVR is of class ui nt 8 .

Remarks

## Example

BVR = di late( BKI, SE)
$B W R=$ di late( $B W 1, S E$, al g)
$B V R=$ di late( $B W 1, S E, \ldots, n)$
BVR $=$ di $\operatorname{l}$ ate $(B V 1, S E)$ performs dilation on the binary image BV1, using the binary structuring element SE. SE is a matrix containing only 1's and 0's.
$B V R=$ di $I$ ate $(B V 1, S E$, al g) performs dilation using the specified algorithm. al $g$ is a string that can have one of these values:

- 'spati al ' (default) - processes the image in the spatial domain.
- ' $f r$ requency' - processes the image in the frequency domain.

Both algorithms produce the same result, but they make different trade-offs between speed and memory use. The frequency al gorithm is faster for large images and structuring elements than the spatial algorithm, but uses much more memory.
$B V R=$ di I ate( $B V 1, S E, \ldots, n)$ performs the dilation operation $n$ times.

| Class Support | The input image BVI can be of class doubl e or ui nt 8 . The output image BVR is <br> of class ui nt 8. |
| :--- | :--- |
| Remarks | You should use the frequency al gorithm only if you have a large amount of <br> memory on your system. If you use this algorithm with insufficient memory, it <br> may actually be slower than the spatial algorithm, due to virtual memory <br> paging. If the frequency algorithm slows down your system excessively, or if <br> you receive "out of memory" messages, use the spatial algorithm instead. |

```
BV1 = i mread('text.tif');
SE = ones(6, 2);
BVR = di I ate( BVI, SE);
i mshow( BVI)
```

fi gure, imshow BVZ)


See Also bunor ph, er ode
References [1] Gonzalez, Rafael C., and Richard E. Woods. Digital Image Processing. Addison-Wesley, 1992. p. 518.
[2] Haralick, Robert M., and Linda G. Shapiro. Computer and Robot Vision, Volumel. Addison-Wesley, 1992. p. 158.

| Purpose | Convert an image, increasing apparent color resolution by dithering |
| :---: | :---: |
| Syntax | $\mathrm{X}=\mathrm{di} \mathrm{ther}(\mathrm{RGB}, \mathrm{map})$ |
|  | $\mathrm{BW}=\operatorname{dither}(\mathrm{I})$ |
| Description | X = di ther (RGB, map) creates an indexed image approximation of the RGB image in the array RGB by dithering the colors in colormap map. |
|  | $X=$ di ther ( RGB, map, Qm Qe) creates an indexed imagefrom RGB, specifying the parameters Qmand Qe. Qmspecifies the number of quantization bits to use along each color axis for the inverse color map, and Qe specifies the number of quantization bits to use for the color space error calculations. If Qe < Qm dithering cannot be performed and an undithered indexed image is returned in $X$. If you omit these parameters, di ther uses the default values $\mathrm{Qm}=5$, $\mathrm{Qe}=8$. |
|  | BW = dither (I) converts the intensity image in the matrixI to the binary (black and white) image BWby dithering. |
| Class Support | The input image (RGB or I ) can be of class ui nt 8, ui nt 16, or doubl e. All other input arguments must be of class doubl e. The output image ( X or BW ) is of class ui nt 8 if it is a binary image or if it is an indexed image with 256 or fewer col ors; otherwise its class is doubl e. |
| Algorithm | di ther increases the apparent col or resolution of an image by applying Floyd-Steinberg's error diffusion dither algorithm. |
| References | [1] Floyd, R. W. and L. Steinberg. "An Adaptive Algorithm for Spatial Gray Scale," International Symposium Digest of Technical Papers. Society for Information Displays, 1975. p. 36. |
|  | [2] Lim, J ae S. Two-Dimensional Signal and Image Processing. Englewood Cliffs, NJ : Prentice Hall, 1990. pp. 469-476. |
| See Also | rgb2i nd |

## double

| Purpose | Convert data to double precision |
| :---: | :---: |
| Syntax | $B=$ doubl e( $A$ ) |
| Description | $B=$ doubl e(A) creates a double-precision array $B$ from the array $A$. If $A$ is a doubl e array, $B$ is identical to $A$. <br> doubl e is useful if you have a ui nt 8 image array that you want to perform arithmetic operations on, because MATLAB does not support these operations on ui nt 8 data. |
| Remarks | double is a MATLAB built-in function. |
| Example | $\begin{aligned} & A=i \operatorname{mread}(' \text { sat urn.tif'); } \\ & B=\operatorname{sqrt}(\operatorname{double}(A)) ; \end{aligned}$ |
| See Also | i m2doubl e, i m2ui nt 8 , i m2ui nt 16, ui nt 8 |

Purpose Find edges in an intensity image

```
Syntax
BW = edge(I,' prewitt')
BW = edge(I,' prewitt',thresh)
BW = edge(I,' prewitt',thresh, di recti on)
[BWthresh] = edge(I,' prewitt',...)
BW = edge(I,'roberts')
BW = edge(I,'roberts',thresh)
[BWthresh] = edge(I,'roberts',...)
BW = edge(I,'l og')
BW = edge(I,' I og' , t hresh)
BW = edge(I,' l og',thresh, si gma)
[ BW threshol d] = edge(I,'log',...)
BW = edge(I,'zer ocross',thresh, h)
[BWthresh] = edge(I,'zerocross',...)
BW = edge(I,' canny' )
BW = edge(I , ' canny' , thresh)
BW = edge( I , ' canny',thr esh, si gmm)
[ BW threshol d] = edge(I,'canny',...)
```

edge takes an intensity imagel as its input, and returns a binary image BWof the same size as I, with 1's where the function finds edges in I and 0's elsewhere.
edge supports six different edge-finding methods:

- The Sobel method finds edges using the Sobel approximation to the derivative. It returns edges at those points where the gradient of I is maximum.
- The Prewitt method finds edges using the Prewitt approximation to the derivative. It returns edges at those points where the gradient of $I$ is maximum.
- The Roberts method finds edges using the Roberts approximation to the derivative. It returns edges at those points where the gradient of $I$ is maximum.
- The Laplacian of Gaussian method finds edges by looking for zero crossings after filtering I with a Laplacian of Gaussian filter.
- Thezero-cross method finds edges by looking for zero crossings after filtering I with a filter you specify.
- TheCanny method finds edges by looking for local maxima of the gradient of I. The gradient is calculated using the derivative of a Gaussian filter. The method uses two thresholds, to detect strong and weak edges, and includes the weak edges in the output only if they are connected to strong edges. This method is therefore less likely than the others to be "fooled" by noise, and more likely to detect true weak edges.

The parameters you can supply differ depending on the method you specify. If you do not specify a method, edge uses the Sobel method.

## Sobel Method

BW = edge(I , ' sobel ' ) specifies the Sobel method.
BW = edge( $I$, ' sobel ' , thr esh) specifies the sensitivity threshold for the Sobel method. edge ignores all edges that are not stronger than $t$ hr esh. If you do not specify $t$ hr esh, or if $t$ hresh is empty ([ ]), edge chooses the value automatically.

BW = edge(I, ' sobel ' , thr esh, di rect i on) specifies direction of detection for the Sobel method. di recti on is a string specifying whether to look for ' horizontal ' or ' vertical ' edges, or ' both' (the default).
[ BW, thresh] = edge(I,' sobel',$\ldots$ ) returns the threshold value.

## Prewitt Method

BW = edge(I , ' prewitt') specifies the Prewitt method.
BW = edge(I , ' prewi tt' , thresh) specifies the sensitivity threshold for the Prewitt method. edge ignores all edges that are not stronger than $t$ hr esh. If
you do not specify $t$ hr esh, or if $t$ hr esh is empty ([ ]), edge chooses the value automatically.

BW = edge(I, ' prewitt', thresh, di rection) specifies direction of detection for the Prewitt method. di rect i on is a string specifying whether to look for ' horizontal ' or ' vertical' edges, or ' both' (the default).
[BWthresh] = edge(I,' prewitt',...) returns the threshold value.

## Roberts Method

BW = edge( 1 , met hod) specifies the Roberts method.
BW = edge( I , met hod, t hr esh) specifies the sensitivity threshold for the Roberts method. edge ignores all edges that are not stronger than thr esh. If you do not specify $t$ hr esh, or if $t$ hr esh is empty ([ ]), edge chooses the value automatically.
[ BW thresh] = edge(I, met hod, ...) returns the threshold value.

## Laplacian of Gaussian Method

BW = edge( I , ' I og' ) specifies the Laplacian of Gaussian method.
BW = edge( I , ' I og' , thresh) specifies the sensitivity threshold for the Laplacian of Gaussian method. edge ignores all edges that are not stronger than $t$ hr esh. If you do not specify $t$ hr esh, or if $t$ hr esh is empty ([ ] ), edge chooses the value automatically.

BW = edge( I, ' I og' , t hresh, si gna) specifies the Laplacian of Gaussian method, using si gma as the standard deviation of the LoG filter. The default si gma is 2 ; the size of the filter is n-by-n, where $n=$ cei I ( si gma* 3 ) ${ }^{2} 2+1$.
[BWthresh] = edge(I,'Iog',...) returns the threshold value.

## Zero-cross Method

BW = edge(I, 'zer ocross', thr esh, h) specifies the zero-cross method, using the filter h. t hr esh is the sensitivity threshold; if the argument is empty ([ ] ), edge chooses the sensitivity threshold automatically.
[BWthresh] = edge(I,'zerocross', ...) returns the threshold value.

## edge

## Canny Method

BW = edge( I , ' canny' ) specifies the Canny method.
BW = edge(I , ' canny' , thr esh) specifies sensitivity thresholds for the Canny method. $t$ hr esh is a two-element vector in which the first element is the low threshold, and the second element is the high threshold. If you specify a scalar for thr esh, this value is used for the high threshold and $0.4 *$ thr esh is used for the low threshold. If you do not specify $t$ hr esh, or if thresh is empty ([ ]), edge chooses low and high values automatically.

BW = edge( I , ' canny' , thr esh, si gma) specifies the Canny method, using si gnm as the standard deviation of the Gaussian filter. The default si gma is 1 ; the size of the filter is chosen automatically, based on si gnm.
[ BW thresh] = edge(I,' canny', ...) returns the threshold values as a two-element vector.



References [3] Canny, J ohn. "A Computational Approach to E dge Detection," IEEE Transactions on Pattern Analysis and M achinel ntelligence, 1986. Vol. PAMI-8, No. 6, pp. 679-698.
[4] Lim, J ae S. Two-Dimensional Signal and Image Processing. Englewood Cliffs, NJ : Prentice Hall, 1990. pp. 478-488.
[5] Parker, J ames R. Al gorithms for Image Processing and Computer Vision. New York: J ohn Wiley \& Sons, Inc., 1997. pp. 23-29.

## erode

Purpose Perform erosion on a binary image
Syntax
Description

BVR $=\operatorname{erode}(B W 1, S E)$
BVR $=\operatorname{erode}(B V 1, S E, ~ a l ~ g)$
BVR $=\operatorname{erode}(B W 1, S E, \ldots, n)$

Class Support The input image BVI can be of class doubl e or ui nt 8 . The output image BVR is of class ui nt 8 .

Remarks

Example
Description

You should use the frequency algorithm only if you have a large amount of memory on your system. If you use this al gorithm with insufficient memory, it may actually be slower than the spatial algorithm, due to virtual memory paging. If the frequency al gorithm slows down your system excessively, or if you receive "out of memory" messages, use the spatial al gorithm instead.

```
BWL = immead('text.tif');
SE = ones(3,1);
BVR = erode( BVI,SE);
i mshow( BVI)
fi gure, i mshow( BVD)
```



See Also
bwmorph, di I ate

## References

[1] Gonzalez, Rafael C., and Richard E. Woods. Digital Image Processing. Addison-Wesley, 1992. p. 518.
[2] Haralick, Robert M., and Linda G. Shapiro. Computer and Robot Vision, Volumel. Addison-Wesley, 1992. p. 158.

## Purpose <br> Compute two-dimensional fast Fourier transform

Syntax | $B$ | $=f f t 2(A)$ |
| ---: | :--- |
| $B$ | $=f f t 2(A, m n)$ |

Description

Class Support The input matrix A can be of class doubl e or of any integer class. The output matrix $B$ is of class doubl $e$.

Remarks $\quad f f t 2$ is a function in MATLAB.
Example
I oad i malems sat urn2 i nshow sat ur n2)

$B=f f t s h i f t(f f t 2(s a t u r n 2))$;
i mshow log(abs(B) ), [ ], ' not ruesize' ), col ormp( j et (64)), col or bar


## Algorithm

fft $2(A)$ is simply
fft(fft(A).').'
This computes the one-dimensional fft of each column A , then of each row of the result. The time required to compute fft 2 ( A ) depends on the number of prime factors of mand $\mathrm{n} . \mathrm{fft} 2$ is fastest when mand n are powers of 2 .

See Also
dct 2, fftshift,idct 2, ifft 2
$f f t, i f f t$ in the MATLAB Function Reference

## Purpose

Syntax | $B$ | $=f f t n(A)$ |
| ---: | :--- |
| $B$ | $=\operatorname{fftn}(A, s i z)$ |

Description

Class Support The input matrix A can be of class doubl e or of any integer class. The output matrix $B$ is of class doubl $e$.

## Remarks

Algorithm
$f f t n(A)$ is equivalent to:
$\mathrm{B}=\mathrm{A} ;$
for $p=1$ : length(size(A) )
$B=f f t(B,[], p)$;
end
This code computes the one-dimensional fast Fourier transform along each dimension of $A$. Thetime required to computefft $n(A)$ depends strongly on the number of prime factors of the dimensions of $A$. It is fastest when all of the dimensions are powers of 2.

## See Also <br> fft $2, i f f t n$

fft in the MATLAB Function Reference

| Purpose | Shift zero-frequency component of fast F ourier transform to center of spectrum |
| :---: | :---: |
| Syntax | $B=f f t s h i f t(A) ~$ |
| Description | $B=f f t s h i f t(A)$ rearranges the outputs of $f f t, f f t 2$, and $f f t n$ by moving the zero frequency component to the center of the array. |
|  | For vectors, $\mathrm{fftshift}(\mathrm{A})$ swaps the left and right halves of A. F or matrices, $\mathrm{fftshift}(\mathrm{A})$ swaps quadrants one and three of A with quadrants two and four. For higher-dimensional arrays, fft shi $\mathrm{ft}(\mathrm{A})$ swaps "half-spaces" of $A$ along each dimension. |
| Class Support | The input matrix A can be of class doubl e or of any integer class. The output matrix $B$ is of the same class as $A$. |
| Remarks | $f f t s h i f t$ is a function in MATLAB. |
| Example | $\begin{aligned} & B=f f t n(A) ; \\ & C=f f t s h i f t(B) ; \end{aligned}$ |
| See Also | fft2, fftn, ifftshift fft in the MATLAB Function Reference |

## filter2

## Purpose Perform two-dimensional linear filtering

Syntax $\quad$| $B$ | $=$ filter $2(\mathrm{~h}, \mathrm{~A})$ |
| ---: | :--- |
| $B$ | $=$ filter $2(\mathrm{~h}, \mathrm{~A}$, shape $)$ |

Description

Class Support The matrix inputs tofilter 2 can be of class doubl e or of any integer class. The output matrix $B$ is of class doubl $e$.

Remarks
$B=$ filter $2(h, A)$ filters the data in A with the two-dimensional FIR filter in the matrix h . It computes the result, B , using two-dimensional correlation, and returns the central part of the correlation that is the same size as $A$.
$B=$ filter 2(h, A, shape) returns the part of B specified by the shape parameter. shape is a string with one of these values:

- ' ful I' returns the full two-dimensional correlation. In this case, B is larger than A.
- ' same' (the default) returns the central part of the correlation. In this case, $B$ is the same size as $A$.
- ' val i d' returns only those parts of the correlation that are computed without zero-padded edges. In this case, B is smaller than A.

Two-dimensional correlation is equivalent to two-dimensional convolution with the filter matrix rotated 180 degrees. See the Algorithm section for more information about how filter 2 performs linear filtering.
filter 2 is a function in MATLAB.

## Example

| $A=\operatorname{magic}(6)$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{A}=$ |  |  |  |  |  |
| 35 | 1 | 6 | 26 | 19 | 24 |
| 3 | 32 | 7 | 21 | 23 | 25 |
| 31 | 9 | 2 | 22 | 27 | 20 |
| 8 | 28 | 33 | 17 | 10 | 15 |
| 30 | 5 | 34 | 12 | 14 | 16 |
| 4 | 36 | 29 | 13 | 18 | 11 |

12-70

```
h = fspecial('sobel')
h =
        1 2 1
        0 0 0
        -1 -2 -1
B = filter2(h, A,'valid')
B =
\begin{tabular}{rrrr}
-8 & 4 & 4 & -8 \\
-23 & -44 & -5 & 40 \\
-23 & -50 & 1 & 40 \\
-8 & 4 & 4 & -8
\end{tabular}
```


#### Abstract

Algorithm


See Also conv2, roifilt2

## freqspace

Purpose

## Syntax

## Description

Remarks freqspace is a function in MATLAB.
See Also fsamp2, f wi nd1, f wi nd2
meshgrid in the MATLAB Function Reference


## freqz2

## Example

See Also
Use the window method to create a 16-by-16 filter, then view its frequency response using freqz2.

```
Hd = zeros(16,16);
Hd( 5: 12, 5: 12) = 1;
Hd(7: 10, 7: 10) = 0;
h = f wi ndl(Hd, bartl ett(16));
col ormap(j et (64) )
freqz2(h,[32 32]); axis ([-1 1-1 1 0 1])
```


freqz in the Signal Processing Tool box User's Guide

| Purpose | Design two-dimensional FIR filter using frequency sampling |
| :---: | :---: |
| Syntax | $\mathrm{h}=\mathrm{fsamp} 2(\mathrm{Hd})$ |
|  | $\mathrm{h}=\mathrm{fsamp} 2(\mathrm{f} 1, \mathrm{f} 2, \mathrm{Hd},[\mathrm{mm}])$ |
| Description | f samp2 designs two-dimensional FIR filters based on a desired two-dimensional frequency response sampled at points on the Cartesian plane. |
|  | $\mathrm{h}=\mathrm{f} \operatorname{samp2}$ ( Hd) designs a two-dimensional FIR filter with frequency response Hd , and returns the filter coefficients in matrix h . (f samp2 returns h as a computational molecule, which is the appropriate form to use with filter 2.) The filter h has a frequency response that passes through points in Hd. If Hd is mby-n, then $h$ is also mby-n. |
|  | Hd is a matrix containing the desired frequency response sampled at equally spaced points between -1.0 and 1.0 al ong the $x$ and $y$ frequency axes, where 1.0 corresponds to half the sampling frequency, or $\pi$ radians. |
|  | $H_{d}\left(f_{1}, f_{2}\right)=\left.H_{d}\left(\omega_{1}, \omega_{2}\right)\right\|_{\omega_{1}=\pi f_{1}, \omega_{2}=\pi f_{2}}$ |
|  | For accurate results, use frequency points returned by fr eqspace to create Hd . (See the entry for freqspace for more information.) |
|  | $\mathrm{h}=\mathrm{fsamp2}(\mathrm{f} 1, \mathrm{f} 2, \mathrm{Hd},[\mathrm{m} \mathrm{n}]$ ) produces an mby-n FIR filter by matching the filter response at the points in the vectors $f 1$ and $f 2$. The frequency vectors $f 1$ and $f 2$ arein normalized frequency, where 1.0 corresponds to half the sampling frequency, or $\pi$ radians. Theresulting filter fits the desired response as closely as possible in the least squares sense. F or best results, there must be at least $n * n$ desired frequency points. f samp2 issues a warning if you specify fewer than n*n points. |
| Class Support | The input matrix Hd can be of class doubl e or of any integer class. All other inputs to f samp2 must be of class doubl e. All outputs are of class doubl e. |
| Example | Use f samp2 to design an approximately symmetric two-dimensional bandpass filter with passband between 0.1 and 0.5 (normalized frequency, where 1.0 corresponds to half the sampling frequency, or $\pi$ radians): |
|  | 1 Create a matrix Hd that contains the desired bandpass response. Use fr eqspace to create the frequency range vectors f 1 and f 2. |

[f1,f2] = freqspace( 21, ' meshgrid' );
Hd = ones(21);
$r=\operatorname{sqrt}\left(\mathrm{f} 1 . \wedge^{\wedge} 2+\mathrm{f} 2 . \wedge^{\wedge}\right)$;
$\mathrm{Hd}((\mathrm{r}<0.1) \mid(r>0.5))=0$;
col ormap( j et (64) )
mesh(f1,f 2, Hd)


2 Design the filter that passes through this response.
h = fsamp2(Hd);
freqz2(h)


| Algorithm | f samp2 computes the filter $h$ by taking the inverse discrete F ourier transform <br> of the desired frequency response. If the desired frequency response is real and <br> symmetric (zero phase), the resulting filter is also zero phase. |
| :--- | :--- |
| See Also | conv2, filt er 2, freqspace, ftrans $2, \mathrm{f}$ wi nd1, f wi nd2 |
| Reference | [1] Lim, J ae S. Two-Dimensional Signal and ImageProcessing. Englewood <br> Cliffs, NJ : Prentice Hall, 1990. pp. 213-217. |

## fspecial

## Purpose Create predefined filters

Syntax $\quad$| $h$ | $=$ fspecial (type) |
| ---: | :--- |
| $h$ | $=$ fspecial (type, par ameters) |

Description
$h=\mathrm{f}$ speci al (type) creates a two-dimensional filter $h$ of the specified type. (fspeci al returns $h$ as a computational molecule, which is the appropriate form to use with filter 2.) type is a string having one of these values:

- ' gaussi an' for a Gaussian lowpass filter
- ' sobel ' for a Sobel horizontal edge-emphasizing filter
- ' prewi tt' for a Prewitt horizontal edge-emphasizing filter
- 'I apl aci an' for a filter approximating the two-dimensional Laplacian operator
- 'I og' for a Laplacian of Gaussian filter
- ' aver age' for an averaging filter
- ' unshar p' for an unsharp contrast enhancement filter
$\mathrm{h}=\mathrm{f}$ speci al (type, parameters) accepts a filter type plus additional modifying par amet er s particular to the type of filter chosen. If you omit these arguments, f speci al uses default values for the par amet ers.

The following list shows the syntax for each filter type. Where applicable, additional parameters are also shown.

- $\mathrm{h}=\mathrm{f}$ speci al ('gaussi an' , n, si gma) returns a rotationally symmetric Gaussian lowpass filter with standard deviation si gnø (in pixels). n is a 1-by-2 vector specifying the number of rows and columns in $h$. ( $n$ can also be a scalar, in which case h is n-by-n.) If you do not specify the parameters, fspeci al uses the default values of [3 3] for $n$ and 0.5 for si gma.
- $\mathrm{h}=\mathrm{f}$ speci al ('sobel ' ) returns this 3-by-3 horizontal edge-finding and $y$-derivative approximation filter:
[1 21
000
-1-2-1]
To find vertical edges, or for $x$-derivatives, use $\mathrm{h}^{\prime}$.
- $\mathrm{h}=\mathrm{f}$ speci al ('prewitt') returns this 3-by-3 horizontal edge-finding and $y$-derivative approximation filter:
[1 11
000
-1 -1-1]
To find vertical edges, or for $x$-derivatives, use $h^{\prime}$.
- h = fspeci al ('I apl aci an', al pha) returns a 3-by-3 filter approximating the two-dimensional Laplacian operator. The parameter al pha controls the shape of the Laplacian and must be in the range 0 to 1.0 . f speci al uses the default value of 0.2 if you do not specify al pha.
- $\mathrm{h}=\mathrm{f}$ speci al ('log', n , si gma) returns a rotationally symmetric Laplacian of Gaussian filter with standard deviation si gma (in pixels). $n$ is a 1-by-2 vector specifying the number of rows and columns in h . ( n can also be a scalar, in which case h is n-by-n.) If you do not specify the parameters, f speci al uses the default values of [5 5] for $n$ and 0.5 for si gma.
- $\mathrm{h}=\mathrm{f}$ speci al (' aver age' , n) returns an averaging filter. n is a 1-by-2 vector specifying the number of rows and columns in h. (n can also be a scalar, in which case $h$ is $n$-by-n.) If you do not specify $n$, $f$ speci al uses the default value of [3 3].
- h = fspeci al (' unsharp' , al pha) returns a 3-by-3 unsharp contrast enhancement filter. f speci al creates the unsharp filter from the negative of the Laplacian filter with parameter al pha. al pha controls the shape of the Laplacian and must be in the range 0 to 1.0. f speci al uses the default value of 0.2 if you do not specify al pha.

```
Example I = imead('saturn.tif');
    h = fspeci al('unsharp',0.5);
    I2 = filter 2(h, l)/ 255;
    i mshow(I)
    figure, i nshow(I 2)
```



## Algorithms

f speci al creates Gaussian filters using

$$
\begin{aligned}
& \mathrm{h}_{\mathrm{g}}\left(\mathrm{n}_{1}, \mathrm{n}_{2}\right)=\mathrm{e}^{-\left(\mathrm{n}_{1}^{2}+\mathrm{n}_{2}^{2}\right) /\left(2 \sigma^{2}\right)} \\
& \mathrm{h}\left(\mathrm{n}_{1}, \mathrm{n}_{2}\right)=\frac{\mathrm{h}_{\mathrm{g}}\left(\mathrm{n}_{1}, \mathrm{n}_{2}\right)}{\sum_{\mathrm{n}_{1}} \sum_{\mathrm{n}_{2}} \mathrm{~h}_{\mathrm{g}}}
\end{aligned}
$$

f speci al creates Laplacian filters using

$$
\begin{aligned}
& \nabla^{2}=\frac{\partial^{2}}{\partial x^{2}}+\frac{\partial^{2}}{\partial y^{2}} \\
& \nabla^{2} \approx \frac{4}{(\alpha+1)}\left[\begin{array}{ccc}
\frac{\alpha}{4} & \frac{1-\alpha}{4} & \frac{\alpha}{4} \\
\frac{1-\alpha}{4} & -1 & \frac{1-\alpha}{4} \\
\frac{\alpha}{4} & \frac{1-\alpha}{4} & \frac{\alpha}{4}
\end{array}\right]
\end{aligned}
$$

fspeci al creates Laplacian of Gaussian (LoG) filters using

$$
\begin{aligned}
& \mathrm{h}_{\mathrm{g}}\left(\mathrm{n}_{1}, \mathrm{n}_{2}\right)=\mathrm{e}^{-\left(\mathrm{n}_{1}^{2}+\mathrm{n}_{2}^{2}\right) /\left(2 \sigma^{2}\right)} \\
& \mathrm{h}\left(\mathrm{n}_{1}, \mathrm{n}_{2}\right)=\frac{\left(\mathrm{n}_{1}^{2}+\mathrm{n}_{2}^{2}-2 \sigma^{2}\right) \mathrm{h}_{\mathrm{g}}\left(\mathrm{n}_{1}, \mathrm{n}_{2}\right)}{2 \pi \sigma^{6} \sum_{\mathrm{n}_{1}} \sum_{\mathrm{n}_{2}} \mathrm{~h}_{\mathrm{g}}}
\end{aligned}
$$

fspeci al creates averaging filters using

$$
\text { ones( } n(1), n(2)) /(n(1) * n(2))
$$

fspeci al creates unsharp filters using

$$
\frac{1}{(\alpha+1)}\left[\begin{array}{ccc}
-\alpha & \alpha-1 & -\alpha \\
\alpha-1 & \alpha+5 & \alpha-1 \\
-\alpha & \alpha-1 & -\alpha
\end{array}\right]
$$

See Also
conv2, edge, filter 2, f samp2, f wi nd1, f wi nd2
del 2 in the MATLAB Function Reference

## ftrans2

Purpose Design two-dimensional FIR filter using frequency transformation
Syntax
$h=f t r a n s 2(b, t)$
$h=f t r a n s 2(b)$

Description

## Remarks

The transformation below defines the frequency response of the two-dimensional filter returned by ftrans2,

$$
\mathrm{H}\left(\omega_{1}, \omega_{2}\right)=\left.\mathrm{B}(\omega)\right|_{\cos \omega=\mathrm{T}\left(\omega_{1}, \omega_{2}\right)}
$$

where $B(\omega)$ is the Fourier transform of the one-dimensional filter b ,

$$
B(\omega)=\sum_{n=-N}^{N} b(n) e^{-j \omega n}
$$

and $T\left(\omega_{1}, \omega_{2}\right)$ is the Fourier transform of the transformation matrixt.

$$
\mathrm{T}\left(\omega_{1}, \omega_{2}\right)=\sum_{\mathrm{n}_{2}} \sum_{\mathrm{n}_{1}} \mathrm{t}\left(\mathrm{n}_{1}, \mathrm{n}_{2}\right) \mathrm{e}^{-\mathrm{j} \omega_{1} \mathrm{n}_{1}} e^{-\mathrm{j} \omega_{2} \mathrm{n}_{2}}
$$

The returned filter h is the inverse F ourier transform of $H\left(\omega_{1}, \omega_{2}\right)$.

$$
h\left(n_{1}, n_{2}\right)=\frac{1}{(2 \pi)^{2}} \int_{-\pi}^{\pi} \int_{-\pi}^{\pi} H\left(\omega_{1}, \omega_{2}\right) e^{j \omega_{1} n_{1}} e^{j \omega_{2} n_{2}} d \omega_{1} d \omega_{2}
$$

## Example

Useftrans 2 to design an approximately circularly symmetrictwo－dimensional bandpass filter with passband between 0.1 and 0.6 （normalized frequency， where 1.0 corresponds to half the sampling frequency，or $\pi$ radians）：

1 Sinceftrans 2 transforms a one－dimensional FIR filter to create a two－dimensional filter，first design a one－dimensional FIR bandpass filter using the Signal Processing Tool box function remez．
col or n⿴囗十（ $j$ et（64））

［ $\mathrm{H}, \mathrm{w}$ ］＝freqz（ $\mathrm{b}, 1,128$ ，＇whol e＇$)$ ；
pl ot（wpi－1，fftshift（abs（H）））


2 Useftrans2 with the default McClellan transformation to create the desired approximately circularly symmetric filter．
$h=f t r a n s 2(b) ;$
freqz2（h）


| See Also | conv2, filter 2, f samp2, f wi nd1, f wi nd2 |
| :--- | :--- |
| Reference | $[1]$ Lim, J ae S. Two-Dimensional Signal and Image Processing. Englewood |
|  | Cliffs, $\mathrm{NJ}:$ Prentice Hall, 1990. pp. 218-237. |

## Purpose

 Design two-dimensional FIR filter using one-dimensional window methodSyntax

$h=f$ wind1 $(H d$, wi $n)$
$h=f$ wi nd1(Hd, wi n1, wi n2)
$h=f$ wi nd1 (f1, f2, Hd, ...)
Description f wi nd1 designs two-dimensional FIR filters using the window method. f wi nd1 uses a one-dimensional window specification to design a two-dimensional FIR filter based on the desired frequency response Hd. f wi nd1 works with one-dimensional windows only; use f wi nd2 to work with two-dimensional windows.
$h=f$ wi nd1( Hd, wi n) designs a two-dimensional FIR filter $h$ with frequency response Hd . ( f wi nd1 returns h as a computational molecule, which is the appropriate form to use with filter 2.) f wi nd1 uses the one-dimensional window wi $n$ to form an approximately circularly symmetric two-dimensional window using Huang's method. You can specify wi $n$ using windows from the Signal Processing Toolbox, such as boxcar, hamming, hanni ng, bartl ett, bl ackman, kai ser, or chebwi n . If I engt $\mathrm{h}(\mathrm{wi} \mathrm{n}$ ) is n , then h is n -by-n.

Hd is a matrix containing the desired frequency response sampled at equally spaced points between -1.0 and 1.0 (in normalized frequency, where 1.0 corresponds to half the sampling frequency, or $\pi$ radians) al ong the $x$ and $y$ frequency axes. For accurate results, use frequency points returned by fr eqs pace to create Hd . (See the entry for fr eqs pace for more information.)
$h=f$ wi nd1(Hd, wi n1, vi n2) uses the two one-dimensional windows wi n1 and wi n2 to create a separable two-dimensional window. If I ength( win1) is $n$ and I engt $h($ wi $n 2$ ) is $m$ then $h$ is mby- $n$.
$h=f$ wi $\operatorname{nd1}(\mathrm{f} 1, \mathrm{f} 2, \mathrm{Hd}, \ldots$ ) lets you specify the desired frequency response Hd at arbitrary frequencies ( f 1 and f 2 ) along the $x$ and $y$ axes. The frequency vectors $f 1$ and f 2 should be in the range -1.0 to 1.0 , where 1.0 corresponds to half the sampling frequency, or $\pi$ radians. The length of the window(s) controls the size of the resulting filter, as above.

## Class Support

The input matrix Hd can be of class doubl e or of any integer class. All other inputs to $f$ wi nd1 must be of class doubl e. All outputs are of class doubl e.

Use f wi nd1 to design an approximately circularly symmetric two-dimensional bandpass filter with passband between 0.1 and 0.5 (normalized frequency, where 1.0 corresponds to half the sampling frequency, or $\pi$ radians):

1 Create a matrix Hd that contains the desired bandpass response. Use fr eqs pace to create the frequency range vectors f 1 and f 2 .

```
[f1,f2] = freqspace( 21,' meshgrid');
Hd = ones(21);
r = sqrt(f1.^2 + f2. ^2);
Hd((r<0.1)|(r>0.5)) = 0;
col ormap(j et (64))
mesh(f 1, f 2, Hd)
```



2 Design the filter using a one-dimensional Hamming window.

```
h = fui nd1(Hd, hamming(21) );
freqz2(h)
```



Algorithm f wi nd1 takes a one-dimensional window specification and forms an approximately circularly symmetric two-dimensional window using Huang's method,

$$
w\left(n_{1}, n_{2}\right)=\left.w(t)\right|_{t=\sqrt{n_{1}^{2}+n_{2}^{2}}}
$$

where $w(t)$ is the one-dimensional window and $w\left(n_{1}, n_{2}\right)$ is the resulting two-dimensional window.

Given two windows, f wi nd1 forms a separable two-dimensional window.

$$
\mathrm{w}\left(\mathrm{n}_{1}, \mathrm{n}_{2}\right)=\mathrm{w}_{1}\left(\mathrm{n}_{1}\right) \mathrm{w}_{2}\left(\mathrm{n}_{2}\right)
$$

f wi nd1 calls $f$ wi nd2 with Hd and the two-dimensional window. $f$ wi nd2 computes h using an inverse Fourier transform and multiplication by the two-dimensional window.

$$
\begin{aligned}
& h_{d}\left(n_{1}, n_{2}\right)=\frac{1}{(2 \pi)^{2}} \int_{-\pi}^{\pi} \int_{-\pi}^{\pi} H_{d}\left(\omega_{1}, \omega_{2}\right) e^{j \omega_{1} n_{1}} e^{j \omega_{2} n_{2}} d \omega_{1} d \omega_{2} \\
& h\left(n_{1}, n_{2}\right)=h_{d}\left(n_{1}, n_{2}\right) w\left(n_{1}, n_{2}\right)
\end{aligned}
$$

## fwind1

See Also<br>conv2, filter 2, fsamp2, freqspace, ftrans 2 , f wi nd2<br>\section*{Reference}<br>[1] Lim, J ae S. Two-Dimensional Signal and Image Processing. Englewood Cliffs, NJ : Prentice Hall, 1990.

## Purpose

Design two-dimensional FIR filter using two-dimensional window method

Syntax<br>\section*{Description}

## Class Support

The input matrix Hd can be of class doubl e or of any integer class. All other inputs to $f$ wi nd2 must be of class doubl e. All outputs are of class doubl e.

## Example

Use f wi nd2 to design an approximately circularly symmetric two-dimensional bandpass filter with passband between 0.1 and 0.5 (normalized frequency, where 1.0 corresponds to half the sampling frequency, or $\pi$ radians):

1 Create a matrix Hd that contains the desired bandpass response. Use fr eqspace to create the frequency range vectors f 1 and f 2 .

```
[f1,f2] = freqspace( 21,' meshgrid' );
Hd = ones(21);
r = sqrt(f1. ^2 + f 2. ^2);
Hd((r<0.1)|(r>0.5)) = 0;
```



2 Create a two-dimensional Gaussian window using fspeci al.
wi $n=$ fspecial('gaussian', 21, 2);
wi $n=$ win./ max(wi $n(:)) ;$ \% Make the maxi mum wi ndow val ue be 1 . mesh( wi n)


3 Design the filter using the window from step 2.
h = fui nd2( Hd, win); freqz2(h)


Algorithm

See Also
Reference
f wi nd2 computes $h$ using an inverse F ourier transform and multiplication by the two-dimensional window wi $n$.

$$
\begin{aligned}
& h_{d}\left(n_{1}, n_{2}\right)=\frac{1}{(2 \pi)^{2}} \int_{-\pi}^{\pi} \int_{-\pi}^{\pi} H_{d}\left(\omega_{1}, \omega_{2}\right) e^{j \omega_{1} n_{1}} e^{j \omega_{2} n_{2}} d \omega_{1} d \omega_{2} \\
& h\left(n_{1}, n_{2}\right)=h_{d}\left(n_{1}, n_{2}\right) w\left(n_{1}, n_{2}\right)
\end{aligned}
$$

conv2, filter $2, \mathrm{f}$ samp2, freqspace, ftrans 2 , f wi nd1
[1] Lim, J ae S. Two-Dimensional Signal and Image Processing. Englewood Cliffs, NJ : Prentice Hall, 1990. pp. 202-213.

| Purpose | Get image data from axes |
| :---: | :---: |
| Syntax | ```A = geti mage(h) [ x, y,A] = get i mage(h) [..., A, fl ag] = get i mage(h) [...] = geti mage``` |
| Description | A = get inage( $h$ ) returns the first image data contained in the $H$ andle Graphics object h. h can be a figure, axes, image, or texture-mapped surface. A is identical to the image CDat a; it contains the same values and is of the same class (ui nt 8 or doubl e) as the image CDat a. If $h$ is not an image or does not contain an image or texture-mapped surface, A is empty. <br> $[x, y, A]=$ get m mge $(\mathrm{h})$ returns the image XDat a in x and theYDat a in y . XDat a and YDat a are two-element vectors that indicate the range of the $x$-axis and $y$-axis. <br> $[\ldots, \mathrm{A}, \mathrm{fl}$ ag] $=$ get i mage( h$)$ returns an integer flag that indicates the type of image $h$ contains. This table summarizes the possible values for fl ag. |
|  | Flag Type of Image |
|  | $0 \quad$ Not an image; A is returned as an empty matrix |
|  | $1 \quad$ Intensity image with values in standard range ( $[0,1]$ for doubl e arrays, [ 0,255 ] for ui nt 8 arrays, [ 0,65535 ] for ui nt 16 arrays) |
|  | 2 Indexed image |
|  | 3 Intensity data, but not in standard range |
|  | $4 \quad$ RGB image |
|  | [...] = get i mage returns information for the current axes. It is equivalent to [...] = geti mage(gca). |
| Class Support | The output array A is of the same class as the image CDat a. All other inputs and outputs are of class doubl e. |

Example
This example illustrates obtaining the image data from an image displayed directly from a file.
inshow rice.tif
I = geti mage;

## gray2ind

| Purpose | Convert an intensity image to an indexed image |
| :---: | :---: |
| Syntax | $[\mathrm{X}, \mathrm{map}]=\operatorname{gray} 2 \mathrm{ind}(\mathrm{I}, \mathrm{n})$ |
| Description | gr ay2i nd scales, then rounds, an intensity image to produce an equivalent indexed image. |
|  | [ $\mathrm{X}, \mathrm{map}$ ] = gray2ind(I,n) converts the intensity imagel to an indexed image $X$ with colormap $\operatorname{gray}(n)$. If $n$ is omitted, it defaults to 64. |
| Class Support | The input imagel can be of class ui nt 8 , ui nt 16, or doubl e. The class of the output image $X$ is ui nt 8 if the colormap length is less than or equal to 256 . If the col ormap length is greater than $256, \mathrm{X}$ is of class doubl e . |
| See Also | i nd2gr ay |

## Purpose

Syntax

Description

## Class Support

Example

Create indexed image from intensity image, using multilevel thresholding
X = grayslice(I, n)
X = grayslice(I, v)
$X=$ graysl $i \operatorname{ce}(I, n)$ thresholds the intensity imagel using cutoff values $\frac{1}{n}, \frac{2}{n}, \ldots, \frac{n-1}{n}$, returning an indexed image in $x$.
$X=$ graysl ice(I, v), where $v$ is a vector of values between 0 and 1 , thresholds $I$ using the values of $v$, returning an indexed image in $X$.

You can view the thresholded image using i nshow ( X , nap) with a colormap of appropriate length.

The input image I can be of class ui nt 8 , ui nt 16 , or doubl e. Note that the threshold values are al ways between 0 and 1 , even if I is of class ui nt 8 or ui nt 16. In this case, each threshold value is multiplied by 255 or 65535 to determine the actual threshold to use.

The class of the output image $x$ depends on the number of threshold values, as specified by $n$ or I engt $h(v)$. If the number of threshold values is less than 256 , then $X$ is of class ui nt 8 , and the values in $X$ range from 0 to $n$ or I engt $h(v)$. If the number of threshold values is 256 or greater, X is of class doubl e , and the values in X range from 1 to $\mathrm{n}+1$ or I engt $\mathrm{h}(\mathrm{v})+1$.

```
    I = imread(' ngc4024mtif');
    X = graysl i ce(I,16);
i mshow(I)
fi gure, i mshow(X, j et (16) )
```


gray2i ndSyntaxDescription
Purpose

Enhance contrast using histogram equalization

```
J = hi st eq(I, hgram)
J = hi steq(I,n)
[J,T] = hi steq(I,...)
newmap = hi st eq( X, map, hgram)
newmpp = hi st eq( }X,m\not=p
[ newmap, T] = hi steq( X, ...)
```

hi st eq enhances the contrast of images by transforming the values in an intensity image, or the values in the colormap of an indexed image, so that the histogram of the output image approximately matches a specified histogram.

J = hi st eq(I, hgram) transforms the intensity imagel so that the histogram of the output intensity imageJ with I engt h(hgram) bins approximately matches hgram The vector hgr amshould contain integer counts for equally spaced bins with intensity values in the appropriate range: $[0,1]$ for images of class doubl e, $[0,255]$ for images of class ui nt 8 , and [ 0,65535 ] for images of class ui nt 16. hi st eq automatically scales hgramso that sum hgr am $=$ prod(size(I)). The histogram of J will better match hgramwhen I engt h ( hgr am) is much smaller than the number of discrete levels in I.
$\mathrm{J}=$ hi steq(I, n) transforms the intensity imagel, returning inJ an intensity image with $n$ discrete gray levels. A roughly equal number of pixels is mapped to each of then levels inJ, so that the histogram of Jis approximately flat. (The histogram of J is flatter when $n$ is much smaller than the number of discrete levels in I.) The default value for n is 64 .
[J, T] = hi st eq( $\mathrm{I}, \ldots$. . ) returns the gray scale transformation that maps gray levels in the intensity imagel to gray levels in J.
newrap = hi st eq( $X$, map, hgram) transforms the colormap associated with the indexed image $X$ so that the histogram of the gray component of the indexed image ( $X$, neurmp) approximately matches hgr am hi st eq returns the transformed colormap in neumap. I engt h( hgram) must be the same as si ze( map, 1).
newnıp $=$ hi st eq( $X, n \neq p$ ) transforms the values in the colormap so that the histogram of the gray component of the indexed image $X$ is approximately flat. It returns the transformed col ormap in newnap.
[ newmap, T] = hi steq( $\mathrm{X}, \ldots$. . ) returns the grayscale transformation T that maps the gray component of nap to the gray component of newrap.

Class Support For syntaxes that include an intensity imagel as input, I can be of class ui nt 8, ui nt 16 , or doubl e, and the output imageJ has the same class as I. For syntaxes that include an indexed image $X$ as input, $X$ can be of class ui nt 8 or doubl e; the output colormap is always of class doubl e. Also, theoptional output T (the gray level transform) is always of class doubl e.

## Example

Enhance the contrast of an intensity image using histogram equalization.

```
| = immead('tire.tif');
J = hi steq(I);
i mshow I)
figure, inmhow(J)
```



Display the resulting histograms.
i mhi st (I, 64)
figure; i mhi st(J, 64)


## Algorithm

When you supply a desired histogram hgr am hi st eq chooses the grayscale transformation T to minimize

$$
\left|c_{1}(T(k))-c_{0}(k)\right|
$$

where $c_{0}$ is the cumulative histogram of $\mathrm{A}, c_{1}$ is the cumulative sum of hgr amfor all intensities $k$. This minimization is subject to the constraints that $T$ must be monotonic and $c_{1}(T(a))$ cannot overshoot $c_{0}(a)$ by more than half the distance between the histogram counts at $a$. hi st eq uses this transformation to map the gray levels in X (or the colormap) to their new values.

$$
\mathrm{b}=\mathrm{T}(\mathrm{a})
$$

If you do not specify hgram hi steq creates a flat hgram

$$
\text { hgr am = ones( } 1, \mathrm{n}) \text { *prod(si ze( A) ) / n; }
$$

and then applies the previous algorithm.
See Also bri ght en, i madj ust, i mini st

## hsv2rgb

Purpose

| Syntax | rgbn¥p $=$ hsv2rgb(hsvn¥p) |
| :--- | :--- |
|  | $R G B=h s v 2 r g b(H S V)$ |

Description rgbnap = hsv2rgb(hsvmap) converts the HSV values in hsvmap to RGB col or space. hsvmap is an mby-3 matrix that contains hue, saturation, and value components as its three columns, and rgbmap is returned as an mby-3 matrix that represents the same set of colors as red, green, and blue values. Both rgbnmp and hsvmap contain values in the range 0 to 1.0.
RGB $=$ hsv2rgb(HSV) converts the HSV image to the equivalent RGB image. HSV is an mby-n-by-3 image array whose three planes contain the hue, saturation, and value components for the image. RGB is returned as an mby-n-by-3 image array whose three planes contain the red, green, and blue components for the image.

## Class Support Theinput array to hsv2r gb must be of class doubl e. Theoutput array is of class

 doubl e.Remarks hsv2rgb is a function in MATLAB.
See Also rgb2hsv, rgbpl ot
col or map in the MATLAB Function Reference

## Purpose <br> Compute two-dimensional inverse discrete cosine transform

Syntax
$B=i \operatorname{dct} 2(A)$
$B=i \operatorname{dct} 2(A, m n)$
$B=i \operatorname{dct} 2(A,[m n])$
Description $\quad \mathrm{B}=\mathrm{i}$ dct 2( A$)$ returns the two-dimensional inverse discrete cosine transform (DCT) of $A$.
$B=i \operatorname{dct} 2(A, m n)$ or $B=i \operatorname{dct} 2(A,[m n])$ pads $A$ with zeros to size mby-n before transforming. If [ mn ] <si ze( A$)$, i dct 2 crops A before transforming.

For any A, i dct 2( $\operatorname{dct} 2(A)$ ) equals A to within roundoff error.
Class Support The input matrix A can be of class doubl e or of any integer class. The output matrix $B$ is of class doubl $e$.

Algorithm i dct 2 computes the two-dimensional inverse DCT using

$$
\begin{aligned}
& \text { M-1 N-1 } \\
& A_{m n}=\sum_{p=0} \sum_{q=0} \alpha_{p} \alpha_{q} B_{p q} \cos \frac{\pi(2 m+1) p}{2 M} \cos \frac{\pi(2 n+1) q}{2 N}, \quad \begin{array}{l}
0 \leq m \leq M-1 \\
0 \leq n \leq N-1
\end{array} \\
& \alpha_{p}=\left\{\begin{array}{ll}
1 / \sqrt{M}, & p=0 \\
\sqrt{2 / M}, & 1 \leq p \leq M-1
\end{array} \quad \alpha_{q}= \begin{cases}1 / \sqrt{N}, & q=0 \\
\sqrt{2 / N}, & 1 \leq q \leq N-1\end{cases} \right.
\end{aligned}
$$

## See Also <br> $\operatorname{dct} 2, \operatorname{dctntx}, f f t 2, i f f t 2$

References
[1]J ain, Anil K. Fundamentals of Digital Image Processing. Englewood Cliffs, NJ : Prentice Hall, 1989. pp. 150-153.
[2] Pennebaker, William B., and J oan L. Mitchell. J PEG: Still Image Data Compression Standard. New York: Van Nostrand Reinhold, 1993.

Purpose Compute two-dimensional inverse fast F ourier transform

Syntax $\quad$| $B$ | $=i f f t 2(A)$ |
| ---: | :--- |
| $B$ | $=i f f t 2(A, m n)$ |

Description $\quad B=i f f t 2(A)$ returns the two-dimensional inverse fast Fourier transform of matrix $A$. If $A$ is a vector, $B$ has the same orientation as $A$.
$B=i f f t(A, m n)$ pads matrix $A$ with zeros to size mby-n. If [mn] <size(A), ifft 2 crops A before transforming.

For any $A$, $i f f t 2(f f t 2(A))$ equals $A$ to within roundoff error. If $A$ is real, ifft2(fft2(A)) may have small imaginary parts.

Class Support The input matrix A can be of class double or of any integer class. The output matrix $B$ is of class doubl $e$.

Remarks ifft2 is a function in MATLAB.
Algorithm The algorithm for $\mathrm{ifft2}(\mathrm{~A})$ is the same as the algorithm for $\mathrm{fft} 2(\mathrm{~A})$, except for a sign change and scale factors of $[\mathrm{m}, \mathrm{n}]=\operatorname{size}(\mathrm{A})$. Likefft 2 , the execution time is fastest when mand $n$ are powers of 2 and slowest when they are large prime numbers.

## See Also

dft ntx, filter, freqz, specpl ot, spectrumin the Signal Processing Tool box User's Guide
$f f t, i f f t$ in the MATLAB Function Reference

| Purpose | Compute N -dimensional inverse fast Fourier transform |
| :---: | :---: |
| Syntax | $B=i f f t n(A)$ |
|  | $B=i f f t n(A, s i z)$ |
| Description | $B=i f f t n(A)$ performs the $N$-dimensional inversefast Fourier transform. The result $B$ is the same size as $A$. |
|  | $B=i f f t n(A, s i z)$ pads $A$ with zeros (or truncates $A$ ) to create an N -dimensional array of size si z before doing the inverse transform. |
|  | For any $A, i f f t n(f f t n(A))$ equals A within roundoff error. If A is real, ifftn(fftn(A)) may have small imaginary parts. |
| Class Support | The input matrix A can be of class doubl e or of any integer class. The output matrix $B$ is of class doubl e. |
| Remarks | ifft n is a function in MATLAB. |
| Algorithm | ifftn(A) is equivalent to |
|  | $B=A ;$ |
|  | for $p=1$ : length(size(A)) |
|  | end |
|  | This code computes the one-dimensional inverse fast Fourier transform along each dimension of $A$. The time required to computei $f f t n(A)$ depends most on the number of prime factors of the dimensions of $A$. It is fastest when all of the dimensions are powers of 2 . |
| See Also | $\mathrm{fft} 2, \mathrm{fftn}, \mathrm{ifft} 2$ |

Purpose

Syntax<br>Description

Class Support The input image can be of class ui nt 8, ui nt 16, or doubl e. The output image BW is of class ui nt 8 .

## Example

I oad trees
$B W=i \operatorname{m2bw}(X, \operatorname{map}, 0.4)$;
i nshow ( $X$, map)
figure, imshow BW)

i nd2gray, rgb2gray

| Purpose | Rearrange image blocks into columns |
| :---: | :---: |
| Syntax | $\begin{aligned} & B=i m 2 \operatorname{col}(A,[m n], \text { bl ock_type }) \\ & B=i m 2 \operatorname{col}(A,[m n]) \\ & B=i m 2 \operatorname{col}\left(A, \text { ' }^{2} \text { ndexed' }, \ldots\right) \end{aligned}$ |
| Description | $B=i \operatorname{m2col}\left(A,[m n], b l o c k \_t y p e\right)$ rearranges image blocks into columns. bl ock_t ype is a string that can have one of these values: <br> - ' di stinct' for mby-n distinct blocks <br> - 'sl i di ng' for mby-n sliding blocks (default) <br> $B=i m 2 c o l(A,[m n], ~ d i s t i n c t ')$ rearranges each distinct mby-n block in the image A into a column of B. i m2col pads A with zeros, if necessary, so its size is an integer multiple of mby-n. If $A=\left[\begin{array}{lll}\text { A11 A12; A21 A22] , where each } A_{i j}\end{array}\right.$ is mby-n, then $B=[$ A11(:) A12(:) A21(:) A22(:)]. <br> $B=i m 2 c o l(A,[m n], ' s l i d i n g ')$ converts each sliding mby-n block of Ainto a column of $B$, with no zero padding. B has n*n rows and will contain as many columns as there are mby-n neighborhoods of $A$. If the size of $A$ is [ mm nn ], then the size of $B$ is $(n * n)$-by- $((m+m+1) *(n n-n+1))$. <br> $B=i m 2 c o l(A,[m n])$ uses the default bl ock_type of 'sliding'. <br> For the sliding block case, each column of B contains the neighborhoods of A reshaped as nhood( : ) where nhood is a matrix containing an mby-n <br> neighborhood of A. i m2col orders the columns of B so that they can be reshaped to form a matrix in the normal way. F or example, suppose you use a function, such as sum( $B$ ), that returns a scalar for each column of B. You can directly store the result in a matrix of size ( $n m+m+1$ )-by-(nn-n+1), using these calls. $\begin{aligned} & B=i \operatorname{m2col}(A,[m n], ' s l i d i n g ') ; \\ & C=r \operatorname{eshape}(\operatorname{sum}(B), n m+m+1, n n-n+1) ; \end{aligned}$ <br> $B=i \mathrm{~m} 2 \mathrm{col}(\mathrm{A}, \mathrm{i}$ indexed' , . . .) processes A as an indexed image, padding with zeros if the class of $A$ is ui nt 8 , or ones if the class of $A$ is doubl $e$. |
| Class Support | The input image A can be of class doubl e or of any integer class. The output matrix $B$ is of the same class as the input image. |
| See Also | bl kproc, col 2 imecolfilt, nlfilter |

## im2double

## Purpose <br> Convert image array to double precision

Syntax<br>Description

See Also

I 2 = i m2doubl e(I 1)
RGB2 $=\mathrm{i}$ m2doubl e(RGB1)
BUR $=\mathrm{i}$ m2doubl e( BVI)
X2 = i m2doubl e( X1, 'i ndexed' )
i m2doubl e takes an image as input, and returns an image of class doubl e. If the input image is of class doubl e, the output image is identical to it. If the input image is of class ui nt 8 or ui nt 16, i m2doubl e returns the equivalent image of class doubl e, rescaling or offsetting the data as necessary.

I 2 = i m2doubl e(I 1) converts the intensity image I 1 to double precision, rescaling the data if necessary.

RGB2 $=$ i m2doubl e( RGB1) converts the truecol or image RGB1 to double precision, rescaling the data if necessary.

BVR $=\mathrm{i}$ m2doubl e( BVI) converts the binary image BVI to double precision.
X2 = i m2doubl e( X1, 'i ndexed' ) converts the indexed image X1 to double precision, offsetting the data if necessary.
doubl e, i mqui nt 8, ui nt 8
Purpose Convert image array to eight-bit unsigned integers
Syntax

I 2 = i m2ui nt 8(I 1)
RGB2 = i m2ui nt 8( RGB1)
BVR $=i$ m2ui nt 8( BVI)
X2 = i m2ui nt 8( X1, ' i ndexed' )
Description
See Also im2ui nt 16, doubl e, i m2doubl e, ui nt 8, i mapprox, ui nt 16

## im2uint16

| Purpose | Convert image array to sixteen-bit unsigned integers |
| :---: | :---: |
| Syntax | $12=\mathrm{im}$ 2ui nt 16(1) |
|  | RGB2 = i m2ui nt 16(RGB1) |
|  | X2 = i m2ui nt 16( X1, ' i ndexed' ) |
| Description | i m2ui nt 16 takes an image as input, and returns an image of class ui nt 16. If the input image is of class ui nt 16 , the output image is identical to it. If the input image is of class doubl e or ui nt 8 , i m2ui nt 16 returns the equivalent image of class ui nt 16 , rescaling or offsetting the data as necessary. |
|  | । 2 = i m2ui nt 16(I 1) converts the intensity image I 1 to ui nt 16 , rescaling the data if necessary. |
|  | RGB2 $=$ i m2ui nt 16( RGB1) converts the truecol or image RGB1 to ui nt 16, rescaling the data if necessary. |
|  | X2 = i mpui nt 16( X1, ' i ndexed' ) converts the indexed image X1 to ui nt 16, offsetting the data if necessary. Note that it is not always possible to convert an indexed image to ui nt 16 . If X 1 is of class doubl e, $\max (\mathrm{X} 1(:)$ ) must be 65536 or less. |

Note i m2ui nt 16 does not support binary images.

See Also im2ui nt 8, doubl e, i m2doubl e, ui nt 8, ui nt 16, i mapprox

| Purpose | Adjust image intensity values or colormap |
| :---: | :---: |
| Syntax | ```J = immdjust(I,[low_in hi gh_i n],[low_out hi gh_out],ganmm) newmap = i m@dj ust(map,[l ow_in hi gh_i n],[l ow_out hi gh_out ], gamm) RGB2 = i madj ust(RGB1, ...)``` |
| Description | J = i madj ust (I, [ I ow_in hi gh_i n], [low_out hi gh_out ], ganmm) maps the values in intensity imagel to new values inJ such that values between I ow in and hi gh_i n map to values between I ow out and hi gh_out. Values below I ow_i n and above hi gh_i $n$ are clipped; that is, values below I ow_in map to I ow_out, and those above hi gh_i n map to hi gh_out. You can use an empty matrix ([ ]) for [I ow_i $n$ hi gh_i n] or for [I ow_out hi gh_out ] to specify the default of [ 0 1]. ganma specifies the shape of the curve describing the relationship between the values in I and J. If gamma is less than 1, the mapping is weighted toward higher (brighter) output values. If gamma is greater than 1 , the mapping is weighted toward lower (darker) output values. If you omit the argument, gamm defaults to 1 (linear mapping). <br> newrap = i madj ust (map, [low_in; hi gh_i n],[Iow_out; hi gh_out], gamma) transforms the colormap associated with an indexed image. IfI ow_in, hi gh_i n, I ow_out, hi gh_out, and ganma are scalars, then the same mapping applies to red, green and blue components. Unique mappings for each color component are possible when: I ow_i n and hi gh_i $n$ are both 1-by-3 vectors, I ow_out and hi gh_out are both 1-by-3 vectors, or gamma is a 1-by-3 vector. The rescaled colormap, newnap, is the same size as nap. |
|  | RGB2 = i madj ust (RGB1, . . . ) performs the adjustment on each image plane (red, green, and blue) of the RGB image RGB1. As with the col ormap adjustment, you can apply unique mappings to each plane. |

Note If hi gh_out < I ow_out, the output image is reversed, as in a photographic negative.

[^4]
## imadjust

Example

$$
\begin{aligned}
& \text { I = imread(' pout.tif'); } \\
& \text { J = i madjust(I,[0.3 0.7],[]); } \\
& \text { inshow(l), figure, inshow() }
\end{aligned}
$$



RGB1 = imead('flowers.tif');
RGB2 = i madj ust(RGB1,[.2 . 3 0; . 6 . 7 1],[]);
i mshow RGB1), fi gure, i mshow( RGB2)


See Also
bri ghten, hi steq

| Purpose | Approximate indexed image by one with fewer colors |
| :---: | :---: |
| Syntax |  |
| Description | [ Y , newñp] = i mゅpprox( $\mathrm{X}, \mathrm{n} \not \mathrm{p}, \mathrm{n}$ ) approximates the colors in the indexed image $X$ and associated colormap map by using minimum variance quantization. i mappr ox returns indexed image $Y$ with col ormap newnap, which has at most n colors. <br>  through uniform quantization. newnap contains at most ( fl oor ( $1 / \mathrm{tol}$ ) +1) ^3 colors. tol must be between 0 and 1.0. <br> Y = i mapprox ( X , map, newmp) approximates the colors in map by using col ormap mapping to find the col ors in newmap that best match the col ors in map. <br> $Y=$ i mapprox(. . . , di ther_opti on) enables or disables dithering. di $t$ her_opt i on is a string that can have one of these values: <br> - ' di ther ' dithers, if necessary, to achieve better col or resolution at the expense of spatial resolution (default). <br> - ' nodi ther' maps each color in the original image to the closest color in the new map. No dithering is performed. |
| Class Support | The input image $X$ can be of class ui nt 8 , ui nt 16 , or doubl e. The output image $Y$ is of class ui nt 8 if the length of newnmp is less than or equal to 256 . If the length of newmap is greater than $256, X$ is of class doubl e. |
| Algorithm | i mappr ox uses rgb2i nd to create a new colormap that uses fewer colors. |
| See Also | cmuni que, di ther, rgb2i nd |

Purpose

Syntax<br>Description

Class Support The input image can be of class ui nt 8, ui nt 16, or doubl e.

## Example

Create a contour plot of image data

```
i meont our(I, n)
i moont our(I,v)
i moont our ( x, y, ...)
i mcont our(..., Li neSpec)
[C, h] = imcontour(...)
```

i meont our (I, n) draws a contour plot of the intensity image I, automatically setting up the axes so their orientation and aspect ratio match the image. $n$ is the number of equally spaced contour levels in the plot; if you omit the argument, the number of levels and the values of the levels are chosen automatically.
i moont our (I, v) draws a contour plot of I with contour lines at the data values specified in vector $v$. The number of contour levels is equal to l engt $h(v)$.
i ncont our ( $x, y, \ldots$ ) uses the vectors $x$ and $y$ to specify the $x$ - and $y$-axis limits.
i meont our ( . . . , Li neSpec) draws the contours using the line type and col or specified by Li neSpec. Marker symbols are ignored.
[ C, h] = i moont our (. . . ) returns the contour matrix C and a vector of handles to the objects in the plot. (The objects are actually patches, and the lines are the edges of the patches.) You can use the cl abel function with the contour matrix $C$ to add contour labels to the plot.

```
| = immead('ic.tif');
i meont our(I, 3)
```



See Also cl abel, cont our, Li neSpec in the MATLAB Function Reference

## imcrop

## Purpose Crop an image

## Syntax

```
I2 = imerop(I)
X2 = i merop(X, map)
RGB2 = imerop( RGB)
I2 = imerop(I,rect)
X2 = imerop(X, m@p,rect)
RGB2 = imerop( RGB, rect)
[...] = imerop(x,y,...)
[A, rect] = imerop(...)
[x,y,A,rect] = imerop(...)
```


## Description

i merop crops an image to a specified rectangle. In the syntaxes below, i mer op displays the input image and waits for you to specify the crop rectangle with the mouse.

```
12 = imerop(1)
X2 = imerop(X, map)
RGB2 = i merop(RGB)
```

If you omit the input arguments, i mor op operates on the image in the current axes.

To specify the rectangle:

- For a single-button mouse, press the mouse button and drag to define the crop rectangle. Finish by releasing the mouse button.
- For a 2- or 3-button mouse, press the left mouse button and drag to define the crop rectangle. Finish by releasing the mouse button.

If you hold down the Shift key while dragging, or if you press the right mouse button on a 2- or 3-button mouse, i mer op constrains the bounding rectangle to be a square.

When you release the mouse button, i mer op returns the cropped image in the supplied output argument. If you do not supply an output argument, i merop displays the output image in a new figure.

You can also specify the cropping rectangle noninteractively, using these syntaxes:

```
12 = imerop(I,rect)
X2 = imerop( X, mpp, rect)
RGB2 = imerop(RGB, rect)
```

rect is a four-element vector with the form [ xmin ymin width hei ght ]; these values are specified in spatial coordinates.

To specify a nondefault spatial coordinate system for the input image, precede the other input arguments with two two-element vectors specifying the XDat a and YDat a. For example,

$$
[\ldots]=i \operatorname{merop}(x, y, \ldots)
$$

If you supply additional output arguments, i nerop returns information about the selected rectangle and the coordinate system of the input image. For example,

```
[A,rect] = imerop(...)
[x,y,A, rect] = imerop(...)
```

A is the output image. x and y are the XDat a and YDDat a of the input image.

## Class Support The input image A can be of class ui nt 8, ui nt 16, or doubl e. The output image $B$ is of the same class as $A$. rect is always of class doubl e. <br> Remarks <br> Becauser ect is specified in terms of spatial coordinates, thewi dt $h$ and hei ght elements of rect do not always correspond exactly with the size of the output image. For example, suppose rect is [20 2040 30], using the default spatial coordinate system. The upper-left corner of the specified rectangle is the center of the pixel $(20,20)$ and the lower-right corner is the center of the pixel $(50,60)$. Theresulting output image is 31-by-41, not 30-by-40, because the output image includes all pixels in the input image that are completely or partially enclosed by the rectangle.

## Example

```
| = immead('ic.tif');
I2 = imerop(I,[60 40 100 90]);
i mshow(1)
figure, i nshow(I 2)
```


## imcrop



See Also
zoom

| Purpose | Compute feature measurements for image regions |  |  |
| :---: | :---: | :---: | :---: |
| Syntax | $\begin{aligned} & \text { st at } s=i \text { nf eat ure }(L, \text { measurement } s) \\ & \text { st at } s=i \text { ff eat ure e( } L \text {, measur ement } s, n) \end{aligned}$ |  |  |
| Description | st at s = inf eat ur e( L, neasur ements) computes a set of measurements for each labeled region in the label matrix $L$. Positive integer elements of $L$ correspond to different regions. For example, the set of elements of $L$ equal to 1 corresponds to region 1 ; the set of elements of $L$ equal to 2 corresponds to region 2; and so on. st at s is a structure array of length max(L(:)). The fields of the structure array denote different measurements for each region, as specified by measurements. |  |  |
|  | ' Ar ea' | ' I mage' | Eul er Number ' |
|  | ' Centroi d' | ' Fill edl mage' | ' Extrema' |
|  | ' Boundi ngBox' | ' Fill edArea' | ' Equi vDi anet er ' |
|  | ' Maj or Axi sLength' | ' ConvexHul I ' | ' Sol i dit ty' |
|  | ' M nor Axi sLengt h' | ' Convexl mage' | Ext ent ' |
|  | ' Eccentricity' | ' ConvexArea' | ' Pi xel Li st' |
|  | ' Ori entation' |  |  |

Measurement strings are case insensitive and can be abbreviated.
If neasur ements is the string ' all', then all of the above measurements are computed. If measur ement s is not specified or if it is the string ' basi $\mathrm{c}^{\prime}$, then these measurements are computed: ' Ar ea' , ' Centroi d' , and ' Boundi ngBox' .
st at $s=i n f$ eat ure( $L$, measur ement $s, n$ ) specifies thetype of connectivity used in computing the ' Fill edl mage' , ' Fill edAr ea' , and 'Eul er Nunber ' measurements. $n$ can have a value of either 4 or 8 , where 4 specifies

## imfeature

4-connected objects and 8 specifies 8-connected objects; if the argument is omitted, it defaults to 8.

## Definitions ' Ar ea' - Scalar; the actual number of pixels in the region. (This value may differ slightly from the value returned by bwar ea, which weights different patterns of pixels differently.)

' Cent r oi d' - 1-by-2 vector; thex- and y-coordinates of the center of mass of the region.
' Boundi ngBox' - 1-by-4 vector; the smallest rectangle that can contain the region. The format of the vector is [ $x$ y wi dth hei ght ], where $x$ and $y$ are the $x$ - and $y$-coordinates of the upper-left corner of the rectangle, and wi dt $h$ and hei ght are the width and height of the rectangle. Note that $x$ and $y$ are always noninteger values, because they are the spatial coordinates for the upper-left corner of a pixel in the image; for example, if this pixel is the third pixel in the fifth row of the image, then $x=2.5$ and $y=4.5$.

This figureillustrates the centroid and bounding box. The region consists of the white pixels; the green box is the bounding box, and the red dot is the centroid.

' Maj or Axi sLengt h' - Scalar; the length (in pixels) of the major axis of the ellipse that has the same second-moments as the region.
' M nor Axi sLengt h' - Scalar; the length (in pixels) of the minor axis of the ellipse that has the same second-moments as the region.
' Eccentri city' - Scalar; the eccentricity of the ellipse that has the same second-moments as the region. The eccentricity is the ratio of the distance between the foci of the ellipse and its major axis length. The value is between 0 and 1. ( 0 and 1 are degenerate cases; an ellipse whose eccentricity is 0 is actually a circle, while an ellipse whose eccentricity is 1 is a line segment.)

[^5]This figure illustrates the axes and orientation of the ellipse. The left side of the figure shows an image region and its corresponding ellipse. The right side shows the sameellipse, with features indicated graphically; the solid bluelines are the axes, the red dots are the foci, and the orientation is the angle between the horizontal dotted line and the major axis.

'I mage' - Binary image (ui nt 8) of the same size as the bounding box of the region; the on pixels correspond to the region, and all other pixels are of $f$.
' Fill edl mage' - Binary image (ui nt 8) of the same size as the bounding box of the region; the on pixels correspond to the region, with all holes filled in.
' FilledAr ea' - Scalar; the number of on pixels in Fill edl mage.
This figure illustrates 'I mage' and ' Fill edl mage'.


Original image, containing a single region

' I nage'

' Fi I I edl nage'
' ConvexHul I' - p-by-2 matrix; the smallest convex polygon that can contain the region. Each row of the matrix contains the $x$ - and $y$-coordinates of one vertex of the polygon.
' Convexl mage' - Binary image (ui nt 8); the convex hull, with all pixels within the hull filled in (i.e., set to on). (F or pixels that the boundary of the hull passes through, i nff eat ure uses the same logic as roi pol y to determine whether the pixel is inside or outside the hull.) The image is the size of the bounding box of the region.
' ConvexAr ea' - Scalar; the number of pixels in ' Convexl mage'.
' Eul er Number ' - Scalar; equal to the number of objects in theregion minus the number of holes in those objects.
' Ext rema' - 8-by-2 matrix; the extremal points in the region. Each row of the matrix contains the $x$ - and $y$-coordinates of one of the points; the format of the vector is [top-l eft top-right right-top right-bot tom bottom right bot tomleft left-bottomleft-top].

This figureillustrates the extrema of two different regions. In the region on the left, each extremal point is distinct; in the region on theright, certain extremal points (e.g., top-I ef $t$ and I ef $t-t o p$ ) areidentical.

' Equi vDi amet er ' - Scalar; the diameter of a circle with the same area as the region. Computed as sqrt ( $4^{*} \mathrm{Area}$ / pi ) .
' Sol i di ty' - Scalar; the proportion of the pixels in the convex hull that are also in the region. Computed as Area/ ConvexAr ea.
' Extent ' - Scalar; the proportion of the pixels in the bounding box that are also in the region. Computed as the Ar ea divided by area of the bounding box.
' Pi xel Li st' - p-by-2 matrix; the actual pixels in the region. Each row of the matrix contains the $x$ - and $y$-coordinates of one pixel in the region.

```
Class Support
The input label matrix L can be of class doubl e or of any integer class.
```

The comma-separated list syntax for structure arrays is very useful when working with the output of i nf eat ure. For example, for a field that contains a scalar, you can use a this syntax to create a vector containing the value of this field for each region in the image.
For instance, if st at s is a structure array with field Ar ea, then these two expressions are equivalent

```
```

Remarks

```
Remarks
stats(1).Area, stats(2).Area, ..., stats(end).Area
stats(1).Area, stats(2).Area, ..., stats(end).Area
stats(1).Area, stats(2).Area, ..., stats(end).Area
and
and
stats. Area
```

stats. Area

```
stats. Area
```

Therefore, you can use these calls to create a vector containing the area of each region in the image.

```
stats = infeature(L,' Area');
al|Area = [stats.Area];
```

al I Ar ea is a vector of the same length as the structure array st at s.
The function i snenber is useful in conjunction with i mf eat ur e for selecting regions based on certain criteria. F or example, these commands create a binary image containing only the regions in text. tif whose area is greater than 80.

```
idx = find([stats.Area] > 80);
BVR = i smember(L, i dx);
```

M ost of the measurements take very little time to compute. The exceptions are these, which may takesignificantly longer, depending on the number of regions in L:

- ' ConvexHul I '
- ' Convexl mage'
- ' ConvexArea'
- ' Fill edl mage'

Note that computing certain groups of measurements takes about the same amount of time as computing just one of them, because i nf eat ure takes advantage of intermediate computations used in both computations. Therefore,
it is fastest to compute all of the desired measurements in a single call to i nff eat ure.

## Example

```
BW = imead('text.tif');
L = bw abel (BW;
stats = i mf eature(L,' all');
stats(23)
ans =
```

Area: 89
Cent roi d: [ 95. 6742 192. 9775]
Boundi ngBox: [ 87.5000 184.5000 16 15]
Maj or Axi sLength: 19. 9127
M nor Axi sLengt h: 14. 2953
Eccentricity: 0.6961
Orientation: 9. 0845
ConvexHull: [ $28 \times 2$ double]
Convexl mage: [ $15 \times 16$ ui nt 8 ]
ConvexArea: 205
I mage: [ $15 \times 16$ ui nt 8 ]
Filledl mage: [ $15 \times 16$ ui nt 8 ]
FilledArea: 122
Eul er Number: 0
Extrenm: [ $8 \times 2$ doubl e]
Equi vDi amet er: 10. 6451
Sol i dity: 0.4341
Ext ent: 0.3708
Pi xel Li st: [ $89 \times 2$ doubl e]
See Also bw abel
i smenber in the MATLAB Function Reference

Purpose Information about graphics file

| Syntax | info = infinfo(fil ename, fmt ) |
| :---: | :---: |
|  | $\mathrm{info}=\mathrm{infinfo(filename)}$ |

Description info = infinfo(filename, fnt) returns a structure whose fields contain information about an image in a graphics file. fil ename is a string that specifies the name of the graphics file, and fmt is a string that specifies the format of the file. The file must be in the current directory or in a directory on the MATLAB path. If i mfi nf o cannot find a file named fil ename, it looks for a file named fi I ename. f mt .

This table lists the possible values for f nt .

| Format | File Type |
| :--- | :--- |
| ' bmp' | Windows Bitmap (BMP) |
| ' cur ' | Windows Cursor resources (CUR) |
| ' hdf ' | Hierarchical Data Format (HDF) |
| ' i co' | Windows Icon resources (ICO) |
| ' j pg' or ' j peg' | J oint Photographic Experts Group (J PEG) |
| ' pcx' | Windows Paintbrush (PCX) |
| ' png' | Portable Network Graphics (PNG) |
| 'tif' or 'tiff' | Tagged Image File Format (TIFF) |
| ' xwd' | X Windows Dump (XWD) |

If fil ename is a TIFF or HDF file containing more than one image, inf o is a structure array with one element (i.e., an individual structure) for each image in the file. For example, i nfo(3) would contain information about the third image in the file.

## imfinfo

The set of fields in i nf o depends on the individual file and its format. However, the first nine fields are always the same. This table lists these fields and describes their values.

| Field | Value |
| :---: | :---: |
| Fil ename | A string containing the name of the file; if the file is not in the current directory, the string contains the full pathname of the file |
| FileMbdDate | A string containing the date when the file was last modified |
| FileSize | An integer indicating the size of the file in bytes |
| Fornmt | A string containing the file format, as specified by fmt ; for JPEG and TIFF files, the three-letter variant is returned |
| For mat Version | A string or number describing the version of the format |
| W dth | An integer indicating the width of the image in pixels |
| Hei ght | An integer indicating the height of the image in pixels |
| Bi t Dept h | An integer indicating the number of bits per pixel |
| Col or Type | A string indicating the type of image; either 'truecol or' for a truecolor RGB image, ' grayscal e' for a grayscale intensity image, or 'i ndexed' for an indexed image |

info o infinfo(fil enane) attempts to infer the format of the file from its contents.

Remarks infinfo is a function in MATLAB.
Example

info = infinfo('canoe.tif')

info =
Fil ename: ' canoe. tif'
FileMbdDate: ' 25-Oct-1996 22: 10: 39'
FileSi ze: 69708
Format: 'tif'
Format Versi on: [ ]
W dt h: 346
Hei ght: 207
Bit Depth: 8
Col or Type: ' i ndexed'
For mat Si gnat ure: [ $\left.\begin{array}{llll}73 & 73 & 42\end{array}\right]$
ByteOrder: 'little-endi an'
NewSubfileType: 0
BitsPerSampl e: 8
Compressi on: ' PackBits'
Phot onetricl nter pret ation: ' RGB Pal ette'
Stripoffsets: [ $9 \times 1$ double]
Sampl esPer Pi xel : 1
RowsPerStrip: 23
StripByteCounts: [ 9x1 double]
XResol ution: 72
YResol ution: 72
Resol utionUnit: 'I nch'
Col ormp: [ $256 \times 3$ doubl e]
Pl anar Conf i gur at i on: ' Chunky'
Til eW' dt h: [ ]
Ti l eLengt h: [ ]
Til eoffsets: []
TileByt eCounts: []
Orientation: 1
FillOrder: 1
GrayResponseUni t: 0.0100
MaxSampl eVal ue: 255
M nSampl eVal ue: 0
Thr eshol di ng: 1
See Also imread, inwrite

## Purpose <br> Display a histogram of image data

Syntax<br>Description

Class Support
Example

```
i nmi st(I,n)
i nmi st(X, m@p)
[ counts,x] = i mhi st(...)
``` one bin for each entry in the col ormap. counts is the same as the length of the colormap. interval
\[
A(p-1.5) /(n-1) \leq x<A(p-0.5) /(n-1)
\] intensity image is ui nt 16 .
```

| = immead('pout.tif');
i mhi st(I)

```
i nmi st (I, n) displays a histogram with \(n\) bins for the intensity imagel above a grayscale colorbar of length \(n\). If you omit the argument, i mis st uses a default value of \(n=256\) if \(।\) is a grayscale image, or \(n=2\) if \(।\) is a binary image.
i mmi st ( \(X, \operatorname{map}\) ) displays a histogram for the indexed image \(X\). This histogram shows the distribution of pixel values above a col orbar of the colormap map. The col ormap must be at least as long as the largest index in X . The histogram has
[ counts, x ] \(=\mathrm{i}\) mist \((\ldots\) ) returns the histogram counts in counts and the bin locations in \(x\) so that st em \(x\), count s) shows the histogram. F or indexed images, it returns the histogram counts for each col ormap entry; the length of

Note For intensity images, the n bins of the histogram are each half-open intervals of width \(A /(n-1)\). In particular, the \(p\) th bin is the half-open

The scale factor A depends on the image class. A is 1 if the intensity image is doubl e; A is 255 if the intensity image is ui nt 8; and A is 65535 if the

The input image can be of class ui nt 8 , ui nt 16 , or doubl e.


See Also
hi steq
hi st in the MATLAB Function Reference

\section*{immovie}
Purpose Make movie of a multiframe indexed image
\begin{tabular}{|c|c|}
\hline Syntax & nov \(=\mathrm{i} \mathrm{mmovi} \mathrm{e( } \mathrm{X}, \mathrm{m}\) mp) \\
\hline \multirow[t]{2}{*}{Description} & mov \(=\) i mmovi e( \(X, n \not a p)\) returns the movie matrix mov from the images in the multiframe indexed image \(X\). As it creates the movie matrix, it displays the movie frames on the screen. You can play the movie using the MATLAB movi e function. \\
\hline & X comprises multipleindexed images, all having the same size and all using the colormap map. X is an mby-n-by-1-by-k array, where \(k\) is the number of images \\
\hline Class Support & \(X\) can be of class ui nt 8 , ui nt 16, or doubl e. nov is of class doubl e. \\
\hline Example & \[
\begin{aligned}
& \text { I oad mi } \\
& \text { mov = i mmovi e(D, map) ; }
\end{aligned}
\] \\
\hline See Also & mont age \\
\hline & avi file, get frame, novi e, novi e2avi in the MATLAB Function Reference \\
\hline Remarks & You can also make movies from images by using the MATLAB function avi file, which creates AVI files. In addition, you can convert an existing MATLAB movie into an AVI file by using the movi e2avi function. \\
\hline
\end{tabular}

\section*{Purpose Add noise to an image}
Syntax \(\quad\)\begin{tabular}{ll} 
J & \(=\) i moi se( I , type) \\
J & \(=\) i moi se( 1, type, par amet ers \()\)
\end{tabular}

Description J = i moi se(I, type) adds noise of type to the intensity image I . type is a string that can have one of these values:
- ' gaussi an' for Gaussian white noise
- ' sal t \& pepper' for "on and off" pixels
- 'speckl e' for multiplicative noise

J = i moi se(I, type, par anet ers) accepts an algorithm type plus additional modifying parameters particular to the type of algorithm chosen. If you omit these arguments, i moi se uses default values for the parameters. Here are examples of the different noise types and their parameters:
- J = i moi se(I, ' gaussi an' , m v) adds Gaussian white noise of mean mand variance \(v\) to the imagel. The default is zero mean noise with 0.01 variance.
- J = i moi se(I, ' sal t \& pepper' , d) adds salt and pepper noisetotheimage I, where \(d\) is the noise density. This affects approximately \(d^{*}\) pr od( si ze(I) ) pixels. The default is 0.05 noise density.
- J = i moi se(I,' speckl e' , v) adds multiplicative noise to the image।, using the equation \(J=1+n * I\), where \(n\) is uniformly distributed random noise with mean 0 and variance \(v\). The default for \(v\) is 0.04 .

Class Support The input imagel can be of class ui nt 8, ui nt 16, or doubl e. The output image \(J\) is of the same class as \(I\).

\section*{Example}
```

l = imead(' ei ght.tif');
J = i mmoi se(I,'salt \& pepper',0.02);
i mshow(I)
figure, inshow(J)

```

\section*{imnoise}

See Also rand, randn in the MATLAB Function Reference

\section*{Purpose Determine pixel col or values}

\section*{Syntax}
```

P = i mpi xel (I )
P = i mpi xel ( X, n⿴p)
P = i mpi xel(RGB)
P = i mpi xel (I, c,r)
P = i mpi xel ( }X,n\not=p,c,r
P = i mpi xel(RGB, c,r r)
[c,r,P] = impixel(...)
P = i mpi xel ( x, y, l, xi, yi)
P = i mpi xel ( }x,y,X,m\not=p,xi,yi
P = i mpi xel ( }x,y,RGB,xi,yi
[xi,yi,P] = i mpi xel (x,y, ...)

```

\section*{Description i mpi xel returns the red，green，and blue col or values of specified image pixels．} In the syntaxes below，i mpi xel displays the input image and waits for you to specify the pixels with the mouse．
```

$\mathrm{P}=\mathrm{impixel}(1)$
$P=i \operatorname{mpi} x e l(X, n \not ⿴ 囗)$
P = i mpi xel (RGB)

```

If you omit the input arguments，i mpi xel operates on the image in the current axes．

Usenormal button clicks to select pixels．Press Backspace or Delete to remove the previously selected pixel．A shift－click，right－click，or double－click adds a final pixel and ends the selection；pressing Return finishes the selection without adding a pixel．

When you finish selecting pixels，i mpi xel returns an mby－3 matrix of RGB values in the supplied output argument．If you do not supply an output argument，i mpi xel returns the matrix in ans．

You can also specify the pixels noninteractively，using these syntaxes．
```

P = i mpi xel (I, c,r)
P = i mpi xel ( X, m⿴囗, c,r)
P = i mpi xel (RGB, c,r)

```
\(r\) and \(c\) are equal-length vectors specifying the coordinates of the pixels whose RGB values are returned in \(P\). The \(k^{\text {th }}\) row of \(P\) contains the RGB values for the pixel ( \(\mathrm{r}(\mathrm{k}), \mathrm{c}(\mathrm{k})\) ).

If you supply three output arguments, i mpi xel returns the coordinates of the selected pixels. F or example,
\[
[\mathrm{c}, \mathrm{r}, \mathrm{P}]=\mathrm{impi} \operatorname{xel}(\ldots)
\]

To specify a nondefault spatial coordinate system for the input image, use these syntaxes.
\[
\begin{aligned}
& \mathrm{P}=\mathrm{i} \text { mi xel }(x, y, l, x i, y i) \\
& P=i \text { mpi xel }(x, y, x, \text { mp, xi , yi }) \\
& P=i \text { mi xel }(x, y, \text { RGB, xi, yi })
\end{aligned}
\]
\(x\) and \(y\) are two-element vectors specifying the image XDat a and YDat \(a . x i\) and yi are equal-length vectors specifying the spatial coordinates of the pixels whose RGB values are returned in P. If you supply three output arguments, i mpi xel returns the coordinates of the selected pixels.
\[
[x i, y i, P]=\text { i mpi xel }(x, y, \ldots)
\]

Class Support Theinput image can be of class ui nt 8, ui nt 16, or doubl e. All other inputs and outputs are of class doubl e.

Remarks

Example
i mpi xel works with indexed, intensity, and RGB images. i mpi xel always returns pixel values as RGB triplets, regardless of the image type:
- For an RGB image, i mpi xel returns the actual data for the pixel. The values are either ui nt 8 integers or doubl e floating-point numbers, depending on the class of the image array.
- For an indexed image, i mpi xel returns the RGB triplet stored in the row of the colormap that the pixel value points to. The values are doubl e floating-point numbers.
- For an intensity image, i mpi xel returns the intensity value as an RGB triplet, where \(R=G=B\). The values are either ui nt 8 integers or double floating-point numbers, depending on the class of the image array.
```

RGB = immead('flowers.tif');
c = [12 146 410];

```

12-132
\[
\begin{aligned}
& r=\left[\begin{array}{ll}
104 & 156 \\
129] ;
\end{array}\right. \\
& \text { pi xel s = i mpi xel (RGB, c, r) } \\
& \text { pi xel s = }
\end{aligned}
\]
See Also i mprofile, pi xval

\section*{improfile}

Purpose

\section*{Syntax}

\section*{Description}

Compute pixel-value cross-sections along line segments
```

c = improfile
c = improfile(n)
c = improfile(I,xi,yi)
c = improfile(I, xi, yi,n)
[cx,cy,c] = improfile(...)
[cx,cy,c, xi,yi] = i mprofile(...)
[...] = improfile(x,y,l,xi, yi )
[...] = improfile(x,y,I,xi,yi,n)
[...] = improfile(...., method)

```
i mpr of ile computes the intensity values al ong a line or a multiline path in an image. i mpr of i I e sel ects equally spaced points al ong the path you specify, and then uses interpolation to find the intensity value for each point. i mpr of ile works with grayscale intensity images and RGB images.

If you call i mpr of i l e with one of these syntaxes, it operates interactively on the image in the current axes.
\[
\begin{aligned}
& \mathrm{c}=\mathrm{improfile} \\
& \mathrm{c}=\mathrm{improfile}(\mathrm{n})
\end{aligned}
\]
n specifies the number of points to computethe intensity valuefor. If you do not provide this argument, i mprof ile chooses a value for \(n\), roughly equal to the number of pixels the path traverses.

You specify theline or path using the mouse, by clicking on points in theimage. Press Backspace or Delete to remove the previously selected point. A shift-click, right-click, or double-click adds a final point and ends the selection; pressing Return finishes the selection without adding a point. When you finish selecting points, i mpr of ile returns the interpolated data values in c. c is an n -by- 1 vector if the input is a grayscal eintensity image, or an n-by-1-by-3 array if the input is an RGB image.

If you omit the output argument, i mpr of i l e displays a plot of the computed intensity values. If the specified path consists of a single line segment, i mprofile creates a two-dimensional plot of intensity values versus the distance along the line segment; if the path consists of two or more line segments, i mpr of ile creates a three-dimensional plot of the intensity values versus their \(x\) - and \(y\)-coordinates.

You can also specify the path noninteractively, using these syntaxes.
```

c = improfile(I, xi,yi)
c = improfile(l,xi,yi,n)

```
xi and yi are equal-length vectors specifying the spatial coordinates of the endpoints of the line segments.

You can use these syntaxes to return additional information.
```

[cx, cy, c] = improfile(...)
[cx, cy, c, xi, yi] = improfile(...)

```
cx and cy are vectors of length \(n\), containing the spatial coordinates of the points at which the intensity values are computed.

To specify a nondefault spatial coordinate system for the input image, use these syntaxes.
\[
\begin{aligned}
{[\ldots] } & =\operatorname{improfile}(x, y, l, x i, y i) \\
{[\ldots] } & =\text { improfile }(x, y, l, x i, y i, n)
\end{aligned}
\]
\(x\) and \(y\) are two-element vectors specifying the image XDat a and YDat a.
[...] = improfile(. . . , method) uses the specified interpolation method. net hod is a string that can have one of these values:
- ' nearest' (default) uses nearest neighbor interpolation.
- ' bi li near' uses bilinear interpolation.
- ' bi cubi c' uses bicubic interpolation.

If you omit the ret hod argument, i mpr of il e uses the default method of ' near est'.

Class Support The input image can be of class ui nt 8, ui nt 16, or doubl e. All other inputs and outputs are of class doubl e.

\section*{Example}
\[
\begin{aligned}
& \text { I = imread(' al ungrns.tif'); } \\
& x=\left[\begin{array}{lll}
35 & 338 & 346 \\
103
\end{array}\right] ; \\
& \text { y = [ } 25325017 \text { 148]; } \\
& \text { i mprofile(l, x,y), grid on }
\end{aligned}
\]


See Also
i mpi xel, pi xval
int er p2 in the MATLAB Function Reference
\begin{tabular}{|c|c|}
\hline Purpose & Read image from graphics files \\
\hline Syntax & \begin{tabular}{l}
A = imead(filename, fmt ) \\
[ \(\mathrm{X}, \mathrm{m} \neq \mathrm{p}]=\mathrm{immead}(\mathrm{fi} \mathrm{I}\) ename, fmt\()\) \\
[...] = imead(fil ename) \\
[...] = imread(...,idx) (CUR,ICO, and TIFF only) \\
[...] = i mead(....ref) (HDF only) \\
[...] = i mread(..., 'BackgroundCol or', BG) (PNG only) \\
[ A, map, al pha] = imead(...) (PNG only)
\end{tabular} \\
\hline \multirow[t]{6}{*}{Description} & \begin{tabular}{l}
A = imead( fi l ename, f nt ) reads a grayscale or truecol or image named fil ename into \(A\). If the file contains a grayscale intensity image, \(A\) is a two-dimensional array. If the file contains a truecolor (RGB) image, \(A\) is a three-dimensional (mby-n-by-3) array. \\
[ \(\mathrm{X}, \mathrm{m} \notin \mathrm{p}\) ] = imead(filename, fmt\()\) reads the indexed image in fil ename into \(X\) and its associated col ormap into mp. The col ormap values are rescaled to the range [0,1]. A and map are two-dimensional arrays. \\
[ . . .] = i mead( fi I ename) attempts to infer the format of the file from its content. \\
fil ename is a string that specifies the name of the graphics file, and \(f \mathrm{mt}\) is a string that specifies the format of the file. If the file is not in the current directory or in a directory in the MATLAB path, specify the full pathname for a location on your system. If i mead cannot find a file named fi I enane, it looks for a file named \(\mathrm{f} \boldsymbol{i} \mathrm{I}\) ename. f nt . If you do not specify a string for f nt , thetool box will try to discern the format of the file by checking the file header. \\
This table lists the possible values for f nt .
\end{tabular} \\
\hline & Format File Type \\
\hline & ' bmp' Windows Bitmap (BMP) \\
\hline & ' cur ' Windows Cursor resources (CUR) \\
\hline & ' hdf ' Hierarchical Data Format (HDF) \\
\hline & ' i co' Windows Icon resources (ICO) \\
\hline
\end{tabular}

\section*{imread}
\begin{tabular}{l|l}
\hline Format & File Type \\
\hline ' j pg' or ' j peg' & J oint Photographic Experts Group (J PEG) \\
' pcx' & Windows Paintbrush (PCX) \\
\hline 'png' & Portable Network Graphics (PNG) \\
\hline 'tif' or 'tiff' & Tagged Image File Format (TIFF) \\
\hline ' xud' & X Windows Dump (XWD) \\
\hline
\end{tabular}

\section*{Special Case Syntax:}

\section*{TIFF-Specific Syntax}
[...] = i mead(..., idx) reads in one image from a multi-image TIFF file. \(i d x\) is an integer value that specifies the order in which the image appears in the file. For example, if i dx is 3, i mread reads the third image in the file. If you omit this argument, i mread reads the first image in the file.

\section*{PN G -Specific Syntax}

The discussion in this section is only relevant to PNG files that contain transparent pixels. A PNG file does not necessarily contain transparency data. Transparent pixels, when they exist, will be identified by one of two components: a transparency chunk or an alpha channed. (A PNG file can only have one of these components, not both.)

The transparency chunk identifies which pixel values will be treated as transparent, e.g., if the value in the transparency chunk of an 8 -bit image is 0.5020 , all pixels in the image with the col or 0.5020 can be displayed as transparent. An alpha channel is an array with the same number of pixels as are in the image, which indicates the transparency status of each corresponding pixel in the image (transparent or nontransparent).

Another potential PNG component related to transparency is the background col or chunk, which (if present) defines a col or value that can be used behind all transparent pixels. This section identifies the default behavior of the tool box for reading PNG images that contain either a transparency chunk or an alpha channel, and describes how you can override it.

Case 1. You do not ask to output the alpha channel and do not specify a background color to use. For example,
```

[A, map] = i mread(fil ename);
A = i mmead(fil ename);

```

If the PNG file contains a background col or chunk, the transparent pixels will be composited against the specified background col or.

If the PNG file does not contain a background color chunk, the transparent pixels will be composited against 0 for grayscale (black), 1 for indexed (first color in map), or [ 0000\(]\) for RGB (black).

Case 2. You do not ask to output the alpha channel but you specify the background color parameter in your call. F or example,
[...] \(=\) i mead(. . . , ' BackgroundCol or ' , bg) ;
The transparent pixels will be composited against the specified color. The form of bg depends on whether the file contains an indexed, intensity (grayscale), or RGB image. If the input image is indexed, bg should be an integer in the range [ 1, P] where P is the col ormap length. If the input image is intensity, bg should be an integer in the range [0,1]. If the input image is RGB, bg should be a three-element vector whose values are in the range [0,1].

There is one exception to thetool box's behavior of using your background col or. If you set background to ' none' no compositing will be performed. F or example,
\[
\text { [...] }=\text { i mead(. . . , ' Back' , ' none' ) ; }
\]

Note If you specify a background col or, you cannot output the alpha channel.

Case 3. You ask to get the alpha channel as an output variable. For example, [A, map, al pha] = imead(filename); [A, map, al pha] = imead(fil ename, fnt);
No compositing is performed; the al pha channel will be stored separately from the image (not merged intothe image as in cases 1 and 2). This form of i m ead returns the al pha channel if one is present, and also returns the image and any associated colormap. If there is no alpha channel, al pha returns [ ]. If there is no colormap, or the image is grayscale or truecol or, map may be empty.

\section*{HDF-Specific Syntax}
[ . . .] = i mread(. . . , ref ) reads in one image from a multi-image HDF file. \(r\) ef is an integer value that specifies the reference number used to identify the image. For example, if \(r\) ef is 12 , i mead reads the image whose reference number is 12. (Note that in an HDF file the reference numbers do not necessarily correspond to the order of the images in the file. You can use i mfi inf o to match up image order with reference number.) If you omit this argument, i mread reads the first image in the file.

\section*{CUR- and ICO-Specific Syntax}
[...] = i mead(....idx) reads in one image from a multi-image icon or cursor file. idx is an integer value that specifies the order that the image appears in the file. F or example, if i dx is 3, i mread reads the third image in the file. If you omit this argument, i mead reads the first image in the file.
[ A, nøp, al pha] = i mread(... ) returns theAND mask for the resource, which can be used to determine the transparency information. For cursor files, this mask may contain the only useful data.

Note By default, Microsoft Windows cursors are 32-by-32 pixels. MATLAB pointers must be 16-by-16. You will probably need to scale your image. If you have the I mage Processing Toolbox, you can use the i mesi ze function.

\section*{Format Support}

This table summarizes the types of images that i mread can read.
\begin{tabular}{l|l}
\hline Format & Variants \\
\hline BMP & \begin{tabular}{l} 
1-bit, 4-bit, 8-bit, and 24-bit uncompressed images; 4-bit \\
and 8-bit run-length encoded (RLE) images
\end{tabular} \\
\hline CUR & 1-bit, 4-bit, and 8-bit uncompressed images \\
\hline HDF & \begin{tabular}{l} 
8-bit raster image datasets, with or without associated \\
colormap; 24-bit raster image datasets
\end{tabular} \\
\hline ICO & 1-bit, 4-bit, and 8-bit uncompressed images \\
\hline
\end{tabular}
\begin{tabular}{l|l}
\hline Format & Variants \\
\hline J PEG & \begin{tabular}{l} 
Any baseline J PEG image (8 or 24-bit); J PEG images with \\
some commonly used extensions
\end{tabular} \\
\hline PCX & 1-bit, 8-bit, and 24-bit images \\
\hline PNG & \begin{tabular}{l} 
Any PNG image, including 1-bit, 2-bit, 4-bit, 8-bit, and \\
16-bit grayscale images; 8-bit and 16-bit indexed images; \\
24-bit and 48-bit RGB images
\end{tabular} \\
\hline TIFF & \begin{tabular}{l} 
Any baseline TIFF image, including 1-bit, 8-bit, and 24-bit \\
uncompressed images; 1-bit, 8-bit, 16-bit, and 24-bit images \\
with packbits compression; 1-bit image with CCITT \\
compression; also 16-bit grayscale, 16-bit indexed, and \\
48-bit RGB images.
\end{tabular} \\
\hline XWD & 1-bit and 8-bit ZPixmaps; XYBitmaps; 1-bit XYPixmaps \\
\hline
\end{tabular}

\section*{Class Support}

In most of the image file formats supported by i mead, pixels are stored using eight or fewer bits per col or plane. When reading such a file, the class of the output (A or X ) is ui nt 8 . i mr ead al so supports reading 16-bit-per-pixel data from TIFF and PNG files; for such image files, the class of the output (A or X) is ui nt 16. Note that for indexed images, i mread always reads the col ormap into an array of class doubl e, even though the image array itself may be of class ui nt 8 or ui nt 16 .

\section*{Remarks i mread is a function in MATLAB.}

Examples \(\quad\) This example reads the sixth image in a TIFF file.
[ \(\mathrm{X}, \mathrm{n} \not \mathrm{P} \mathrm{p}\) ] = imead('flowers.tif', 6);
This example reads the fourth image in an HDF file.
info = infinfo('skull.hdf');
[ \(\mathrm{X}, \mathrm{n} \nexists \mathrm{p}\) ] = i mread(' skull. hdf ' , i nf o(4). Ref er ence);
This example reads a 24-bit PNG image and sets any of its fully transparent (alpha channel) pixels to red.
\(\mathrm{bg}=\left[\begin{array}{lll}255 & 0 & 0\end{array}\right] ;\)
```

A = i mread(' i mage. png',' BackgroundCol or',bg);

```

This example returns the alpha channel（if any）of a PNG image．
［ A，n⿴囗十，al pha］＝i mead（＇i mage．png＇）；
This example reads an ICO image，applies a transparency mask，and then displays the image．
［ a，b，c］＝i mread（＇myi con．ico＇）；
\％Augment col ormap for background col or（white）．
b2＝\(\left[\begin{array}{lll}b ; & 1 & 1\end{array}\right]\) ；
\％Create new i mage for di splay．
d＝ones（size（a））＊（length（b2）－1）；
\％Use the AND mask to mix the background and
\％for eground data on the new i mage
\(\mathrm{d}(\mathrm{c}=0)=\mathrm{a}(\mathrm{c}=0)\) ；
\％Di spl ay new i mage
i ms how ui nt 8（d），b2）
See Also
doubl e，fread，i minfo，i murite，ui nt 8，ui nt 16
\begin{tabular}{|c|c|}
\hline Purpose & Resize an image \\
\hline \multirow[t]{4}{*}{Syntax} & \(B=i m m e s i z e(A, m m e t h o d)\) \\
\hline & B = immesize( \(\mathrm{A},[\mathrm{mmows}\) ncol s], met hod) \\
\hline & \(B=i m m e s i z e(\ldots, ~ m e t h o d, ~ n) ~\) \\
\hline & \(B=i m e s i z e(\ldots\), met hod, \(h\) ) \\
\hline
\end{tabular}

Description
i mesi ze resizes an image of any type using the specified interpolation method. met hod is a string that can have one of these values:
- ' nearest' (default) uses nearest neighbor interpolation.
- ' bi li near' uses bilinear interpolation.
- ' bi cubi c' uses bicubic interpolation.

If you omit the ret hod argument, i mesi ze uses the default method of ' near est'
\(B=i m e s i z e(A, m\) met hod) returns an image that is mtimes the size of \(A\). If \(m\) is between 0 and 1.0, B is smaller than A . If mis greater than \(1.0, \mathrm{~B}\) is larger than A.
\(B=i \operatorname{mesi} z e(A,[\) mows ncol \(s]\), met hod) returns an image of size [ mrows ncol s]. If the specified size does not produce the same aspect ratio as the input image has, the output image is distorted.

When the specified output size is smaller than the size of the input image, and met hod is 'bi I i near ' or ' bi cubi c' , i mresi ze applies a lowpass filter before interpolation to reduce aliasing. The default filter size is 11-by-11.

You can specify a different order for the default filter using
[... ] = i mmesi ze(. . . , met hod, n)
\(n\) is an integer scalar specifying the size of the filter, which is \(n-b y-n\). If \(n\) is 0 (zero), i mesi ze omits the filtering step.

You can also specify your own filter h using
[...] = imesize(... , met hod, h)

\section*{imresize}
\(h\) is any two-dimensional FIR filter (such as thosereturned by ftrans2, f wi nd1, f wi nd2, or f samp2).

\section*{Class Support The input image can be of class ui nt 8, ui nt 16, or doubl e. The output image is of the same class as the input image.}

\author{
See Also int er p2 in the MATLAB Function Reference
}
\begin{tabular}{|c|c|}
\hline Purpose & Rotate an image \\
\hline \multirow[t]{2}{*}{Syntax} & \(B=i \operatorname{mot}\) ate ( \(A\), angle, met hod) \\
\hline & \(B=i \operatorname{mot}\) ate( \(A\), angle, met hod, ' crop' ) \\
\hline \multirow[t]{7}{*}{Description} & \(B=i \operatorname{mot}\) at e( \(A\), angl e, met hod) rotates the image \(A\) by angl e degrees in a counter-clockwise direction, using the specified interpolation method. met hod is a string that can have one of these values: \\
\hline & - ' nearest' (default) uses nearest neighbor interpolation. \\
\hline & - ' bi l i near' uses bilinear interpolation. \\
\hline & - ' bi cubi c' uses bicubic interpolation. \\
\hline & If you omit the met hod argument, i mrot ate uses the default method of ' near est'. \\
\hline & The returned image matrix B is, in general, larger than A to include the whole rotated image. i mot at e sets invalid values on the periphery of \(B\) to 0 . \\
\hline & \(B=i \operatorname{mot}\) ate( \(A\), angle, met hod, ' crop' ) rotates the image A through angle degrees and returns the central portion which is the same size as \(A\). \\
\hline Class Support & The input image can be of class ui nt 8 , ui nt 16 , or doubl e. The output image is of the same class as the input image. \\
\hline Remarks & To rotate the image clockwise, specify a negative angle. \\
\hline \multirow[t]{3}{*}{Example} & \(\mathrm{l}=\mathrm{immead}\left(\mathrm{ic} . \mathrm{tif}{ }^{\prime}\right)\); \\
\hline &  \\
\hline & i mshow (I) \\
\hline
\end{tabular}


See Also
i merop, i mesize
\begin{tabular}{|c|c|}
\hline Purpose & Display an image \\
\hline \multirow[t]{9}{*}{Syntax} & i mshow (1, n) \\
\hline & i mshow( I, [low hi gh]) \\
\hline & i mshow BW) \\
\hline & i mshow ( X , map) \\
\hline & i ms how (RGB) \\
\hline & i mshow(..., di spl ay_option) \\
\hline & i nshom \(x, y, A, \ldots\) ) \\
\hline & i mshow fil ename \\
\hline & \(\mathrm{h}=\mathrm{i}\) mshow (...) \\
\hline \multirow[t]{7}{*}{Description} & inshow (1,n) displays theintensity imagel with \(n\) discrete levels of gray. If you omit n, i ms howuses 256 gray levels on 24-bit displays, or 64 gray levels on other systems. \\
\hline & i nshow(I, [ low hi gh] ) displays I as a grayscale intensity image, specifying the data range for I. The value I ow (and any value less than I ow) displays as black, the value hi gh (and any value greater than hi gh) di splays as white, and values in between display as intermediate shades of gray. i ms how uses the default number of gray levels. If you use an empty matrix ([ ]) for [ I ow hi gh], imshowuses [min(I(:)) max(I(:))]; the minimum valuein I displays as black, and the maximum value displays as white. \\
\hline & i nshow BW displays the binary image BW Values of 0 display as black, and values of 1 display as white. \\
\hline & i ms how ( \(\mathrm{X}, \mathrm{m} \not \mathrm{p}\) ) displays the indexed image X with the col ormap map. \\
\hline & i ms how (RGB) displays the truecol or image RGB. \\
\hline & i nshow(... , di spl ay_opt ion) displays the image, calling truesi ze if di spl ay_opti on is ' truesi ze', or suppressing the call to truesi ze if di spl ay_opti on is ' not ruesi ze' . Either option string can be abbreviated. If you do not supply this argument, i ms how determines whether to call truesi ze based on the setting of the'I mshowTruesi ze' preference. \\
\hline & i mฐhow ( \(\mathrm{x}, \mathrm{y}, \mathrm{A}, \ldots\) ) uses the two-element vectors x and y to establish a nondefault spatial coordinate system, by specifying the image XDat a and YData. \\
\hline
\end{tabular}

\section*{imshow}
i ns howf il ename displays the image stored in the graphics file fil ename. i ms how calls i mread to read the image from the file, but the image data is not stored in the MATLAB workspace. The file must be in the current directory or on the MATLAB path.
\(\mathrm{h}=\mathrm{i}\) ns how (...) returns the handle to the image object created by ins how.

\section*{Class Support The input image can be of class ui nt 8, ui nt 16, or doubl e.}

Remarks

See Also
You can use the i pt set pr ef function to set several tool box preferences that modify the behavior of imshow. For example,
- 'I nshowBor der ' controls whether i nshow displays the image with a border around it.
- ' I mshowAxesVi si bl e' controls whether i mshow displays the image with the axes box and tick labels.
- 'InshowTruesi ze' controls whether i mshow calls the truesi ze function.
Note that the di spl ay_opti on argument toi ns howenables you to override the 'ImshowTruesi ze' preference.
F or more information about these preferences, see the reference entry for i pt set pref.
get i mage, i mead, i pt get pr ef, i pt set pr ef, subi mage, truesi ze, war p i mage, i magesc in the MATLAB Function Reference

\begin{abstract}
Purpose Write image to graphics file
Syntax imurite(A, filename, fnt)

i murite(..., filename)
i mwite(.... Param1, Val 1, Par am2, Val 2. . . )
i murite( A, fil ename, fnt ) writes the image in A to fil ename in the format specified by f nt . A can be either a grayscal e image ( \(\mathrm{M}-\mathrm{by}-\mathrm{N}\) ) or a truecol or image ( M -by- N -by-3). If \(A\) is of class ui nt 8 or ui nt 16 , i nwrite writes the actual values in the array to the file. If A is of class doubl e, i mwrite rescales the values in the array before writing, using ui nt 8( round( \(255 *\) A) ) . This operation converts the floating-point numbers in the range [0,1] to 8-bit integers in the range \([0,255]\).
i murite( \(X\), n⿴p, filenane, \(f\) nt \()\) writes the indexed image in \(X\) and its associated col ormap map to fil ename in the format specified by ftt . If X is of class ui nt 8 or ui nt 16, i mwrite writes the actual values in the array to the file. If \(X\) is of class doubl e, inwrite offsets the values in the array beforewriting using ui nt \(8(X-1)\). (See note below for an exception.) nap must be a valid MATLAB colormap of class doubl e; i mwrite rescales the values in map using ui nt 8 ( round ( \(255^{*}\) nap) ) . N ote that most image file formats do not support colormaps with more than 256 entries.
\end{abstract}

Note If the image is doubl e, and you specify PNG as the output format and a bit depth of 16 bpp , the values in the array will be offset using ui nt \(16(\mathrm{X}-1)\).
i murite(..., fillename) writes the image to fil ename, inferring the format to use from the filename's extension. The extension must be one of the legal values for f nt .
i mwrite(. . . . Par am1, Val 1, Par am2, Val 2. . . ) specifies parameters that control various characteristics of the output file. Parameter settings can currently be made for HDF, PNG, JPEG, and TIFF files. For example, if you are writing a J PEG file, you can set the "quality" of theJ PEG compression. For the lists of parameters available for each format, see the tables below.

\section*{imw rite}
fil ename is a string that specifies the name of the output file, and f nt is a string that specifies the format of the file.

This table lists the possible values for f mt .
\begin{tabular}{l|l}
\hline Format & File Type \\
\hline ' bmp' & Windows Bitmap (BMP) \\
\hline ' hdf ' & Hierarchical Data Format (HDF) \\
\hline ' j pg' or ' j peg' & J oint Photographic Experts Group (J PEG) \\
\hline ' pcx' & Windows Paintbrush (PCX) \\
\hline ' png' & Portable Network Graphics (PNG) \\
\hline ' tif' or ' tiff' & Tagged Image File Format (TIFF) \\
\hline ' xwd' & X Windows Dump (XWD) \\
\hline
\end{tabular}

This table describes the available parameters for HDF files.
\begin{tabular}{l|l|l}
\hline Parameter & Values & Default \\
\hline ' Compressi on' & \begin{tabular}{l} 
One of these strings: ' none' (the default), ' rl e' , \\
' j peg'. ' rl e' is valid only for grayscale and \\
indexed images. ' j peg' is valid only for grayscale \\
and RGB images.
\end{tabular} & ' rl e' \\
\hline ' Qual ity' & \begin{tabular}{l} 
A number between 0 and 100; this parameter \\
applies only if ' Compressi on' is ' j peg' . \\
Higher numbers mean higher quality (less image \\
degradation due to compression), but the resulting \\
file size is larger.
\end{tabular} & 75 \\
\hline 'WiteMbde' & \begin{tabular}{l} 
One of these strings: ' over write' (the default), or \\
' append' .
\end{tabular} & ' overwrite' \\
\hline
\end{tabular}

This table describes the available parameters for J PEG files.
\begin{tabular}{l|l|l}
\hline Parameter & Values & Default \\
\hline ' Qual i ty' & \begin{tabular}{l} 
A number between 0 and 100; higher numbers \\
mean higher quality (less image degradation due to \\
compression), but the resulting file size is larger.
\end{tabular} & 75 \\
\hline
\end{tabular}

This table describes the available parameters for TIFF files.
\begin{tabular}{|c|c|c|}
\hline Parameter & Values & Default \\
\hline ' Compressi on' & One of these strings: ' none', ' packbits', ' ccitt', ' fax3', or ' fax4'. The' ccitt', ' fax3', and ' fax4' compression schemes are valid for binary images only. & ' ccitt' for binary images; ' packbits' for nonbinary images \\
\hline ' Description' & Any string; fills in the I mageDescription field returned by i mf info. & empty \\
\hline ' Resol ution' & A two-element vector containing the XResolution and YResolution, or a scalar indicating both resolutions. & 72 \\
\hline 'WiteMbde' & One of these strings: ' over write' or ' append' & ' over write' \\
\hline
\end{tabular}

This table describes the available parameters for PNG files.
\begin{tabular}{l|l|l}
\hline Parameter & Values & Default \\
\hline ' Aut hor' & A string & Empty \\
\hline ' Descri pt i on' & A string & Empty \\
\hline ' Copyri ght ' & A string & Empty \\
\hline ' Creati onTi me' & A string & Empty \\
\hline ' Sof t ware' & A string & Empty \\
\hline ' Di scl ai mer' & A string & Empty \\
\hline
\end{tabular}

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\section*{imw rite}
\begin{tabular}{|c|c|c|}
\hline Parameter & Values & Default \\
\hline ' Whrni ng' & A string & Empty \\
\hline ' Sour ce' & A string & Empty \\
\hline ' Comment \({ }^{\text {' }}\) & A string & Empty \\
\hline ' I nter I aceType' & Either ' none' or ' adam' & 'none' \\
\hline ' Bi t Depth' & A scalar value indicating desired bit depth. For grayscale images this can be \(1,2,4,8\), or 16. For grayscaleimages with an alpha channel this can be 8 or 16 . For indexed images this can be 1, 2, 4 , or 8 . For truecolor images with or without an alpha channel this can be 8 or 16 . & \begin{tabular}{l}
8 bits per pixel if image is doubleor uint8 \\
16 bits per pixel if image is uint16 1 bit per pixel if image is logical
\end{tabular} \\
\hline ' Tr anspar ency' & \begin{tabular}{l}
This value is used to indicate transparency information only when no al pha channel is used. Set to the value that indicates which pixels should be considered transparent. (If the image uses a col ormap, this value will represent an index number to the colormap.) \\
For indexed images: a Q element vector in the range \([0,1]\) where \(Q\) is nolarger than the colormap length and each value indicates the transparency associated with the corresponding colormap entry. In most cases, Q=1. \\
For grayscale images: a scalar in the range [0,1]. The value indicates the grayscale col or to be considered transparent. \\
For truecol or images: a three-element vector in the range [0,1]. The value indicates the truecol or col or to be considered transparent. \\
You cannot specify ' Tr ansparency' and 'Al pha' at the same time.
\end{tabular} & Empty \\
\hline
\end{tabular}
\begin{tabular}{|c|c|c|}
\hline Parameter & Values & Default \\
\hline ' Background' & The value specifies background col or to be used when compositing transparent pixels. For indexed images: an integer in the range [1,P], where \(P\) is the colormap length. For grayscale images: a scal ar in the range \([0,1]\). For truecol or images: a three-element vector in the range [0,1]. & Empty \\
\hline ' Gamma' & A nonnegative scalar indicating the file gamma & Empty \\
\hline ' Chr omaticities' & An eight-element vector [ wx wy rx ry gx gy bx by] that specifies the reference white point and the primary chromaticities & Empty \\
\hline ' XResol ution' & A scalar indicating the number of pixels/unit in the horizontal direction & Empty \\
\hline ' YResol ution' & A scalar indicating the number of pixels/unit in the vertical direction & Empty \\
\hline ' Resol utionUnit' & Either 'unknown' or 'ret er' & Empty \\
\hline ' Al pha' & A matrix specifying the transparency of each pixel individually. The row and column dimensions must be the same as the data array; they can be ui nt 8, ui nt 16, or doubl e, in which case the values should be in the range \([0,1]\). & Empty \\
\hline 'Signifi cant Bits' & \begin{tabular}{l}
A scalar or vector indicating how many bits in the data array should be regarded as significant; values must be in the range [1,Bi t Dept h ]. \\
For indexed images: a three-element vector. For grayscale images: a scalar. For grayscale images with an alpha channel: a two-element vector. For truecol or images: a three-element vector. For truecol or images with an alpha channel: a four-element vector
\end{tabular} & Empty \\
\hline
\end{tabular}

\section*{imw rite}

In addition to these PNG parameters, you can use any parameter name that satisfies the PNG specification for keywords, including only printable characters, 80 characters or fewer, and noleading or trailing spaces. The value corresponding to these user-specified parameters must be a string that contains no control characters other than linefeed.

\section*{Format Support}

This table summarizes the types of images that i mwr it e can write.
\begin{tabular}{l|l}
\hline Format & Variants \\
\hline BMP & \begin{tabular}{l} 
8-bit uncompressed images with associated col ormap; \\
24-bit uncompressed images
\end{tabular} \\
\hline HDF & \begin{tabular}{l} 
8-bit raster image datasets, with or without associated col ormap; \\
24-bit raster image datasets; uncompressed or with RLE or J PEG compression
\end{tabular} \\
\hline J PEG & \begin{tabular}{l} 
Baseline J PEG images (8 or 24-bit) \\
Note: Indexed images are converted to RGB before writing out J PEG files, \\
because the J PEG format does not support indexed images.
\end{tabular} \\
\hline PCX & \begin{tabular}{l} 
8-bit images
\end{tabular} \\
\hline PNG & \begin{tabular}{l} 
1-bit, 2-bit, 4-bit, 8-bit, and 16-bit grayscale images; \\
8-bit and 16-bit grayscale images with al pha channels; \\
1-bit, 2-bit, 4-bit, and 8-bit indexed images; \\
24-bit and 48-bit truecolor images with or without alpha channels
\end{tabular} \\
\hline TIFF & \begin{tabular}{l} 
Baseline TIFF images, including 1-bit, 8-bit, and 24-bit uncompressed images; \\
1-bit, 8-bit, and 24-bit images with packbits compression; \\
1-bit images with CCITT 1D, Group 3, and Group 4 compression
\end{tabular} \\
\hline XWD & \begin{tabular}{l} 
8-bit ZPixmaps
\end{tabular} \\
\hline
\end{tabular}

\footnotetext{
Class Support Most of the supported image file formats store ui nt 8 data. PNG and TIF F additionally support ui nt 16 data. For grayscale and RGB images, if the data array is doubl e, the assumed dynamic range is \([0,1]\). The data array is automatically scaled by 255 before being written out as ui nt 8 . If the data array is ui nt 8 or ui nt 16 (PNG and TIFF only), then it is written out without scaling as ui nt 8 or ui nt 16, respectively.
}

Note If a logical double or ui nt 8 is written to a PNG or TIFF file, it is assumed to be a binary image and will be written with a bit depth of 1.

For indexed images, if the index array is doubl e, then the indices are first converted to zero-based indices by subtracting 1 from each element, and then they are written out as ui nt 8 . If the index array is ui nt 8 or ui nt 16 (PNG and TIFF only), then it is written out without modification as ui nt 8 or ui nt 16, respectively. When writing PNG files, you can override this behavior with the ' Bit Dept h' parameter; see the PNG table in this imwite reference for details.

\section*{Remarks imuite is a function in MATLAB.}

Example This example appends an indexed image \(X\) and its colormap map to an existing uncompressed multipage HDF file named fI ower s . hdf.
```

i mwr i te( X, m@p, ' fl ower s. hdf ' , ' Compr essi on' , ' none' , . . .
' W'iteMbde', ' append' )

```

See Also fwrite, infinfo, imead

\section*{ind2gray}

\section*{Purpose}

\section*{Syntax}

Description

Class Support

\section*{Example}

\section*{Algorithm}

\author{
See Also
}
\begin{tabular}{|c|c|}
\hline Purpose & Convert an indexed image to an RGB image \\
\hline Syntax & \(\mathrm{RGB}=\mathrm{i} \mathrm{nd} 2 \mathrm{rgb}(\mathrm{X}, \mathrm{n} ⿴ 囗 十 \mathrm{p})\) \\
\hline Description & RGB \(=\mathrm{i} n d 2 \mathrm{rgb}(\mathrm{X}, \mathrm{n} \not \pm \mathrm{p})\) converts the matrix X and corresponding col ormap map to RGB（truecolor）format． \\
\hline Class Support & \(X\) can be of class ui nt 8 ，ui nt 16 ，or doubl e．RGB is an mby－n－by－ 3 array of class double． \\
\hline See Also & i nd2gray，rgb2i nd \\
\hline
\end{tabular}

\section*{iptgetpref}
\begin{tabular}{|c|c|}
\hline Purpose & Get I mage Processing Tool box preference \\
\hline Syntax & val ue = i pt get pr ef ( pref name) \\
\hline Description & val ue \(=i\) pt get pr ef ( pr ef name) returns the value of the I mage Processing Tool box preference specified by the string pr ef name. Preferencenames are case insensitive and can be abbreviated. \\
\hline & i pt get pr ef without an input argument displays the current setting of all I mage Processing Tool box preferences. \\
\hline Example & val ue = i pt get pref ('I nฐ howAxesVi si ble' ) \\
\hline & val ue \(=\) \\
\hline & of \(f\) \\
\hline See Also & i ns how, i pt set pref \\
\hline
\end{tabular}
Purpose Set Image Processing Tool box preference
Syntax i pt set pr ef (pr ef name, val ue)
Description specified by the string pr ef name to val ue. The setting persists until the end of the current MATLAB session, or until you change the setting. (To make the value persist between sessions, put the command in your st art up. mfile.)
This table describes the available preferences. Note that the preference names are case insensitive and can be abbreviated.
\begin{tabular}{l|l}
\hline Preference Name & Values \\
\hline 'I nshowBor der' & ' I oose' (default) or 'tight'
\end{tabular}
If 'I mshowBor der ' is 'I oose' , i mshow displays the image with a border between the image and the edges of the figure window, thus leaving room for axes labels, titles, etc. If ' I mshowBor der ' is ' ti ght ' , i mshowadjusts the figure size so that the image entirely fills the figure. (However, there may still be a border if the image is very small, or if there are other objects besides the image and its axes in the figure.)
'InshowAxesVisi bl e' ' on' or ' of f' (default)
If 'I ns howAxesVi si bl e' is ' on' , i nshow displays the image with the axes box and tick labels. If ' I nshowAxes Vi si ble' is ' of \(f\) ', i mshow displays the image without the axes box and tick labels.
```

' I nshowTr uesi ze' ' aut o' (default) or ' manual '

```
If 'I nshowTr uesize' is ' manual ', i nshow does not call truesi ze. If'InshowTruesi ze' is ' aut o' , i ns howautomatically decides whether to call truesi ze. (i nshowcalls truesi ze if there will be no other objects in the resulting figure besides the image and its axes.) You can override this setting for an individual display by specifying the di spl ay_opt i on argument to inshow or you can call truesi ze manually after displaying the image.
' Truesi zeVar ni ng' ' on' (default) or ' of f '
If ' Tr uesi zeWar ni ng' is ' on' , the t ruesi ze function displays a warning if the image is too large to fit on the screen. (The entire image is still displayed, but at less than true size.) If
' Truesi zeWar ni ng' is ' of \(f\) ' , truesi ze does not display the warning. Note that this preference applies even when you call truesi ze indirectly, such as through ims how

\section*{iptsetpref}
i pt set pr ef ( pr ef name) displays the valid values for pref name.

\section*{Example}
i pt set pref('I nshowBor der',' ti ght')
See Also inshow, i pt get pref, truesize
axi s in the MATLAB Function Reference

\section*{Purpose \\ Compute inverse Radon transform}

\author{
Syntax \\ Description
}

I = iradon( P , t het a )
l = iradon(P, theta, interp,filter, d, n)
[ \(\mathrm{I}, \mathrm{h}\) ] = iradon(...)

I = ir adon( P , thet a) reconstructs the image I from projection data in the two-dimensional array \(P\). The columns of \(P\) are parallel beam projection data. i r adon assumes that the center of rotation is the center point of the projections, which is defined as ceil(size(P, 1)/2).
thet a describes the angles (in degrees) at which the projections were taken. It can be either a vector containing the angles or a scalar specifying D_t het a, the incremental angle between projections. If thet a is a vector, it must contain angles with equal spacing between them. If \(t\) het a is a scalar specifying D_t het a, the projections are taken at angles thet a = n*D_t het a, where \(m=0,1,2, \ldots\), si ze( \(P, 2\) ) - 1 . If the input is the empty matrix ([ ]), \(D_{\_} t\) het a defaults to 180/ si ze( \(\mathrm{P}, 2\) ).

I = ir adon( P , theta, interp, filter, \(\mathrm{d}, \mathrm{n}\) ) specifies parameters to use in the inverse Radon transform. You can specify any combination of the last four arguments. i r adon uses default values for any of these arguments that you omit.
i nt er p specifies the type of interpol ation to use in the backprojection. The available options are listed in order of increasing accuracy and computational complexity:
- ' nearest' - nearest neighbor interpolation
- 'I i near' - linear interpolation (default)
- 'spl ine' - spline interpolation
filter specifies the filter to use for frequency domain filtering. filter is a string that specifies any of the following standard filters:
- ' Ram Lak' - The cropped Ram-Lak or ramp filter (default). The frequency response of this filter is | f |. Because this filter is sensitive to noise in the projections, one of the filters listed below may be preferable. These filters multiply the Ram-Lak filter by a window that de-emphasizes high frequencies.
- ' Shepp- Logan' - The Shepp-Logan filter multiplies the Ram-Lak filter by a sinc function.
- ' Cosi ne' - The cosine filter multiplies the Ram-Lak filter by a cosine function.
- ' Hamming' - The Hamming filter multiplies the Ram-Lak filter by a Hamming window.
- ' Hann' - The Hann filter multiplies the Ram-Lak filter by a Hann window.
d is a scalar in the range \((0,1]\) that modifies the filter by rescaling its frequency axis. The default is 1 . If \(d\) is less than 1 , the filter is compressed to fit into the frequency range [0,d], in normalized frequencies; all frequencies aboved are set to 0 .
\(n\) is a scalar that specifies thenumber of rows and col umns in the reconstructed image. If \(n\) is not specified, the size is determined from the length of the projections.
```

n = 2*floor(size(P, 1)/(2*sqrt(2)))

```

If you specify n , i radon reconstructs a smaller or larger portion of the image, but does not change the scaling of the data. If the projections were calculated with the radon function, the reconstructed image may not be the same size as the original image.
\([\mathrm{l}, \mathrm{h}]=\mathrm{i}\) radon(... ) returns the frequency response of the filter in the vector h.

\section*{Class Support}

All input arguments must be of class doubl e. The output arguments are of class double.

\section*{Example}
```

P = phant on( 128);
R = radon(P, 0: 179);
I = iradon( R, 0: 179,' near est',' Hann' );
i mshow(P)
figure, imshow(l)

```


Algorithm

See Also radon, phant om
References the FFT.
i r adon uses thefiltered backprojection algorithm to perform the inverse Radon transform. The filter is designed directly in the frequency domain and then multiplied by the FFT of the projections. The projections are zero-padded to a power of 2 before filtering to prevent spatial domain aliasing and to speed up
Purpose Return true for a binary image

\section*{Syntax \\ \(\mathrm{flag}=\mathrm{i} \operatorname{sbw}(\mathrm{A})\)}

Description
\(\mathrm{flag}=\mathrm{i} \operatorname{sbw}(\mathrm{A})\) returns 1 if A is a binary image and 0 otherwise.
i sbwuses these criteria to decide if \(A\) is a binary image:
- If A is of class doubl e, all values must be either 0 or 1 , the logical flag must be on, and the number of dimensions of A must be 2 .
- If A is of class ui nt 8, the logical flag must be on, and the number of dimensions of A must be 2 .
- If A is of class ui nt 16, it is not a binary image. (The tool box does not support ui nt 16 binary images.)

Note A four-dimensional array that contains multiple binary images returns 0 , not 1 .

\author{
Class Support A can be of class ui nt 8, ui nt 16, or doubl e. \\ See Also i si nd, i sgray, i srgb
}
\begin{tabular}{|c|c|}
\hline Purpose & Return true for intensity image \\
\hline Syntax & \(\mathrm{flag}=\mathrm{isgray}(\mathrm{A})\) \\
\hline Description & \begin{tabular}{l}
fl ag \(=\mathrm{i} \operatorname{sgray}(\mathrm{A})\) returns 1 if Ais a grayscal i sgr ay uses these criteria to decide if \(A\) is an \\
- If \(A\) is of class doubl e, all values must be in of dimensions of A must be 2 . \\
- If \(A\) is of class ui nt 16 or ui nt 8 , the number \\
Note A four-dimensional array that contai returns 0 , not 1 .
\end{tabular} \\
\hline Class Support & A can be of class ui nt 8 , ui nt 16 , or doubl e. \\
\hline See Also & i sbw, i si nd, i srgb \\
\hline
\end{tabular}

\section*{isind}

\section*{Purpose Return true for an indexed image}

\section*{Syntax \\ fl ag \(=\mathrm{i}\) sind( A\()\)}

Description
fl ag \(=\mathrm{i}\) sind( A\()\) returns 1 if A is an indexed image and 0 otherwise.
i si nd uses these criteria to determine if \(A\) is an indexed image:
- If \(A\) is of class doubl e, all values in A must be integers greater than or equal to 1 , and the number of dimensions of \(A\) must be 2 .
- If \(A\) is of class ui nt 8 , its logical flag must be off, and the number of dimensions of A must be 2 .
- If \(A\) is of class ui nt 16 , the number of dimensions of \(A\) must be 2 .

Note A four-dimensional array that contains multiple indexed images returns 0 , not 1 .

\section*{Class Support \\ A can be of class ui nt 8 , ui nt 16 , or doubl e.}

\section*{See Also}
\begin{tabular}{|c|c|}
\hline Purpose & Return true for an RGB image \\
\hline Syntax & \(\mathrm{flag}=\mathrm{isrgb}(\mathrm{A})\) \\
\hline \multirow[t]{2}{*}{Description} & \begin{tabular}{l}
\(\mathrm{fl} \mathrm{ag}=\mathrm{i} \operatorname{srgb}(\mathrm{A})\) returns 1 if A is an RGB truecolor image and 0 otherwise. i srgb uses these criteria to determine if \(A\) is an RGB image: \\
- If \(A\) is of class doubl e, all values must be in the range [0,1], and A must be mby-n-by-3. \\
- If \(A\) is of class ui nt 16 or ui nt \(8, A\) must be maby-n-by-3.
\end{tabular} \\
\hline & Note A four-dimensional array that contains multipleRGB images returns 0 , not 1. \\
\hline Class Support & A can be of class ui nt 8 , ui nt 16 , or doubl e. \\
\hline See Also & i sbw, i sgray, i si nd \\
\hline
\end{tabular}

\section*{Purpose \\ Construct a lookup table for use with appl yl ut}
Syntax \(\quad\)\begin{tabular}{rl} 
I ut & \(=\operatorname{makel} u t(f\) un, \(n)\) \\
I ut & \(=\operatorname{makel}\) ut \((f\) un, \(n, P 1, P 2, \ldots)\)
\end{tabular}

Description

Class Support
Example at a time, and constructing either a 16-element vector (for 2-by-2 consists of the output from \(f\) un for each possible neighborhood.

I ut = nakel ut ( f un, \(\mathrm{n}, \mathrm{P} 1, \mathrm{P} 2, \ldots\) ) passes the additional parameters P1, P2, ... , to fun.

I ut is returned as a vector of class doubl e.
In this example, the function returns 1 (true) if the number of 1 's in the

I ut = makel ut ( f un, n ) returns a lookup table for use with appl yl ut. f un is either a string containing the name of a function or an inline function object. The function should take a 2-by-2 or 3-by-3 matrix of 1's and 0's as input and return a scalar. \(n\) is either 2 or 3 , indicating the size of theinput tof un. nakel ut creates I ut by passing all possible 2-by-2 or 3-by-3 neighborhoods to f un, one neighborhoods) or a 512-element vector (for 3-by-3 neighborhoods). The vector neighborhood is 2 or greater, and returns 0 (false) otherwise. makel ut then uses the function to construct a lookup table for 2-by-2 neighborhoods.
```

f = inline('sum(x(:)) >= 2');
l ut = makel ut(f, 2)
| ut =

```
0
0
0
1
0
1
1
1
0
1
1
1

See Also appl yl ut

Purpose Convert a matrix to a grayscale intensity image
```

Syntax
I = mat $2 \operatorname{gray}(A,[\operatorname{amin} \operatorname{amax}])$
I = mat $2 \mathrm{gray}(\mathrm{A})$

```

Description

Class Support The input array A and the output image I are of class doubl e.

\section*{Example}
 The returned matrix I contains values in the range 0 (black) to 1.0 (full intensity or white). amin and amax are the values in A that correspond to 0 and 1.0 in 1 .
\(I=\) mat \(2 g r a y(A)\) sets the values of amin and amax to the minimum and maximum values in \(A\).
```

| = imread('rice.tif');
J = filter2(fspecial('sobel'),I);
K = mat 2gray(J);
i mshow(I)
figure, i mshow( K)

```


\footnotetext{
See Also
gray2i nd
}
\begin{tabular}{|c|c|}
\hline Purpose & Compute the mean of the elements of a matrix \\
\hline Syntax & \(\mathrm{b}=\operatorname{mean2}(\mathrm{A})\) \\
\hline Description & \(b=\operatorname{mean2}(A)\) computes the mean of the values in \(A\). \\
\hline Class Support & Ais an array of class doubl e or of any integer class. b is a scalar of class double. \\
\hline Algorithm & mean2 computes the mean of an array \(A\) using mean( \(\mathrm{A}(:))\). \\
\hline See Also & st d2 \\
\hline & mean, st d in the MATLAB Function Reference \\
\hline
\end{tabular}
Purpose Perform two-dimensional median filtering
\begin{tabular}{|c|c|}
\hline Syntax & \(B=\operatorname{medfilt~} 2(A,[m \mathrm{n}])\) \\
\hline & \(B=\) medfilt \(2(A)\) \\
\hline & \(B=\) medfilt \(2(A, ' i n d e x e d ' ~\) \\
\hline
\end{tabular}

\(B=\) medfilt2(A) performs median filtering of the matrix A using the default 3-by-3 neighborhood.
\(B=\) medfilt 2( \(A\), 'indexed',\(\ldots\) ) processes \(A\) as an indexed image, padding with zeros if the class of \(A\) is ui nt 8 , or ones if the class of \(A\) is doubl \(e\).

Class Support The input image A can be of class ui nt 8, ui nt 16, or doubl e (unless the ' i ndexed' syntax is used, in which case A cannot be of class ui nt 16). The output image \(B\) is of the same class as \(A\).

\section*{Remarks}

If the input image \(A\) is of class ui nt 8, all of the output values are returned as ui nt 8 integers. If the number of pixels in the neighborhood (i.e., n*n) is even, some of the median values may not be integers. In these cases, the fractional parts are discarded.

For example, suppose you call medf ilt 2 using 2-by-2 neighborhoods, and the input image is a ui nt 8 array that includes this neighborhood.

15
48
medf i I t 2 returns an output value of 4 for this neighborhood, although the true median is 4.5.

Example

Algorithm
medfilt 2 uses ordfilt 2 to perform the filtering.

\section*{See Also}

Reference using medfilt 2 .
```

l = imead('ei ght.tif');
J = i mmoi se(I,'salt \& pepper',0.02);
K = medfilt2(J);
i mshow(J)
figure, i mshow(K)

```

filter 2, or dfilt 2, wi ener 2
[1] Lim, J ae S. Two-Dimensional Signal and Image Processing. Englewood

This example adds salt and pepper noise to an image, then restores the image
 Cliffs, NJ : Prentice Hall, 1990. pp. 469-476.
\begin{tabular}{|c|c|}
\hline Purpose & Display multiple image frames as a rectangular montage \\
\hline Syntax & \begin{tabular}{l}
mont age(I) \\
mont age( BW) \\
mont age( \(X\), map) \\
mont age( RGB) \\
h = montage(...)
\end{tabular} \\
\hline Description & \begin{tabular}{l}
mont age displays all of the frames of a multiframe image array in a single image object, arranging the frames so that they roughly form a square. \\
mont age(I) displays the \(k\) frames of the intensity image array I .1 is maby-n-by-1-by-k. \\
mont age( BW displays the \(k\) frames of the binary image array BW BWis maby-n-by-1-by-k. \\
mont age ( \(X, m p\) ) displays the \(k\) frames of the indexed image array \(X\), using the col ormap map for all frames. \(X\) is mby-n-by-1-by-k. \\
mont age( RGB) displays the \(k\) frames of the truecol or image array RGB. RGB is maby-n-by-3-by-k. \\
\(h=\) nont age (. . . ) returns the handle to the image object.
\end{tabular} \\
\hline Class Support & The input image can be of class ui nt 8 , ui nt 16 , or doubl e. \\
\hline Example & I oad mi mont age( D, map) \\
\hline
\end{tabular}


See Also
i movie
Purpose Perform general sliding-neighborhood operations
Syntax \(B=n l f i l t e r(A,[m n], f u n)\)
\(B=\) nlfilter (A, [mn],fun, P1, P2, ... )
\(B=n l\) filter \((A, ' i n d e x e d ', \ldots)\)
Description
Class SupportThe input image A can be of any class supported by \(f\) un. The class of \(B\) dependson the class of the output from \(f\) un.
Remarks
Example
See Also ..... bl kproc, colfilt

See Also bl kproc, col filt
nl filt er can take a long time to process large images. In some cases, the colfilt function can perform the same operation much faster.
f un can be a f uncti on_handl e, created using @ This example produces the same result as calling medfilt 2 with a 3-by-3 neighborhood.
B = nlfilter(A, [3 3], @nf un);
where myf un is an \(M\)-file containing
```

function scal ar = myfun(x)
scal ar = medi an(x(:));

```
fun can also be an inline object. The example above can be written as
fun = inline(' medi an(x(:))');

\section*{Purpose Convert NTSC values to RGB color space}
\begin{tabular}{ll} 
Syntax & rgbmap \(=n t \operatorname{sc} 2 r g b(\) yi qmap \()\) \\
& \(R G B=n t s c 2 r g b(Y I Q)\)
\end{tabular}

Description rgbmap \(=n t s c 2 r g b(\) yi qmap) converts the mby-3 NTSC (television) color values in yi qmap to RGB col or space. If yi qmap is mby-3 and contains the NTSC luminance \((Y)\) and chrominance ( \(I\) and \(Q\) ) color components as columns, then rgbmap is an mby-3 matrix that contains the red, green, and blue values equivalent to those colors. Both rgbnap and yi qmap contain intensities in the range 0 to 1.0. The intensity 0 corresponds to the absence of the component, while the intensity 1.0 corresponds to full saturation of the component.

RGB \(=n t s c 2 r g b(Y I Q)\) converts theNTSC image YI Qto the equivalent truecolor image RGB.
nt sc2rgb computes the RGB values from the NTSC components using
\[
\left[\begin{array}{l}
\mathrm{R} \\
\mathrm{G} \\
\mathrm{~B}
\end{array}\right]=\left[\begin{array}{rrr}
1.000 & 0.956 & 0.621 \\
1.000 & -0.272 & -0.647 \\
1.000 & -1.106 & 1.703
\end{array}\right]\left[\begin{array}{l}
\mathrm{Y} \\
\mathrm{I} \\
\mathrm{Q}
\end{array}\right]
\]

Class Support The input image or colormap must be of class doubl e. The output is of class doubl e.

See Also rgb2nt sc, rgb2i nd, ind2rgb, ind2gray
\begin{tabular}{|c|c|}
\hline Purpose & Perform two-dimensional order-statistic filtering \\
\hline Syntax & \[
\begin{aligned}
& B=\operatorname{ordfilt} 2(A, \text { order, donai } n) \\
& B=\operatorname{ordfilt} 2(A, \text { order, domiai } n, S) \\
& B=\operatorname{ordfilt} 2(\ldots, \text { padopt })
\end{aligned}
\] \\
\hline Description & \begin{tabular}{l}
\(B=\operatorname{ordfilt2}(A\), order, domai \(n\) ) replaces each element in \(A\) by the order-th element in the sorted set of neighbors specified by the nonzero elements in domain. \\
\(B=\) or dfilt2(A, or der, domai \(n, S\) ), where \(S\) is the same size as domai \(n\), uses the values of \(S\) corresponding to the nonzero values of domai \(n\) as additive offsets. \\
\(\mathrm{B}=\) ordfilt2(..., padopt) controls how the matrix boundaries are padded. Set padopt to 'zer os' (the default), or 'symmetri c'. If padopt is 'zer os', A is padded with zeros at the boundaries. If padopt is 'symmet ric', A is symmetrically extended at the boundaries.
\end{tabular} \\
\hline Class Support & A can be of class ui nt 8 , ui nt 16 , or doubl e. Theclass of \(B\) is the sameas the class of \(A\), unless the additive offset form of or df i I t 2 is used, in which case the class of \(B\) is doubl \(e\). \\
\hline Remarks & domai \(n\) is equivalent to the structuring element used for binary image operations. It is a matrix containing only 1's and 0's; the 1's define the neighborhood for the filtering operation. \\
\hline & For example, \(\mathrm{B}=\mathrm{ordfilt} 2(\mathrm{~A}, 5\), ones( 3,3 ) ) implements a 3-by-3 median filter; \(B=\) or dfilt \(2(A, 1\), ones \((3,3)\) ) implements a 3-by-3 minimum filter; and \(B=\) ordfilt \(2(A, 9\), ones ( 3,3\()\) ) implements a 3-by-3 maximum filter. \(B=\) ordfilt2(A, 1, [ \(010 ; 101 ; 010]\) ) replaces each element in \(A\) by the minimum of its north, east, south, and west neighbors. \\
\hline & The syntax that includes \(S\) (the matrix of additive offsets) can be used to implement grayscale morphological operations, including grayscale dilation and erosion. \\
\hline See Also & medfilt 2 \\
\hline
\end{tabular}

Reference
[1] Haralick, Robert M., and Linda G. Shapiro. Computer and Robot Vision, VolumeI. Addison-Wesley, 1992.
Purpose Generate a head phantom image
Syntax \begin{tabular}{ll}
\(P=\) phant om \((\operatorname{def}, n)\) \\
& \(P=\) phantom \(E, n)\) \\
& \([P, E]=\) phant on( \(\ldots)\)
\end{tabular}

Description \(\quad P=\) phant om def,\(n\) ) generates an image of a head phantom that can be used to test the numerical accuracy of radon and i radon or other two-dimensional reconstruction algorithms. \(P\) is a grayscale intensity image that consists of one large ellipse (representing the brain) containing several smaller ellipses (representing features in the brain).
def is a string that specifies the type of head phantom to generate. Valid values are:
- ' Shepp- Logan' - a test image used widely by researchers in tomography.
- ' Mbdi fi ed Shepp- Logan' (default) - a variant of the Shepp-Logan phantom in which the contrast is improved for better visual perception.
\(n\) is a scalar that specifies the number of rows and columns in P. If you omit the argument, \(n\) defaults to 256 .
\(P=\) phant om \(E, n\) ) generates a user-defined phantom, where each row of the matrix E specifies an ellipse in the image. E has six columns, with each column containing a different parameter for the ellipses. This table describes the columns of the matrix.
\begin{tabular}{l|l|l}
\hline Column & Parameter & Meaning \\
\hline Column 1 & A & \begin{tabular}{l} 
Additive intensity value of the \\
ellipse
\end{tabular} \\
\hline Column 2 & a & \begin{tabular}{l} 
Length of the horizontal semi-axis of \\
the ellipse
\end{tabular} \\
\hline Column 3 & b & \begin{tabular}{l} 
Length of the vertical semi-axis of \\
the ellipse
\end{tabular} \\
\hline Column 4 & x0 & \begin{tabular}{l} 
x-coordinate of the center of the \\
ellipse
\end{tabular} \\
\hline
\end{tabular}
\begin{tabular}{l|l|l}
\hline Column & Parameter & Meaning \\
\hline Column 5 & y0 & \begin{tabular}{l} 
y-coordinate of the center of the \\
ellipse
\end{tabular} \\
\hline Column 6 & phi & \begin{tabular}{l} 
Angle (in degrees) between the \\
horizontal semi-axis of the ellipse \\
and the \(x\)-axis of the image
\end{tabular} \\
\hline
\end{tabular}

For purposes of generating the phantom, the domains for the \(x\) - and \(y\)-axes span \([-1,1]\). Columns 2 through 5 must be specified in terms of this range.
[ P, E] = phant ont . . . ) returns the matrix E used to generate the phantom.

\section*{Class Support \\ All inputs must be of class doubl e. All outputs are of class doubl e. \\ Remarks \begin{tabular}{l} 
For any given pixel in the output image, the pixel 's value is equal to the sum of \\
the additive intensity values of all ellipses that the pixel is a part of. If a pixel \\
is not part of any ellipse, its value is 0 . \\
The additive intensity value \(A\) for an ellipse can be positive or negative; if it is \\
negative, the ellipse will be darker than the surrounding pixels. Note that, \\
depending on the values of \(A\), some pixels may have values outside the range \\
{\([0,1]\).}
\end{tabular}}

Example
P = phant omf ' Mbdi fied Shepp- Logan', 200);
i mshow ( P )


\section*{Reference}

See Also
[1] J ain, Anil K. Fundamentals of Digital Image Processing. Englewood Cliffs, NJ : Prentice Hall, 1989. p. 439.
radon, i radon
Purpose Display information about image pixels
Syntax pi xval on ..... pi xval off
pi xval
pi xval (fig, option)
Purpose
See Also i mpi xel , i mprof ile
Purpose
Syntax
Description

Perform quadtree decomposition
```

S = qt decomp(I )
S = qt decomp(I , threshol d)
S = qt decomp(I , threshol d, mi ndi m)
S = qt decomp( I , t hr eshol d, [ mindi m maxdi m] )
S = qt decomp(I , fun)
S = qt decomp(I, f un, P1, P2, . . )

```
qt decomp divides a square image into four equal-sized square blocks, and then tests each block to see if it meets some criterion of homogeneity. If a block meets the criterion, it is not divided any further. If it does not meet the criterion, it is subdivided again into four blocks, and thetest criterion is applied to those blocks. This process is repeated iteratively until each block meets the criterion. The result may have blocks of several different sizes.
\(\mathrm{S}=\mathrm{qt}\) decomp(I) performs a quadtree decomposition on the intensity image I , and returns thequadtree structure in the sparsematrix S . If \(\mathrm{S}(\mathrm{k}, \mathrm{m})\) is nonzero, then ( \(k, m\) ) is the upper-left corner of a block in the decomposition, and the size of the block is given by \(\mathrm{S}(\mathrm{k}, \mathrm{m})\). By default, qt decomp splits a block unless all elements in the block are equal.
\(\mathrm{S}=\mathrm{qt}\) decomp( \(\mathrm{I}, \mathrm{threshol} \mathrm{d}\) ) splits a block if the maximum value of the block elements minus the minimum value of the block elements is greater than t hr eshol d. threshol d is specified as a value between 0 and 1 , even if I is of class ui nt 8 or ui nt 16. If I is ui nt 8 , the threshold value you supply is multiplied by 255 to determine the actual threshold to use; if I is ui nt 16, the threshold value you supply is multiplied by 65535.
\(\mathrm{S}=\mathrm{qt}\) decomp(I, threshol d, mindim) will not produce blocks smaller than m ndi m even if the resulting blocks do not meet the threshold condition.
\(\mathrm{S}=\mathrm{qt}\) decomp(l,threshol d, [ min ndimman mill not produce blocks smaller than min ndi mor larger than maxdi m Blocks larger than naxdi maresplit even if they meet the threshold condition. maxdi man ndi mmust be a power of 2 .
\(\mathrm{S}=\mathrm{qt}\) decomp(I, f un) uses the function f un to determine whether to split a block. qt decomp calls \(f\) un with all the current blocks of size mby-mstacked into an mby-mby-k array, wherek is the number of \(m\) mby-mblocks. \(f\) un should return

\section*{qtdecomp}
a k-element vector, containing only 1's and 0's, where 1 indicates that the corresponding block should be split, and 0 indicates it should not be split. (F or example, if \(k\) ( 3 ) is 0 , the third \(m b y\)-mblock should not be split.) f un can be a f unct i on_handl e, created using @ or an inline object.

S = qt decomp(I, f un, P1, P2, . . . ) passes P1, P2, . . . , as additional arguments to \(f\) un.

Class Support For the syntaxes that do not include a function, the input image can be of class ui nt 8 , ui nt 16, or doubl e. F or the syntaxes that include a function, the input image can be of any class supported by the function. The output matrix is always of class sparse.
Remarks \begin{tabular}{l} 
qt decomp is appropriate primarily for square images whose dimensions are a \\
power of 2, such as 128-by-128 or 512-by-512. These images can be divided \\
until the blocks are as small as 1-by-1. If you use qt decomp with an image \\
whose dimensions are not a power of 2, at some point the blocks cannot be \\
divided further. For example, if an image is 96-by-96, it can be divided into \\
blocks of size 48-by-48, then 24-by-24, 12-by-12, 6-by-6, and finally 3-by-3. No \\
further division beyond 3-by-3 is possible. To process this image, you must set \\
min ndi mto 3 (or to 3 times a power of 2); if you are usingthe syntax that includes \\
a function, the function must return 0 at the point when the block cannot be \\
divided further.
\end{tabular}
\begin{tabular}{|c|c|c|c|c|c|c|c|c|}
\hline Example & \(1=[1\) & 1 & 1 & 1 & 2 & 3 & 6 & 6 \\
\hline & 1 & 1 & 2 & 1 & 4 & 5 & 6 & 8 \\
\hline & 1 & 1 & 1 & 1 & 10 & 15 & 7 & 7 \\
\hline & 1 & 1 & 1 & 1 & 20 & 25 & 7 & 7 \\
\hline & 20 & 22 & 20 & 22 & 1 & 2 & 3 & 4 \\
\hline & 20 & 22 & 22 & 20 & 5 & 6 & 7 & 8 \\
\hline & 20 & 22 & 20 & 20 & 9 & 10 & 11 & 12 \\
\hline & 22 & 22 & 20 & 20 & 13 & 14 & 15 & 16]; \\
\hline
\end{tabular}
full (S)
\[
\begin{array}{rlllllll}
\text { ans }= & & & & & & & \\
& & & 0 & 2 & 0 & 2 & 0 \\
4 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 1 & 2 & 0 \\
0 & 0 & 0 & 0 & 1 & 1 & 0 \\
0 & 0 & 0 & 0 & 1 & 1 & 0 & 0 \\
4 & 0 & 0 & 0 & 2 & 0 & 2 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 2 & 0 & 2 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0
\end{array}
\]

\footnotetext{
See Also
qt get bl k , qt set bl k
}

\section*{Purpose \\ Get block values in quadtree decomposition}
Syntax \(\quad\)\begin{tabular}{rl}
{\([\) val \(s, r, c]\)} & \(=\) qt get bl \(k(I, S\), di \(m)\) \\
{\([\) val \(s, i d x]\)} & \(=\) qt get bl \(k(I, S, d i m)\)
\end{tabular}

Description

Class Support I can be of class ui nt 8, ui nt 16, or doubl e. S is of class sparse.
Remarks The ordering of the blocks in val s matches the columnwise order of the blocks in I . F or example, if val s is 4-by-4-by-2, val \(s(:,:, 1)\) contains the values from thefirst 4-by-4 block in I , and val s(:, , 2) contains the values from the second 4-by-4 block.

This example continues the qt decomp example.
```

[ val s, r, c] = qt get bl $k(1, S, 4)$
vals(:,:,1) =

```
\begin{tabular}{llll}
1 & 1 & 1 & 1 \\
1 & 1 & 2 & 1 \\
1 & 1 & 1 & 1 \\
1 & 1 & 1 & 1
\end{tabular}

\section*{qtgetblk}
\[
\begin{aligned}
& \text { val s(:,:,2) = } \\
& \begin{array}{llll}
20 & 22 & 20 & 22
\end{array} \\
& \begin{array}{llll}
20 & 22 & 22 & 20
\end{array} \\
& 20 \quad 22 \quad 20 \quad 20 \\
& 22 \quad 22 \quad 20 \\
& r= \\
& 1 \\
& 5 \\
& \text { c }=
\end{aligned}
\]

Purpose Set block values in quadtree decomposition
Syntax J = qt set bl \(k(1, S\), di \(m\) val \(s)\)
Description \(\quad J=q t\) set bl \(k(I, S\), di \(m\) val s) replaces each di \(m b y\)-di mblock in the quadtree decomposition of I with the corresponding di mby-di mblock in val s. S is the sparse matrix returned by qt decomp; it contains the quadtree structure. val s is a di mby-di mby-k array, where \(k\) is the number of di mby-di mblocks in the quadtree decomposition.

Class Support I can be of class ui nt 8, ui nt 16, or doubl e. S is of class sparse.
Remarks

Example
This example continues the qt get bl ock example.
```

newals = cat(3, zeros(4), ones(4));
J = qtset bl k(I, S, 4, newal s)
J =

```
\begin{tabular}{rlllrrrr}
0 & 0 & 0 & 0 & 2 & 3 & 6 & 6 \\
0 & 0 & 0 & 0 & 4 & 5 & 6 & 8 \\
0 & 0 & 0 & 0 & 10 & 15 & 7 & 7 \\
0 & 0 & 0 & 0 & 20 & 25 & 7 & 7 \\
1 & 1 & 1 & 1 & 1 & 2 & 3 & 4 \\
1 & 1 & 1 & 1 & 5 & 6 & 7 & 8 \\
1 & 1 & 1 & 1 & 9 & 10 & 11 & 12 \\
1 & 1 & 1 & 1 & 13 & 14 & 15 & 16
\end{tabular}

See Also qt decomp, qt get bl k

\section*{radon}

\section*{Purpose Compute Radon transform}

\section*{Syntax \\ Description}

Remarks

Example

Class Support I can be of class doubl e or of any integer class. All other inputs and outputs are of class doubl e.
\(R=r\) adon( 1, thet \(a)\)
\(\mathrm{R}=\mathrm{radon}(\mathrm{I}, \mathrm{thet} \mathrm{a}, \mathrm{n})\)
[ \(R, x p]=r a d o n(\ldots)\)
The radon function computes the Radon transform, which is the projection of the image intensity along a radial line oriented at a specified angle.
\(R=r\) adon( \(I\), thet a) returns the Radon transform of the intensity image I for the angle thet a degrees. If \(t\) het a is a scalar, the result \(R\) is a column vector containing the Radon transform for thet a degrees. If \(t\) het a is a vector, then \(R\) is a matrix in which each column is the Radon transform for one of the angles in \(t\) het a. If you omit \(t\) het a, it defaults to 0:179.
\(R=r\) adon( 1 , thet \(\mathrm{a}, \mathrm{n}\) ) returns a Radon transform with the projection computed at \(n\) points. \(R\) has \(n\) rows. If you do not specify \(n\), the number of points at which the projection is computed is
```

2* cei I (nor m( si ze(I ) -fl oor(( si ze(I ) - 1)/ 2) -1) ) +3

```

This number is sufficient to compute the projection at unit intervals, even along the diagonal.
[ R, xp] = radon( . . . ) returns a vector xp containing the radial coordinates corresponding to each row of R .

The radial coordinates returned in \(x p\) are the values along the \(x^{\prime}\)-axis, which is oriented at \(t\) het a degrees counterclockwise from the \(x\)-axis. The origin of both axes is the center pixel of the image, which is defined as
floor((si ze(1)+1)/2)
For example, in a 20-by-30 image, the center pixel is \((10,15)\).
i pt set pref('I nฐhowAxesVi si bl e', ' on' )
| = zeros(100, 100);
\(I(25: 75,25: 75)=1\);
```

thet a = 0: 180;
[ R, xp] = radon(I, thet a);
i nshow(t het a, xp, R, [ ], ' not ruesi ze' ), col ormap( hot ), col orbar

```


\section*{See Also ir radon, phant om}

References Bracewell, Ronald N. Two-Dimensional Imaging. Englewood Cliffs, NJ : Prentice Hall, 1995. pp. 505-537.

Lim, J ae S. Two-Dimensional Signal and Image Processing. Englewood Cliffs, NJ : Prentice Hall, 1990. pp. 42-45.

\section*{rgb2gray}
\begin{tabular}{|c|c|}
\hline Purpose & Convert an RGB image or colormap to grayscale \\
\hline Syntax & \[
\begin{aligned}
& I=r g b 2 g r a y(R G B) \\
& \text { newmp }=r g b 2 g r a y(m a p)
\end{aligned}
\] \\
\hline \multirow[t]{3}{*}{Description} & rgb2gr ay converts RGB images to grayscale by eliminating the hue and saturation information while retaining the luminance. \\
\hline & I = rgb2gray(RGB) converts the truecolor image RGB to the grayscale intensity imagel. \\
\hline & newnmp = rgb2gr ay (map) returns a grayscale colormap equivalent to map. \\
\hline Class Support & If the input is an RGB image, it can be of class ui nt 8, ui nt 16, or doubl e; the output image I is of the same class as the input image. If the input is a colormap, the input and output colormaps are both of class doubl e. \\
\hline Algorithm & rgb2gr ay converts the RGB values to NTSC coordinates, sets the hue and saturation components to zero, and then converts back to RGB color space. \\
\hline See Also & i nd2gray, nt sc2rgb, rgb2i nd, rgb2nt sc \\
\hline
\end{tabular}

\section*{Purpose}
\begin{tabular}{ll} 
Syntax & hsvmap \(=r g b 2 h s v(r g b m a p)\) \\
& \(H S V=r g b 2 h s v(R G B)\)
\end{tabular}

Description hsvmap \(=\) rgb2hsv( \(r\) gbmap) converts the mby-3 RGB values in RGB to HSV color space. hsvmap is an mby-3 matrix that contains the hue, saturation, and value components as col umns that are equivalent to the colors in the RGB colormap. Both rgbmap and hsvmap are of class doubl e and contain values in the range 0 to 1.0.

HSV \(=\) rgb2hsv( RGB) converts the truecolor image RGB to the equivalent HSV image HSV.

Class Support If the input is an RGB image, it can be of class ui nt 8, ui nt 16, or doubl e; the output image is of class doubl e. If the input is a col ormap, the input and output colormaps are both of class doubl e.
\(r g b 2 h s v\) is a function in MATLAB.
See Also hsv2rgb, rgbpl ot
col or map in the MATLAB Function Reference

Convert an RGB image to an indexed image
\[
\begin{aligned}
& {[X, n \boxplus p]=r g b 2 i \operatorname{nd}(\text { RGB, tol })} \\
& {[X, n \boxplus p]=r g b 2 i \operatorname{nd}(\text { RGB, } n)} \\
& X=r g b 2 i \operatorname{nd}(\text { RGB, } n \not a p) \\
& {[\ldots]=r g b 2 i \operatorname{nd}(\ldots, \text { di ther_opt } i \text { on })}
\end{aligned}
\]

Purpose
Syntax

Description

\section*{Class Support}

Remarks

The input image can be of class ui nt 8 , ui nt 16 , or doubl e. The output image is of class ui nt 8 if the length of map is less than or equal to 256 . It is doubl e otherwise.

If you specify \(t\) ol, \(\mathrm{rgb2i}\) nd uses uniform quantization to convert the image. This method involves cutting the RGB col or cube into smaller cubes of length tol. For example, if you specify a tol of 0.1, the edges of the cubes are one-tenth the length of the RGB cube. The total number of small cubes is
\[
n=(f l \text { oor }(1 / t \mathrm{ol})+1) \wedge 3
\]

Each cube represents a single color in the output image. Therefore, the maximum length of the colormap is \(n\). rgb2i nd removes any colors that don't appear in the input image, so the actual colormap may be much smaller than \(n\).

If you specify \(n\), rgb2i nd uses minimum variance quantization. This method involves cutting the RGB col or cube into smaller boxes (not necessarily cubes) of different sizes, depending on how the col ors are distributed in the image. If the input image actually uses fewer colors than the number you specify, the output colormap is also smaller.

If you specify map, rgb2i nd uses colormap mapping, which involves finding the colors in map that best match the colors in the RGB image.

\section*{Example}
```

RGB = imead('fl owers.tif');
[ X, m\&p] = rgb2i nd(RGB, 128);
i mshow( X, map)

```


See Also cmuni que, di ther, i mapprox, i nd2rgb, rgb2gray

\section*{rgb2ntsc}

\section*{Purpose Convert RGB values to NTSC color space}
\begin{tabular}{ll} 
Syntax & yi qmap \(=r g b 2 n t s c(r g b m a p)\) \\
& YI Q \(=r g b 2 n t s c(R G B)\)
\end{tabular}

Description yi qnap \(=r\) gb2nt sc( \(r\) gbmap) converts the mby-3 RGB values in rbgmap to NTSC color space. yi qmap is an mby-3 matrix that contains the NTSC luminance ( Y ) and chrominance (I and Q) col or components as col umns that are equivalent to the colors in the RGB colormap.

YI \(\mathrm{Q}=\mathrm{rgb2ntsc}(\) RGB \()\) converts thetruecol or image RGB to the equivalent NTSC image YI Q.
rgb2nt sc defines the NTSC components using
\[
\left[\begin{array}{l}
\mathrm{Y} \\
\mathrm{I} \\
\mathrm{Q}
\end{array}\right]=\left[\begin{array}{rrr}
0.299 & 0.587 & 0.114 \\
0.596 & -0.274 & -0.322 \\
0.211 & -0.523 & 0.312
\end{array}\right]\left[\begin{array}{l}
\mathrm{R} \\
\mathrm{G} \\
\mathrm{~B}
\end{array}\right]
\]

\section*{Class Support If the input is an RGB image, it can be of class ui nt 8, ui nt 16, or doubl e; the output image is of class doubl e. If theinput is a col ormap, theinput and output colormaps are both of class doubl e. \\ Remarks \\ In the NTSC col or space, the luminance is the grayscale signal used to display pictures on monochrome (black and white) tel evisions. The other components carry the hue and saturation information.}

See Also
nt sc2rgb, rgb2i nd, i nd2rgb, i nd2gray
\begin{tabular}{|c|c|}
\hline Purpose & Convert RGB values to YCbCr color space \\
\hline \multirow[t]{2}{*}{Syntax} & ycbermap = rgb2ycbcr (rgbmap) \\
\hline & YCBCR \(=\) rgb2ycbcr( RGB ) \\
\hline \multirow[t]{4}{*}{Description} & ycbornap \(=\) rgb2ycbcr ( rgbmap ) converts the RGB values in rbgnmp to the \\
\hline & YCbCr col or space. ycbcr map is an mby-3 matrix that contains the YCbCr luminance \((\mathrm{Y})\) and chrominance ( Cb and Cr ) color components as columns. \\
\hline & Each row represents the equivalent color to the corresponding row in the RGB colormap. \\
\hline & YCBCR \(=\) rgb2ycbcr( RGB) converts the truecolor image RGB to the equivalent image in the YCbCr color space. \\
\hline Class Support & If the input is an RGB image, it can be of class ui nt 8 , ui nt 16, or doubl e; the output image is of the same class as the input image. If the input is a col ormap, the input and output colormaps are both of class doubl e. \\
\hline See Also &  \\
\hline
\end{tabular}

\section*{rgbplot}

\section*{Purpose Plot colormap}

\section*{Syntax rgbpl ot (map)}

Description rgbpl ot ( \(n \not a p\) ) plots the three columns of map, where map is an \(m b y-3\) col ormap matrix. rgbpl ot draws the first column in red, the second in green, and the third in blue.

\section*{Example}
\[
\text { rgbpl ot ( } \mathrm{j} \text { et ) }
\]


See Also
col ormap in the MATLAB Function Reference

\section*{Purpose}

\section*{Syntax}

\section*{Description}

\section*{Class Support}

Select region of interest, based on color
\(B W=\) roi col or (A, low, hi gh)
\(B W=r o i \operatorname{col} \operatorname{or}(A, v)\)
roi col or selects a region of interest within an indexed or intensity image and returns a binary image. (Y ou can use the returned image as a mask for masked filtering using roi filt 2.)
\(\mathrm{BW}=\mathrm{roi} \operatorname{col}\) or (A, I ow, hi gh) returns a region of interest selected as those pixels that lie within the col ormap range [I ow hi gh].
\[
B W=(A>=1 \text { ow }) \&(A<=h i g h)
\]

BWis a binary image with 0's outside the region of interest and 1's inside.
\(B W=\) roi col or (A, v) returns a region of interest selected as those pixels in A that match the values in vector v. BWis a binary image with l's where the values of \(A\) match the values of \(v\).

The input array A can be of class doubl e or of any integer class. The output array BWis of class ui nt 8 .


See Also roifilt2, roi poly

Purpose Smoothly interpolate within an arbitrary image region
\begin{tabular}{|c|c|}
\hline \multirow[t]{4}{*}{Syntax} & \(\mathrm{J}=\) roifill \((\mathrm{l}, \mathrm{c}, \mathrm{r})\) \\
\hline & \(\mathrm{J}=\) roifill (I) \\
\hline & \(\mathrm{J}=\) roifill (I, BW) \\
\hline & [ \(\mathrm{J}, \mathrm{BW}\) = roifill( \(\ldots\) ) \\
\hline & \(J=r o i f i l l(x, y, l, x i, y i)\) \\
\hline & \([\mathrm{x}, \mathrm{y}, \mathrm{J}, \mathrm{BW} \mathrm{xi}, \mathrm{yi}]=\mathrm{roifi}\) \\
\hline
\end{tabular}
roifill fills in a specified polygon in an intensity image. It smoothly interpolates inward from the pixel values on the boundary of the polygon by solving Laplace's equation. roi fill can be used, for example, to "erase" small objects in an image.
\(J=r\) oifill (I, c, r) fills in the polygon specified by cand \(r\), which are equal-length vectors containing the row-column coordinates of the pixels on vertices of the polygon. The \(k\) - \(t h\) vertex is the pixel \((r(k), c(k))\).

J = roifill(I) displays the imagel on the screen and lets you specify the polygon using the mouse. If you omit I, roi fill operates on the image in the current axes. Use normal button clicks to add vertices to the polygon. Pressing Backspace or Delete removes the previously selected vertex. A shift-click, right-click, or double-click adds a final vertex to the selection and then starts the fill; pressing Return finishes the selection without adding a vertex.
\(\mathrm{J}=\) roifill (I, BW uses BW(a binary image the same size as I ) as a mask. roi fill fills in the regions in I corresponding to the nonzero pixels in BW If there are multiple regions, roifill performs the interpolation on each region independently.
[ \(\mathrm{J}, \mathrm{BW}\) = roifill(...) returns the binary mask used to determine which pixels in I get filled. BWis a binary image the same size as I with 1's for pixels corresponding to the interpolated region of \(I\) and 0 's elsewhere.
\(\mathrm{J}=\mathrm{r}\) oi fill(x,y,l,xi,yi) uses the vectors x and y to establish a nondefault spatial coordinate system. xi and yi are equal-length vectors that specify polygon vertices as locations in this coordinate system.
\([\mathrm{x}, \mathrm{y}, \mathrm{J}, \mathrm{BW} \mathrm{xi}, \mathrm{yi}]=\) roifill(...) returns the XDat a and YDat a in x and y ; the output image in J ; the mask image in BW and the polygon coordinates in xi and yi . xi and yi are empty if the roifill (I, BWV form is used.

If roifill is called with no output arguments, the resulting image is displayed in a new figure.

Class Support The input image I can of class ui nt 8, ui nt 16, or doubl e. The binary mask BW can be of class ui nt 8 or doubl e. The output imageJ is of the same class as I. All other inputs and outputs are of class doubl e.

\section*{Example}
```

| = imead(' ei ght.tif');
c = [222 272 300 270 221 194];
r = [21 21 75 121 121 75];
J = roifill(l,c,r);
i mshow(1)
figure, i mshow(J)

```


See Also roifilt2, roi poly

\section*{Purpose}

\section*{Syntax}

\section*{Description}

\section*{Class Support}

\section*{Filter a region of interest}
\[
\begin{aligned}
& J=\text { roifilt } 2(h, I, B W \\
& J=\text { roifilt } 2(I, B W \text { fun }) \\
& J=\text { roifilt } 2(I, B W \text { fun, } P 1, P 2, \ldots)
\end{aligned}
\]
\(\mathrm{J}=\) roifilt2(h, I, BW filters the data in I with the two-dimensional linear filter h. BWis a binary image the same size as I that is used as a mask for filtering. roi filt 2 returns an image that consists of filtered values for pixels in locations where BWcontains 1's, and unfiltered values for pixels in locations where BWcontains 0's. For this syntax, roifilt 2 calls filter 2 to implement the filter.
\(\mathrm{J}=\) roifilt2(I, BW fun) processes the data in I using the function fun. The result J contains computed values for pixels in locations where BWcontains 1's, and the actual values in I for pixels in locations where BWcontains 0's.
f un can be a functi on_handl e, created using @ or an inline object. f un should take a matrix as a single argument and return a matrix of the same size.
\[
y=f u n(x)
\]

J = roifilt2(I, BWfun, P1, P2, ...) passes the additional parameters P1, P2, ..., to \(f\) un.

For the syntax that includes a filter \(h\), the input image \(l\) can be of class ui nt 8 , ui nt 16 , or doubl e, and the output array J is of class doubl e. F or the syntax that includes a function, l can be of any class supported by \(f\) un, and the class of \(J\) depends on the class of the output from \(f\) un.

Example This example continues the roi pol y example.
```

| = immead('ei ght.tif');
c =[ 222 272 300 270 221 194];
r =[llllllllll}121 121 75]
BW = roi pol y(I,c,r);
h = fspeci al('unsharp');
J = roifilt2(h,l,BW);
imshow(J), fi gure, imshow(J)

```

\section*{See Also \\ filter 2, roi poly}

\section*{Purpose Select a polygonal region of interest}
\begin{tabular}{ll} 
Syntax & \(B W=\) roi pol \(y(I, c, r)\) \\
& \(B W=\) roi pol \(y(I)\)
\end{tabular}\(\quad\)\begin{tabular}{l} 
BW \(=\) roi pol \(y(x, y, I, x i, y i)\) \\
{\([B W x i, y i]=\) roi pol \(y(\ldots)\)} \\
{\([x, y, B W x i, y i]=r o i \operatorname{pol} y(\ldots)\)}
\end{tabular}

\section*{Description}

Use roi pol y to select a polygonal region of interest within an image. roi pol y returns a binary image that you can use as a mask for masked filtering.
\(B W=r\) oi pol \(y(I, c, r)\) returns the region of interest selected by the polygon described by vectors c and \(r\). BWis a binary image the same size as I with 0's outside the region of interest and 1 's inside.
\(B W=\) roi pol \(y(I)\) displays the image \(I\) on the screen and lets you specify the polygon using the mouse. If you omit I, roi pol y operates on the image in the current axes. Use normal button clicks to add vertices to the polygon. Pressing Backspace or Delete removes the previously selected vertex. A shift-click, right-click, or double-click adds a final vertex to the selection and then starts the fill; pressing Return finishes the selection without adding a vertex.
\(B W=\) roi pol \(y(x, y, I, x i, y i)\) uses the vectors \(x\) and \(y\) to establish a nondefault spatial coordinate system. xi and yi are equal-length vectors that specify polygon vertices as locations in this coordinate system.
[ BW xi , yi ] = roi pol \(\mathrm{y}(\ldots\). . ) returns the polygon coordinates in xi and yi . Note that roi pol y always produces a closed polygon. If the points specified describe a closed polygon (i.e., if the last pair of coordinates is identical to the first pair), the length of \(x i\) and \(y i\) is equal to the number of points specified. If the points specified do not describe a closed polygon, roi pol y adds a final point having the same coordinates as the first point. (In this case the length of xi and yi is one greater than the number of points specified.)
\([x, y, B W x i, y i]=r\) oi pol \(y(\ldots)\) returns the XDat a and YDat a in \(x\) and \(y\); the mask image in BW and the polygon coordinates in xi and yi .

If roi pol y is called with no output arguments, theresulting image is displayed in a new figure.

\section*{Class Support}

The input image I can be of class ui nt 8, ui nt 16, or doubl e. The output image BWis of class ui nt 8 . All other inputs and outputs are of class doubl e.

Remarks

Example
```

| = imead('ei ght.tif');
c = [ 222 272 300 270 221 194];
r =[[21 21 75 121 121 75];
BW = roi pol y(I,c,r);
i mshow(I)
figure, inshow BW)

```


\footnotetext{
See Also roifilt2, roicolor, roifill
}
\begin{tabular}{|c|c|}
\hline Purpose & Compute the standard deviation of the elements of a matrix \\
\hline Syntax & \(b=s t d 2(A)\) \\
\hline Description & \(b=s t d 2(A)\) computes the standard deviation of the values in A. \\
\hline Class Support & A is an array of class doubl e or of any integer class. b is a scalar of class doubl e. \\
\hline Algorithm & st d2 computes the standard deviation of the array A using std(A( ) ) . \\
\hline See Also & cor r2, mean2 \\
\hline & std, mean in the MATLAB Function Reference \\
\hline
\end{tabular}

Purpose Display multiple images in the same figure
\begin{tabular}{ll} 
Syntax & subi mage \((X\), nap \()\) \\
& subi mage（ \()\) \\
& subi mage（ \(B W\) \\
& subi mage \((R G B)\) \\
& subi mage \((x, y, \ldots)\) \\
& \(h=\operatorname{subi}\) mage（ \(\ldots\) ）
\end{tabular}

\section*{Description}

Class Support The input image can be of class ui nt 8，ui nt 16，or doubl e．

\section*{Example}

You can use subi mage in conjunction with subpl ot to create figures with multiple images，even if the images have different colormaps．subi mage works by converting images to truecol or for display purposes，thus avoiding col ormap conflicts．
subi mage（ \(X, n \notin p\) ）displays the indexed image \(X\) with colormap map in the current axes．
subi mage（I）displays the intensity imagel in the current axes．
subi mage（ BWY displays the binary image BWin the current axes．
subi mage（ RGB）displays the truecol or image RGB in the current axes．
subi mage（ \(x, y . .\). ）displays an image using a nondefault spatial coordinate system．
h＝subi mage（ ．．．）returns a handle to an image object．

\section*{I oad trees}
［ X2，map2］＝imread（＇forest．tif＇）；
subpl ot（ \(1,2,1\) ），subi mage（ \(X, n \not ⿴ 囗 十\) ）
subpl ot（ \(1,2,2\) ），subi mage（ \(X 2, n \not ⿴ 囗 十)\)

\section*{subimage}


\section*{See Also}
ins how
subpl ot in the MATLAB Function Reference
Purpose Adjust display size of an image
Syntax truesize(fig,[mows ncol s]) truesi ze(fig)
DescriptionRemarks
See Alsoi mshow, i pt set pr ef, i pt get pref

Purpose Convert data to unsigned 8-bit integers

\section*{Syntax \(\quad B=\) ui nt 8( A)}

Description \(\quad B=u i \operatorname{nt} 8(A)\) creates the unsigned 8-bit integer array B from the array A. If A is a ui nt 8 array, B is identical to A .

The elements of a ui nt 8 array can range from 0 to 255 . Values outside this range are mapped to 0 or 255 . If \(A\) is already an unsigned 8 -bit integer array, ui nt 8 has no effect.

The fractional part of each value in A is discarded on conversion. This means, for example, that ui nt 8(102. 99) is 102, not 103. Therefore, it is often a good idea to round off the values in A before converting to ui nt 8 . F or example,
\[
B=\text { ui nt } 8(\operatorname{round}(A))
\]

MATLAB supports these operations on ui nt 8 arrays:
- Displaying data values
- Indexing into arrays using standard MATLAB subscripting
- Reshaping, reordering, and concatenating arrays, using functions such as reshape, cat, and per mute
- Saving to and loading from MAT-files
- The all and any functions
- Logical operators and indexing
- Relational operators

MATLAB also supports the find function for ui nt 8 arrays, but the returned array is of class doubl e.

Most of the functions in the I mage Processing Tool box accept ui nt 8 input. See the individual reference entries for information about ui nt 8 support.

Remarks ui nt 8 is a MATLAB built-in function.

\section*{Example}

See Also
a \(=\left[\begin{array}{lll}1 & 3 & 5\end{array}\right] ;\)
b = ui nt 8(a) ;
whos
Name Si ze Bytes Cl ass
    a \(1 \times 3\)
    b \(1 \times 3\)
    24 doubl earray
    3 ui nt 8 array
    double, i m2double, i mqui nt 8
Purpose Convert data to unsigned 16-bit integers
Syntax ..... I = ui nt 16(X)
Description I = ui nt 16(X) converts the vector X into an unsigned 16 -bit integer. X can beany numeric object (such as a doubl e). The elements of a ui nt 16 range from 0to 65535 . Values outside this range are mapped to 0 or 65535 . If X is al ready anunsigned 16-bit integer array, ui nt 16 has no effect.
The ui nt 16 class is primarily meant to be used to store integer values. Hence most operations that manipulate arrays without changing their elements are defined, for example, the functions reshape and si ze, the relational operators, subscripted assignment, and subscripted reference. While most MATLAB arithmetic operations cannot be performed on ui nt 16 data, the following operations are supported: sum conv2, convn, fft 2 , and fftn . In these cases the output will always be doubl e. If you attempt to perform an unsupported operation you will receive an error such as Function ' + ' not defined for variables of class 'ui nt 16'.
You can define your own methods for ui nt 16 (as you can for any object) by placing the appropriately named method in an @ui nt 16 directory within a directory on your path.
Other operations and functions supported for ui nt 16 data include:
- Displaying data values
- Indexing into arrays using standard MATLAB subscripting
- Logical operators
- Saving to and loading from MAT-files
- The functions cat, per mite, al I, and any
M ost functions in the Image Processing Tool box accept ui nt 16 input. See the individual reference entries for information about ui nt 16 support.
Class Support The input image can be of class ui nt 8 or doubl e.
Remarks ui nt 16 is a MATLAB built-in function.

\section*{Example}

See Also
a \(=\left[\begin{array}{lll}1 & 3 & 5\end{array}\right] ;\)
\(b=\) ui nt \(16(a) ;\)
whos
Name
\begin{tabular}{clr} 
a & Si ze & \(1 \times 3\)
\end{tabular}
\begin{tabular}{ll} 
b & \(1 \times 3\)
\end{tabular}
doubl e, ui nt 8 , ui nt 32 , i nt 8 , int 16, int 32

\section*{Purpose Display an image as a texture-mapped surface}
Syntax \(\quad\)\begin{tabular}{ll}
\(\operatorname{war} p(X, n \not a p)\) \\
& \(\operatorname{war} p(I, n)\) \\
& \(\operatorname{war} p(B W)\) \\
& \(\operatorname{war} p(R G B)\) \\
& \(\operatorname{war} p(z, \ldots)\) \\
& \(\operatorname{war} p(x, y, z, \ldots)\) \\
& \(h=\operatorname{war} p(\ldots)\)
\end{tabular}

Description war \(p(X, n \notin p)\) displays the indexed image \(X\) with col ormap map as a texture map on a simple rectangular surface.
war \(p(1, n)\) displays the intensity image I with gray scale col ormap of length \(n\) as a texture map on a simple rectangular surface.
war p( BW displays the binary image BWas a texture map on a simple rectangular surface.
war \(p\) ( RGB) displays the RGB image in the array RGB as a texture map on a simple rectangular surface.
war \(p(z, \ldots)\) displays the image on the surface \(z\).
war \(p(x, y, z \ldots)\) displays the image on the surface ( \(x, y, z\) ).
\(h=\operatorname{war} p(\ldots)\) returns a handle to a texture mapped surface.
Class Support The input image can be of class ui nt 8, ui nt 16, or doubl e.
Remarks Texture-mapped surfaces generally render more slowly than images.
Example This example texture maps an image of a test pattern onto a cylinder.
```

[ x,y,z] = cyl inder;
| = imread('testpat 1.tif');
warp(x,y,z,l);

```


\section*{See Also}
i mshow
i mage, i magesc, surf in the MATLAB Function Reference

Purpose
Syntax

Description

Example

\section*{Algorithm}

Class Support The input imagel can be of class ui nt 8, ui nt 16, or doubl e. The output image J is of the same class as I.
Perform two-dimensional adaptive noise-removal filtering
\(\mathrm{J}=\) wi ener \(2(\mathrm{I},[\mathrm{m} \mathrm{n}]\), noi se)
[J, noi se] = wi ener 2(I,[mn])
wi ener 2 lowpass filters an intensity image that has been degraded by constant power additive noise. wi ener 2 uses a pixel-wise adaptive Wiener method based on statistics estimated from a local neighborhood of each pixel.
\(\mathrm{J}=\) wi ener 2(I, [mn], noi se) filters the imagel using pixel-wise adaptive Wiener filtering, using neighborhoods of size mby-n to estimatethe local image mean and standard deviation. If you omit the [ mn ] argument, mand n default to 3. The additive noise (Gaussian white noise) power is assumed to be noi se.
[ ] , noi se] = wi ener 2( \(\mathrm{I},[\mathrm{mn}\) ]) also estimates the additive noise power before doing the filtering. wi ener 2 returns this estimate in noi se.

Degrade and then restore an intensity image using adaptive Wiener filtering.
I = imread('saturn.tif');
\(\mathrm{J}=\mathrm{imoi}\) se(I,'gaussi an' \(, 0,0.005\) );
K = wi ener2(J,[5 5]);
i mshow J )
figure, inshow (K)

wi ener 2 estimates the local mean and variance around each pixel
\[
\begin{aligned}
& \mu=\frac{1}{N M} \sum_{n_{1}, n_{2} \in \eta} a\left(n_{1}, n_{2}\right) \\
& \sigma^{2}=\frac{1}{N M} \sum_{n_{1}, n_{2} \in \eta} a^{2}\left(n_{1}, n_{2}\right)-\mu^{2}
\end{aligned}
\]
where \(\eta\) is the \(N\)-by- \(M\) local neighborhood of each pixel in the image \(A\). wi ener 2 then creates a pixel-wise Wiener filter using these estimates
\[
\mathrm{b}\left(\mathrm{n}_{1}, \mathrm{n}_{2}\right)=\mu+\frac{\sigma^{2}-v^{2}}{\sigma^{2}}\left(\mathrm{a}\left(\mathrm{n}_{1}, \mathrm{n}_{2}\right)-\mu\right)
\]
where \(v^{2}\) is the noise variance. If the noise variance is not given, wi ener 2 uses the average of all the local estimated variances.
\begin{tabular}{ll} 
See Also & filter 2, nedfilt 2 \\
Reference & {\([1]\) Lim, J ae S. Two-Dimensional Signal and Image Processing. Englewood } \\
& Cliffs, NJ : Prentice Hall, 1990. pp. 536-540.
\end{tabular}

\section*{ycbcr2rgb}

\section*{Purpose Convert YCbCr values to RGB col or space}
\begin{tabular}{ll} 
Syntax & \(r g b n \boxplus p=y c b c r 2 r g b(y c b c r n \boxplus p)\) \\
& \(R G B=y c b c r 2 r g b(Y C B C R)\)
\end{tabular}

Description rgbmap \(=y c b c r 2 r g b(y c b c r m p)\) converts the YCbCr values in the col ormap ycbcr map to the RGB color space. If ycbcr map is mby-3 and contains the YCbCr luminance \((\mathrm{Y})\) and chrominance ( Cb and Cr ) color components as its columns, then rgbmap is returned as an mby-3 matrix that contains the red, green, and blue values equivalent to those colors.

RGB \(=\) ycbcr \(2 \mathrm{rgb}(\mathrm{YCBCR})\) converts the YCbCr image YCBCR to the equivalent truecolor image RGB.

\section*{Class Support If the input is a YCbCr image, it can be of class ui nt 8 , ui nt 16, or doubl e; the output image is of the same class as the input image. If the input is a colormap, the input and output col ormaps are both of class doubl e.}

See Also ntsc2rgb,rgb2ntsc,rgb2ycbcr
\begin{tabular}{ll} 
Purpose & \begin{tabular}{l} 
Zoom in and out of an image \\
Syntax \\
zoom on \\
zoom of \(f\) \\
zoom out \\
zoom reset \\
zoom \\
zoom xon \\
zoom yon \\
zoomf fact or ) \\
zoom fi g, opt i on)
\end{tabular} \\
zoom on turns on interactive zooming for the current figure. When zooming is \\
enabled, clicking the mouse on a point within an axes changes the axes limits \\
by a factor of 2, to either zoom in on or out from the point:
\end{tabular}
zoom fi g , opt i on) applies the zoomcommand to the figure specified by fi g . opt \(i\) on is a string containing any of the above arguments. If you do not specify a figure, zoomworks on the current figure.

See Also imerop

\section*{Working with Function Functions}

\author{
Passing an M-File Function to a Function Function \\ A-3 \\ Passing an Inline Object to a Function Function . . . . . . A-4 \\ Passing a String to a Function Function . . . . . . . . . A-4
}

The Image Processing Tool box contains several functions called function functions, so named because they enable you to supply one of your own functions as an input argument. F or example, bl kpr oc enables you to input your own block processing function, and qt decomp enables you to input your own algorithm for defining a criterion of homogeneity. This section shows you the different ways in which you can input your own function to a function function.

Note As you may know, MATLAB has a directory named f unf un containing function functions. However, the function functions of the I mage Processing Toolbox are not included in this directory. For a discussion of the MATLAB functions in f unf un, see the section in the MATLAB documentation entitled "Function Functions."

There are three different methods for passing your own function to a function function:
- Pass in a function handle to an M-file function
- Pass in an inline function
- Pass in a string containing an expression

This appendix contains three examples - one to demonstrate each method.

Note Function handles are a new class in MATLAB 6.0. One advantage to using them is that you can call a function function with a function handle to a private function or subfunction. In previous versions of MATLAB, your function had to be on the MATLAB path. For more information, see funct i on_handl e in the MATLAB Function Reference.

All three examples use the function function bl kproc. The following bl kproc syntax variation is used.
\[
B=B L K P R O C(A,[m n], f u n, P 1, P 2, \ldots)
\]

This syntax takes as its arguments an image A , a block size[ mn ] used to divide the image, and a function \(f\) un, which is used to process each block. This syntax also takes any number of parameters (P1, P2, etc.) that may be needed by f un.

All three examples use the same simple function to alter the brightness of a grayscale image.
\[
f(x)=x \times P 1
\]
\(x\) represents a block of size [ m n ], and P1 can take any value. Note that this function was chosen because it works well for illustrative purposes; if you really want to brighten an image, you should use the i madj ust function.

\section*{Passing an M-File Function to a Function Function}

Create an M-file containing your block-processing function. Using the example function above, your \(M\)-file might contain the following lines.
function \(y=m y b l\) kf \(u n(x, P 1)\)
\% For an input block of \(x\), di vi de the pi xel val ues by P1.
\% Temporarily make \(x\) double so you can performarithmetic on it.
\(y=\) ui nt 8( doubl e(x)*P1);
To use your M -file with bl kproc, create a function handle (f unct i on_handl e) to it, and pass in the handle and any desired value for P1. F or example,

I = imead(' camer anmen.tif');
\(\mathrm{f}=\) @nybl kf un; \% Create a function handle.
12 = bl kproc(l, [10 10], f, 2);
imshow (1);
figure, inshow(12);


Figure A-1: Original Image (left) and Brightened Image (right)

\section*{Passing an Inline Object to a Function Function}

Create an inline object at the MATLAB prompt. Pass the inline object and any desired value for P1 to bl kproc. For example,
mybl kf un = inline('uint 8( (double(x)*2) )', 1);
l = imead(' camer aman.tif');
l2 = bl kproc(l,[10 10], mybl kfun, 2);
The results are the same as those shown in Figure A-1. F or more information about inline functions, see the online MATLAB reference page for i nl i ne.

\section*{Passing a String to a Function Function}

You can also pass an expression to a function function. J ust set the f un parameter to a string containing your expression. For example,

I = imead('camer aman.tif');
\(12=\) bl kproc(I,[10 10], 'ui nt8((double(x)*2))');
The results are the same as those shown in Figure A-1.

\section*{Numerics}

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[^0]:    Note For the most up-to-date information about system requirements, see the system requirements page, available in the products area at the MathWorks Web site (ht t p: / / www. mat hwor ks. com).

[^1]:    bw= $3>0$. 2; \% Make 13 bi nary using a threshol d val ue of 0.2 .
    fi gure, inshow bw)

[^2]:    i mฐhow RGB( : , : : , 7) ) ;

[^3]:    1. The zero-frequency coefficient, $\mathrm{F}(0,0)$ is often called the "DC component." DC is an electrical engineering term that stands for direct current.
[^4]:    Class Support For syntax variations that includean input image(rather than a colormap), the input image can be of class ui nt 8 , ui nt 16, or doubl e. The output image has the same class as the input image. For syntax variations that include a colormap, the input and output colormaps are of class doubl e.

[^5]:    ' Ori ent at i on' - Scalar; the angle (in degrees) between the x-axis and the major axis of the ellipse that has the same second-moments as the region.

