## A computational feature binding model

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- 2 The competitive layer model
- 3 Feature Extraction
- 4 The CLM texture segmentation model







#### Introduction

The competitive layer model Feature Extraction The CLM texture segmentation model Results Conclusions

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# **Binding Problem**

#### Overview

Information processing in the human brain is highly parallel. This means that different features of an object are processed in different parts of the brain.







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#### Overview

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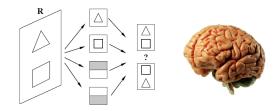


Figure: Binding Problem Illustration [Rosenblatt, 62]



#### Introduction

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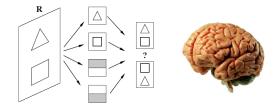


Figure: Binding Problem Illustration [Rosenblatt, 62]

#### Question?

How features that are processed in parallel are bound to the one unique percept?



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The competitive layer model

#### Principles

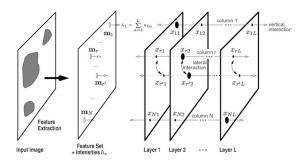
- Finite set of features: Representation of the structure of the sensory input.
- Measure of the mutual compatibility: Gestalt Laws.

#### Objective

To use these compatibilities to partition the input features into salient groups by the recurrent dynamics in a layered neural network with topographically structured competitive and cooperative interactions.



## The competitive layer model

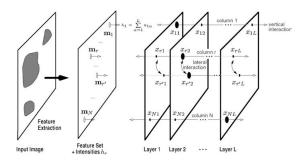


#### Architecture

Image positions:  $r = (x, y) \in I$ Stimulus:  $m_r$  - spatial, texture or edge information. Significance of the detection feature:  $h_r$ 



## The competitive layer model



#### Architecture

Number of Layers: *L* Number of formal neurons with nonnegative activity  $x_{r\alpha} \ge 0$ : *N* Superposition condition:  $\sum_{\alpha=1}^{L} x_{r\alpha} \approx h_r$ 

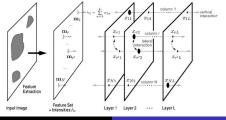
The competitive layer model

### Energy function

$$E = \frac{J}{2} \Sigma_r (\Sigma_\beta x_{r\beta} - h_r)^2 + \frac{1}{2} \Sigma_\alpha \Sigma_{rr'} f_{rr'} x_{r\alpha} x_{r'\alpha}$$

#### Interaction function

$$\dot{x_{r\alpha}} = -x_{r\alpha} + \sigma (J(h_r - \Sigma_\beta x_{r\beta}) + \Sigma_{r'} f_{rr'} x_{r'\alpha})$$
  
where  $\sigma(x) = max(x, 0)$  and  $f(m_r, m_{r'} = f_{rr'})$ 





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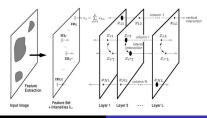
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### The competitive layer model

#### Image Segmentation

- Initialize all  $x_{r\alpha}$  with small random values  $x_{r\alpha}(t=0) \in [h_r/L \epsilon, h_r/L + \epsilon]$
- **2** Do *NL* times: choose  $(r, \alpha)$  randomly and update  $x_{r\alpha} = max(0, \xi)$ , where  $\xi = \frac{J(h_r \Sigma_{\beta \neq \alpha} x_{r\beta}(t)) + \Sigma_{r' \neq r} f_{rr'} x_{r'\alpha}(t))}{J f_{rr'}}$

**③** Go to step 2 until convergence





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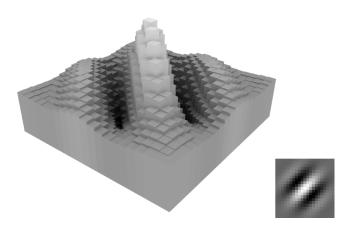
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# Multiscale Filtering





# Multiscale Filtering

#### 2D Gabor Filters

$$g(x,y) = e^{\left(\frac{(x-x_0)^2}{2\sigma_x^2} + \frac{(y-y_0)^2}{2\sigma_y^2}\right)} e^{-ik(x-x_0)}$$

### 2D Gabor Filters

Center of the receptive field:  $(x_0, y_0)$ Widths of the Gaussian envelope along the x- and y-axes:  $\sigma_x$  and  $\sigma_y$ Spatial frequency of a complex plane wave with wave normal along the x-axis and wavelength  $\lambda$ :  $k = 2\pi/\lambda$ 



# Multiscale Filtering

#### 2D Gabor Filters

$$g(x,y) = e^{\left(\frac{(x-x_0)^2}{2\sigma_x^2} + \frac{(y-y_0)^2}{2\sigma_y^2}\right)} e^{-ik(x-x_0)}$$

#### Gabor Wavelets

$$g_{mn} = g(x', y')$$
  
 $x' = a^{-m}(x \cos \Theta_n + y \sin \Theta_n)$  and  
 $y' = a^{-m}(-x \sin \Theta_n + y \cos \Theta_n)$ 

#### Gabor Wavelets

A sparse sampling of the phase space (which is spanned by m, n,  $x_0$  and  $y_0$ ) is sufficient for a complete representation of arbitrary image data.



# Multiscale Filtering

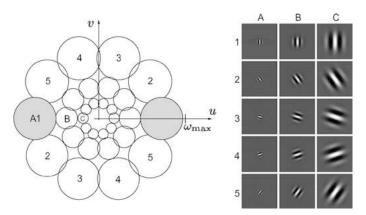


Figure: Set of 2D Gabor Filters for Feature Extraction



# Multiscale Filtering

### Algorithm

- Compute a set of 2D Gabor filters tuned to five different orientations and three scales.
- For each element of the filter bank, compute its response image, or channel, c<sub>mn</sub> to the given input.
- Apply the nonlinear contrast transfer function to each channel c<sub>mn</sub>, yielding c<sup>CTF</sup><sub>mn</sub>.
- Compute the texture features  $\mu_{mn}$  and  $\sigma_{mn}$  for each of the 15 channels according to steps (3) and (4).

$$\mu_{mn} = c_{mn}^{CTF} * gs_{mn}(x, y)$$
  
$$\sigma_{mn} = \sqrt{(c_{mn}^{CTF} - \mu_{mn})^2 * gs_{mn}(x, y)}$$

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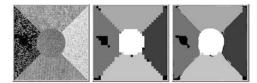
## The CLM texture segmentation model

#### Multi-dimensional scaling

Feature space: 30-dimensional hyperellipsoid  $t_r$ Principal component analysis: 4-dimensional  $p_r$ 

#### Feature subsampling

Image 256 × 256 pixels: 65536 features 1024 8 × 8 regions: 1024 4D feature vectors  $p_r$ Nearest neighbour:  $|p_r - p_{near}| + |r - r_{near}| = min$ .



# The CLM texture segmentation model

#### Interaction matrix

$$f_{rr'} = e^{-\frac{d_{text}(r,r')^2}{R_{sim}^2}} + ce^{-\frac{|x_r - x_{r'}|^2}{R_{prox}^2}} - k$$
$$d_{text}(r,r') = \sqrt[n]{\sum_{i=1}^4 \left(\frac{|p_r^i - p_{r'}^i|}{\sqrt{\sigma(p^i)}}\right)^n}$$

### CLM's output

$$x_{r\alpha} = h_r + \frac{1}{J_1} \sum_{r'} f_{rr'} x_{r'\alpha}$$
 or  $x_{r\alpha} = 0$   
Threshold:  $1/2h_r$ 



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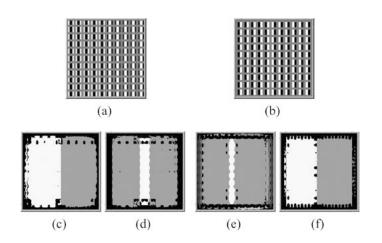
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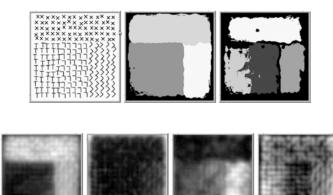


## Artificial Textures





### Artificial Textures



(a) 1st



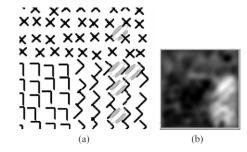
(c) 3rd



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(d) 4th

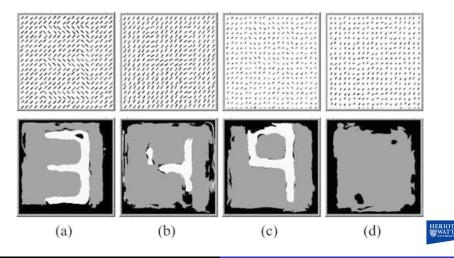
## Artificial Textures



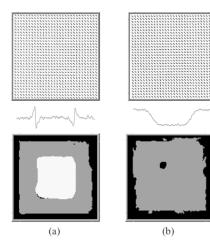


Conclusions

# Edge- and region-based phenomena

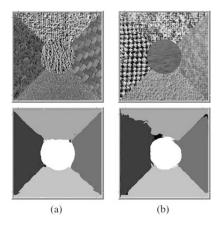


# Edge- and region-based phenomena



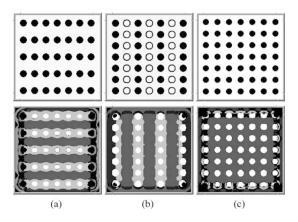


## Natural textures





### Gestalt laws





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# Conclusions

- A feature extraction algorithm was developed to produce meaningful texture descriptor.
- OLM Model reproduces edge-based as well as region-based phenomena.
- The incorporation of Gestalt laws offers an interesting perspective to describe saliency groups.
- Parameters tuning process was not necessary.
- Model can mimic a large variety of human perception phenomena.





 Jorg Ontrup and Heiko Wersing and Helge J. Ritter. A computational feature binding model of human texture perception. Cognitive Processing. pp. 31-44. 2004.

